δ-doped LaAlO₃-SrTiO₃ interface: Electrical transport and characterization of the interface potential

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Here we investigate LaAlO₃-SrTiO₃ heterostructure with δ -doping of the interface by LaMnO₃ at less than one monolayer. This doping strongly inhibits the formation of mobile electron layer at the interface. This results in giant increase of the resistance and the thermopower of the heterostructure. Several aspects of this phenomena are investigated. A model to calculate the carrier concentration is presented and effect of doping and detailed temperature dependence is analyzed in terms of model parameters and the weak-scattering theory. The large enhancement of thermopower is attributed to the increased spin and orbital entropy originating from the LaMnO_3 mono-layer.

The recent discovery of a highly mobile twodimensional electron liquid (2-DEL) at the interface of two perovskite oxides has naturally evoked a huge amount of interest[1–3]. These heterostructures have since been widely investigated both experimentally and theoretically, (a) to understand the mechanism of formation of 2-DEL [4–7] (b) to investigate its properties and examine new phenomena exhibited by it [8–11] and (c) for exploitation of its unique properties for technological ends [12, 13]. Here we contribute to this effort by investigating a δ -doped interface. We have prepared an interface of SrTiO₃ and LaAlO₃ with δ -doping of a sublayer of LaMnO_3 at the interface. Fig. 1a shows the layer structure of our system.

Our motivation was to seek a material structure with improved thermoelectric performance. The quantum size effect in low-dimensional systems is now well known to enhance thermopower [14, 15]. Ohtomo et al [16]. investigated superlattices of $SrTiO₃$ and $LaTiO₃$ and showed that at interfaces the Ti ion exist in mixed valence states $(Ti^{3+}$ and Ti^{4+}). Such mixed-valent states along with strong correlations have interesting consequences for the enhancement of TEP, as earlier work [17–19] has shown that large contribution can come from spin and orbital degrees of freedom.

In the present work, we report electrical transport, the resistance and the thermoelectric power in a series of LaAlO₃-SrTiO₃ oxide hetero-structures with δ -doping by a fraction of a single monolayer of Mn ions in the vicinity of the interface. Our key finding is that this sublayer has a drastic effect on the properties of the interface. The resistance and thermopower increase considerably compared to the undoped interface. These effects are undoubtedly related to the mechanism of formation of the nearly two-dimensional electron liquid (2-DEL) at the interface. We find that our set of measurements offer an opportunity to develop a simple model which extends the standard polar-catastrophe ideas. While interface physics is rather complex due to several factors, like relaxation of ionic positions, resulting electrostatic forces, disorder and other interface reconstruction effects, our

simple analysis of transport properties does pave way for a better understanding of some key issues of the interface physics.

Pulsed laser deposition (with KrF laser of wavelength 248 nm) technique has been employed for layer by layer growth of $LaAlO₃$ films on TiO₂ terminated (001) oriented $SrTiO₃$ single crystal substrate. To tailor atomically sharp interfaces, growth parameters such as O_2 partial pressure and substrate temperature have been critically examined since these parameters determine the film stoichiometry and defects [20–22]. The substrate was kept 7 cm away from the target. The laser pulses were fired at 2 Hz and flunce \sim 1 J cm⁻² per pulse, which leads to a growth rate of \sim 0.15 Å/s. Further details of growth are described in our earlier publications [23, 24]. A fraction δ ($0 \le \delta \le 0.6$) of a monolayer of LaMnO₃ was first deposited on the $TiO₂$ terminated $SrTiO₃$ substrate at 10^{-4} mbar of O₂ pressure and 800 ^oC, followed by 20 u.c. thick $LaAlO₃$ film. Sample was thereafter cooled under the same deposition pressure. These heterostructures were characterized by X-ray diffraction on PANalytical X'PERT PRO, revealing a tetragonal strained perovskite structure. Top electrodes of Ag/Cr were deposited in Van der Pauw and standard four probe geometry on films using shadow masking. The thermoelectric measurements were carried out in the Quantum Design PPMS.

In order to describe various effects of the Mn-layer on the formation of the interfacial 2-DEL, we begin with the observation that no interfacial electronic conductivity was observed when LaMnO_3 films of several unit cells were deposited on $TiO₂$ terminated $SrTiO₃$ substrates [25]. The interfacial conduction could be observed only with less than one layer of LaMnO_3 . This implies a unit cell consisting of one layers $Mn_{\delta}Al_{1-\delta}O_2$ and LaO at the interface as shown in Fig. 1(a). Whereas for LAO-STO system a minimum of 4 to 5 unit cells of LAO are required on TiO2-terminated substrate of STO to form a 2-DEL, for the doped interface the minimum number of LAO unit cells required to achieve the same is a lot larger and strongly depends on the Mn concentration in the layer. Fig.1(b) shows the change of sheet resistance on decreas-

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ing the LAO thickness for $\delta = 0.5$. One sees that R_{\Box} at room temperature increases sharply by three orders in magnitude as the LAO thickness decreases from 20 to 10 u.c. The presence of even half a monolayer of LaMnO_3 changes the number of LAO layers required to achieve a good conducting 2-DEL, to 17 to 20 as compared to 4 to 5 for STO-LAO interface. To further confirm this finding, we reduced the LaMnO₃ to monolayer fraction $\delta = 0.2$. Here we find that ≈ 13 - 15 u.c., were required to make the interface conducting. Moreover, for $\delta > 0.5$, we find that the system remains insulating for 20 u.c., of $LaAlO₃$. The variation in $R_{\Box}(T)$ as a function of LaMnO₃ monolayer fraction (δ) for a fixed LaAlO₃ over-layer (20 u.c.) is shown in Fig.1(c). We see a very rapid rise in resistance when δ exceeds 0.2, confirming again that the LaMnO₃ monolayer inhibits the formation of 2-DEL at the interface in a strong way. The $Fig.1(d)$ shows the variation of the sheet resistance (R_{\Box}) with temperature in the range 2K to 300K for five films with monolayer Mn-doping in the range $0 \le \delta \le 0.5$ and an optimal LAO thickness of 20 u.c.. The data is also shown for $\delta = 0.6$, at which doping the interface is non-metallic. All the curves show a minimum in temperature range of 40K to 50K. The decrease from room temperature to the minimum is rather sharp, the resistance decreasing by a factor of about 7 to 8. At lower temperatures there is a slow increase of resistance suggesting a weak-scattering regime. In order

Figure 1: Color online: (a) shows interface of STO and LAO with δ -doping of a fraction of monolayer of LaMnO₃. Note that the second layer from the interface on LAO side is Mn_δAl_{1−δ}. (b) Variation of room temperature R_□ of the heterostructure with of $\delta = 0.5$ with the thickness of LaAlO₃ from 10 to 20 u.c. (c) The change in R_{\Box} with increasing doping at room temperature. (d) Variation of the sheet resistance (R_{\Box}) with temperature of samples with doping fractions δ from 0.0 to 0.6 in the temperature range from 5K to 200K. No metallic behavior for $\delta > 0.5$.

to understand this set of results we have developed a sim-

ple model which primarily calculates the density of the electron liquid at the interface as a function of temperature. Referring to Fig. $1(a)$, recall that LAO due to its alternating charged layers $(\text{LaO})^+$ and $(\text{AlO}_2)^-$ creates a large positive potential at the interface compared to the ground or surface potential. In the ideal picture layers can be treated as capacitors in series, the potential offset is proportional to the number k of such pairs. Recall that for the bulk STO a gap of 1.6 eV exists between the conduction band and the Fermi level and it is this gap that is presumably reduced by the LAO layers. Therefore a certain minimum number of unit cells of LAO are needed to provide a threshold potential to draw electrons to the conduction band of STO. The potential catastrophe with increasing k is clearly avoided by the solid by relaxation of ionic positions, buckling of layers etc., which screen the field. This makes the resulting potential far smaller and saturate rapidly with k.

Another important point to note is that, if the layers are charge-balanced they only produce this potential offset i.e. potential is constant outside the set of charged layers. To generate the electron layer at the interface. one needs an electric field which can come from some unbalanced positive charge, which one can reasonably presume, exists on the LaO layer at the interface. Electrons drawn to the conduction band of STO occupy mostly the Ti d_{xy} levels of TiO₂ layer at the interface [26]. These electrons screen the positively charged LaO layer at the interface. Though there is smaller occupation in other bands like d_{zx} and d_{yz} till around five layers, the mobile electrons should mostly be from Ti d_{xy} levels due to their high dispersion along the interface $[26-28]$.

This leads us to account for the role of LAO layers by two parameters: a potential offset ϕ_0 and an excess charge density $\alpha e/a^2$ (a=lattice parameter of LaO layer). Due to potential offset, the excitation gap in the $TiO₂$ is reduced to $\Delta = (1.6 - e\phi_0)$ eV. The charge density produces an electric field $E_0 = \alpha e/(2\epsilon_0 \epsilon_s a^2)$, where ϵ_s is the dielectric constant of STO which is also temperature dependent. We now use Thomas-Fermi theory to find a self-consistent equation for potential on STO side. Thomas-Fermi theory is valid only when length scale of potential variation is much larger than the De Broglie wavelength, which approximation is not quite valid near the interface. We assume that the charge is induced by occupation in the conduction band of STO. Taking z-axis to be perpendicular to the interface, the carrier density $N(z)$ is given in terms of potential $V(z)$ as $N(z) = 2g(u(z) + \beta \Delta)/\lambda_T^3$. Here $u(z) = \beta eV(z)$, $\beta = (k_BT)^{-1}$ and $\lambda_T = \hbar/(2m^*k_BT)^{1/2}$. where m^* denotes the effective mass in the conduction band of STO. The function $g(u)$ is essentially the Fermi-Dirac distribution given by

$$
g(u) = \frac{2}{\sqrt{\pi}} \int_0^\infty \frac{x^{1/2} dx}{e^{x+u} + 1}.
$$
 (1)

This enables us to obtain the equation of potential as

$$
\frac{d^2u}{dz^2} = \frac{1}{2\lambda^2} \left[\frac{g(u+\beta\Delta)}{g(\beta\Delta)} - 1 \right],
$$
 (2)

where the screening length λ is given by

$$
\lambda^{-2} = \frac{4\beta e^2 g(\beta \Delta)}{\epsilon_0 \epsilon_s \lambda_T^3},\tag{3}
$$

The equation is solved for the boundary condition given by the field E_0 and the profile of carrier density is found. The sheet density $N_2(T)$ is obtained by integrating $N(z)$ over a depth of order λ . The variation of N_2 with temperature for a typical set of parameters used here is shown in the inset of Fig. 2. It should be mentioned that the sheet density is a rather sensitive function of parameters Δ and α . These parameters mimic changes in the electronic density due to the presence of interface and subsequent ionic relaxations. Here they are obtained from experimental parameters as discussed below.

We first discuss the effect of doping in qualitative terms. As shown in Fig. $1(a)$, when the LaMnO₃ layer is inserted, the Mn ions occupy the negatively charged layer next to LaO but away from the interface. We surmise that due to mixed-valent character of Mn ion between states Mn^{3+} and Mn^{4+} a charge transfer occurs from negatively charged $Mn_{\delta}Al_{1-\delta}O_2$ layer toward the LaO layer neutralizing its charge considerably. Further a reduced charge on Mn- layer would also lead to a relaxation of charge on other LAO layers, thereby affecting both ϕ_0 and α . Small changes in these parameters can drastically affect the field on the $TiO₂$ layers at the interface and consequently a larger number of LaO layers are needed to generate the interfacial 2-DEL. Clearly, an ion with mixed-valent character greatly facilitates the charge transfer, which was restricted with Al ions.

Next we discuss the detailed temperature dependence of resistance as shown in Fig. $1(d)$. This allows us to obtain the model parameters which corroborate to an extent the qualitative reasoning described above. We focus on the weak-scattering regime for temperatures below the resistance minimum. The resistance in this regime is fitted according to the formula,

$$
\sigma(T) = \frac{N_2(T)e^2 \tau_0}{m^*} - \frac{e^2}{4\pi^2 \hbar} \left[2\ln\left(\frac{\tau_0^{-1} + \tau_i^{-1} + \tau_{so}^{-1}}{\tau_i^{-1} + \tau_{so}^{-1}}\right) + \ln\left(\frac{\tau_0^{-1} + \tau_i^{-1} + 2\tau_{so}^{-1}}{\tau_i^{-1} + 2\tau_{so}^{-1}}\right) - \ln\left(\frac{\tau_0^{-1} + \tau_i^{-1}}{\tau_i^{-1}}\right) \right]
$$
(4)

The first term is the Drude term and the second one is the weak-scattering correction describing quantum interferece effects [29–31]. Three relaxation times occur in this expression. First is the elastic scattering time τ_0 which is temperature independent. The second one is the inelastic scattering time τ_i whose temperature dependence is taken to be of the form $\tau_0(T_0/T)^p$ where p depends on the inelastic scattering mechanism. The inelastic scattering typically gives rise to logarithmic increase of resistance with decreasing temperature. Finally τ_{so} is the

Table I: Values of model parameters used to fit resistance curves in the temperature range 6K to 46K for δ =0.0, 0.1, 0.2, 0.4 and 0.5 shown in Figure 1(d). The elastic scattering time for all curves is $\tau_0=2.3\times10^{-14}\text{s}$

	0.0	0.1		$0.2 \quad 0.4 \quad 0.5$	
α	$\begin{bmatrix} 0.15 & 0.11 & 0.086 & 0.045 & 0.025 \end{bmatrix}$				
$\Delta(eV)$	[0.001] 0.001] 0.001] 0.001] 0.002]				
$\tau_{s0}(\times 10^{-13} \text{s})$ 1.6		1.9	2.5	3.0	3.9

relaxation time due to spin-orbit scattering. This is important here due to interface electric field which causes significant effect on electrons moving parallel to the interface [32]. The spin-orbit scattering works oppositely to the inelastic scattering and it slows down the increase of resistance at lower temperatures, where $\tau_{in} > \tau_{so}$.

We first note that this data could not be accounted for in terms of a straightforward weak-scattering correction over a temperature-independent Drude term. This is to be expected as the mechanism of carrier generation at the interface implies a temperature-dependent concentration. Since several parameters are required we need to describe how have these been obtained for fitting. The model parameters Δ and α are fixed from the estimates of the carrier density and thickness of 2-DEL. They both depend, of course, on temperature and δ -doping. We have made Hall measurements (not reported here) to obtain the carrier density in our heterostructures. Our estimates and similar estimates available in literature [2] range between 6 to $8\times10^{13}/\text{cm}^2$ for the undoped layer around 50K. The estimates for the thickness of the electron layer are in the range 60-70 A at room temperature. We have chosen Δ and α so that between 5K to 50K, N_2 lies between 4 to $8\times10^{13}/\text{cm}^2$ and λ ranges between 50Åto 10Å. These values are shown in Table 1 for various dopings. For a typical value of parameters the inset of Fig.2 shows the variation of N_2 with temperature.

The value of τ_0 cannot be determined unambiguously from our data, but a survey of estimates in the literature place it to be of the order 10^{-14} s. We take $\tau_0 = 2.25 \times 10^{-14}$ s which then gives consistent magnitudes for other parameters. To determine the parameters for τ_i , we plot measured $\Delta \sigma(T) = \sigma(T) - \sigma_{Drude}$ with $\ln T$. It shows an approximate linear behavior with a slope of 2.8. So we take $p=2.8$. T_0 in the expression for τ_i is adjusted in the fitting procedure and is found to be 95K. The first estimate for τ_{so} is taken to be $\tau_i(T_d)$ where T_d is the temperature where the increase of resistance with decreasing temperature begins to flatten. Thereafter it is fine tuned to obtain the best fits. For the temperature range of interest we take ϵ_s =300. Our fits for four resistance curves corresponding to $\delta = 0.0, 0.1,$ 0.2 and 0.4 are shown in Fig.2. The fits are reasonably good in the temperatures range 6-46K with parameters shown in Table 1. A good fit is also obtained for $\delta = 0.5$, but is not shown in Fig. 2.

Following comments are in order. From Table 1, we

see that with doping α decreases in accordance with our reasoning that Mn-doping reduces charge on LaO layer at the interface. It is corroborated further by increase in τ_{so} . Thus the layer charge density (α) accounts for increase of resistance with doping. The gap parameter Δ does not vary with doping till δ =0.4, beyond which it may rise rapidly. The quantitative accuracy of these numbers is limited due to rather approximate nature of the Thomas-Fermi theory. In the above we have ignored the electron-electron interaction which also gives rise to $log(T)$ terms. These are incorporated through multiplication by a factor $(1 - F)$ to the weak-scattering correction term [35]. From the data, we cannot disentangle this factor as here it also depends on temperature through density. This interaction also leads to a $log(T)$ correction to thermopower [36], but we find it too small to account for the data presented below. This is consistent with the remarks of Caviglia et al [32].

From temperature of the minimum to room temperature the resistance rises rapidly by a factor of seven or so. This model cannot account for this as this would have contributions from the usual increase of relaxation rate as well as possible renormalization of ϕ_0 with temperature due to charge relaxation etc.

Figure 2: (Color online) We show theoretical fits of resistance measurements in the temperature range 5K to 50K for four films with $\delta = 0.0, 0.1, 0.2$ and 0.4. The fits use Eq. (4) in which the carrier density used N_2 used in the Drude term is obtained using Eqs. (1) to (3). The inset shows the variation of N_2 with temperature for $\delta = 0.0$ and $\alpha = 0.15$

Fig.3 shows the temperature dependence of thermopower $S(T)$ for the LAO-STO heterostructure and two δ-doped samples, with fractions $\delta = 0.2$ and $\delta = .0.5$ of monolayer of LaMnO_3 between 5 K to 150 K. A negative TEP is observed indicating that the charge carriers are electrons in these systems. The magnitude of S for LAO-STO is rather small and shows a weak variation with temperature. This is much less than what one would theoretically expect from carrier confinement in the $SrTiO₃$ quantum wells. This may partly be attributed to the effective thickness of the electron gas. It thereby loses the two dimensional advantage. The flat temperature variation seen here is a large departure from the free two dimensional electron gas which for example, at a density of $2x10^{13}/\text{cm}^2$ shows linear variation upto 300 K. Note

Figure 3: (Color online) Thermopower (S) for three different fractions of LaMnO_3 layer in the temperature range 5 K to 150 K. The inset shows the differences at lower temperatures in a zoomed plot.

that some earlier measurements of thermopower on LAO-STO [33, 34] reported much larger values for $T > 77$ K. The LAO films in these studies are much thinner (4 to 6 U.C.) and have larger sheet resistance R_{\Box} .

The other two curves in Fig.3 show the effect of insertion of LaMnO₃ monolayer on thermopower. At $\delta = 0.2$ one sees a modest increase but at $\delta = .0.5$ there is a substantial increase in the magnitude of S at temperatures higher than 60 K. At 150 K, the magnitude of S for $\delta = 0.5$ is 96 $\mu V/K$, which is more than twice than that of LaAlO₃/SrTiO₃ system ($\simeq 40 \mu V/K$). In the lower temperature range a salient feature is the emergence of a step like variation in S. This feature could arise from factors like: 1) due to the step like feature associated with the density of states of the confined gas, 2) to the the phonon drag which is also expected in this temperature range.

However, more remarkable is the behavior in the temperature range from 80 K to 150 K, where we find that curves for the δ -doped system are almost parallel.to the undoped system. This corresponds to a temperature-independent contribution which is suggestive of Heikes-like contribution. The mixed-valent Mn ions in $Al_{1-\delta}Mn_{\delta}O_2$ layer are the most likely contributors to it. Beni and Chaikin [17] extended the Heikes formula to strongly-correlated systems at high temperatures $(k_BT \gg W; W$ is bandwidth). They showed that under such conditions a large contribution to thermopower comes from the spin and orbital degrees of freedom, which is basically due to entropy associated with these degrees of freedom [17–19]. Thus it is natural to assume that the large enhancement in S comes from 3d electrons of the Mn ions. In LaMnO₃ the Mn ions are in the $3d^4$ state. As argued above, this monolayer loses some electrons in order to screen the positive field of LaO layer (see Fig. 1a). This assumption leads to the model in which Mn

ions in $\text{Al}_{1-\delta} \text{Mn}_{\delta} \text{O}_2$ layer exist in states of $3d^4$ and $3d^3$. Given that the degeneracy of these states are $g_4 = 10$ and $g_3 = 4$, respectively, one obtains the following formula,

$$
S_{(Mn)} = \frac{k_B}{e} \ln \left(\frac{g_4 \rho_h}{g_3 \left(1 - \rho_h \right)} \right) \tag{5}
$$

where ρ_h is the number of holes from the $3d^4$ state. The correct magnitude for the observed thermopower is obtained with $\rho_h = 0.44$ at $\delta = 0.5$ and $\rho_h = 0.31$ at $\delta = 0.2$. The charge transfer per cell implied by this is $(1 - \rho_h)\delta$ which has the same trend with doping as α . An experimental determination of ρ_h would be a direct way to validate the picture presented here.

To summarize, we report the transport properties of the $LaAlO₃-STIO₃$ heterostructures subjected to interface δ-doping by insertion of fractional mono-layer of LaMnO₃. This inhibits the formation of 2-DEL at the interface reflected by increase in resistance and the larger critical thickness of the $LaAlO₃$ over-layers needed to induce 2-DEL at the interface.

We have developed a simple model by extending the polarization catastrophe ideas and Thomas-Fermi theory to make temperature-dependent estimates of the density of the electron liquid at the interface. In this framework we provide an explanation of the above results by arguing

that $\text{Al}_{1-\delta} \text{Mn}_{\delta} \text{O}_2$ layer due to the mixed-valent nature of Mn^{3+} ion transfers charge to the LaO layer at the interface, thereby reducing the interface field. Further by using weak-scattering mechanism we have provided theoretical fits to the resistance data at low temperatures and extracted the doping dependence of model parameters which substantiates the above reasoning. The δ doping of the interface also leads to an increase of its thermopower in the higher temperature range, above 60 K in the present case. This increase is constant in temperature and can be attributed to the contribution from the $AlMnO₂$ layer. This work opens interesting possibilities for further work in this direction.

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