

# Techno-economic analysis of solar stills using integrated fuzzy analytical hierarchy process and data envelopment analysis

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## Abstract

Desalination using solar stills is an ancient economic method for water desalination. Over the years, research and development in the area of solar still has resulted in increased distillate yield by means of **integration** of PCM (phase change material), photo-voltaic thermal (PVT), etc with the still. Nano-PCM is an upcoming technology which modifies the thermal performance of PCM. The aim of this research is to analyze the efficiency of 20 solar stills including nano-PCM based solar stills considering various input and output criteria using integrated fuzzy analytical hierarchy process (AHP) and data envelopment analysis (DEA). **The efficiency derived here is relative with regard to the parameters and stills considered in this study.** The result infers that, even though the productivity of stepped solar still with sun tracking system was high, but when techno-economic aspects were considered it is not among the top solar stills. The analysis indicated pyramid type solar still, single slope solar still with PVT, solar still with NPCM (paraffin + copper oxide), solar still with NPCM (paraffin + titanium dioxide) and solar still with PCM (paraffin) occupies the top five positions with **relative** efficiency of 100, 100, 88.47, 88.46 and 76.93% respectively.

## Keywords

Solar stills; Fuzzy AHP DEA; Relative efficiency; MCDM

## 1. Introduction

Solar desalination is a type of desalination process in which evaporation and condensation processes **are** driven by solar energy. Among the various types of solar desalination processes, solar stills **are significant** because of **their** low environmental impact, technical simplicity, low capital and maintenance cost (Dsilva Winfred Rufuss et al., 2016). Solar still can be used in extremely adverse **environments**, where there is no source of power for running the otherwise efficient desalination process (Dsilva Winfred Rufuss et al., 2016). Various researchers have modified the conventional solar still to improve its productivity. However this led to an increase in capital and maintenance cost. **Studies** carried out by **earlier researchers** (El-Bialy et al., 2016; Kabeel et al., 2010) **determined** the various costs of solar stills. However, there is no study found in the literature review **so far** which presents an optimized **multi-criteria** decision model (MCDM) that considers **various** criteria such as cost, employee's skill, productivity and technical

1 features of solar stills. These aspects need to be considered to ascertain the importance of each  
2 criteria for the selection of an ideal solar still that can be taken up for commercialization. This  
3 paper focuses on the MCDM approach to analyze the relative efficiency of solar stills based on  
4 various input and output criteria using an integrated fuzzy AHP model.  
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7 There are various criteria / parameters influencing a solar still such as atmospheric condition,  
8 design and economics. Atmospheric condition includes weather, ambient temperature, location,  
9 and latitude / longitude degrees. The design aspect includes area, glass cover inclination, brine  
10 depth, solar intensity, productivity, salt concentration and insulators. Economic aspects include  
11 present capital cost, annual maintenance/ operational cost, annual salvage value and cost of  
12 distilled water per litre. Hence selection of a solar still for commercialization needs to be done by  
13 considering such parameters as mentioned above. In this paper, fuzzy analytical hierarchy  
14 process (AHP) and data envelopment analysis (DEA) techniques are used to optimize some of  
15 the above mentioned parameters to arrive at an efficiency for each still relative to the parameters  
16 considered. Generally, technical (thermodynamic) efficiency will be used in the comparison of  
17 solar stills which considers only the technical aspects. In this study in addition to technical  
18 aspects other parameters are considered and the efficiency is obtained relative to the parameters  
19 and the stills considered. Technical efficiency is an absolute efficiency that can be compared  
20 across various stills while relative efficiency is constrained within the parameters used and the  
21 stills used in the study.  
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29 Many researchers have used fuzzy AHP techniques in desalination systems like multi-stage  
30 desalination (MSD), reverse osmosis (RO), multi-stage flash desalination (MSF), vapor  
31 compression (VC) and multi-effect distillation (MED). Fuzzy logic was used in controlling the  
32 upper saline water temperature of MSD plants. The research also focused on controlling various  
33 parameters for implementing MSD plants in the selected location (Ismail, 1998). Various  
34 operational constraints was adopted for implementing a RO desalination plant using fuzzy logic.  
35 The proposed methodology resulted in profit for the plant by increasing the availability and  
36 decreasing the manpower requirement for RO implementation (Zilouchian and Jafar, 2001).  
37 Fuzzy logic was adopted for analyzing MSF and RO systems using various control parameters  
38 like brine salinity, pre-heating (Gambier and Badreddin, 2003). Water potential was assessed for  
39 irrigation and human consumption using fuzzy logic. It was found that the water used for  
40 irrigation is more important than for human consumption (Tsakiris et al., 2009). Major factors  
41 which affect the daily productivity of solar still was analyzed using fuzzy logic (Mamlook and  
42 Badran, 2007). The same authors (Mamlook and Al-Rawajfeh, 2008) extended the research by  
43 using fuzzy logic to analyze which of those factors affect the productivity of MED. The various  
44 factors considered in their research included top saline water temperature, pH, temperature and  
45 salinity of the sea water. The AHP was used to determine the most suitable desalination process  
46 considering seven factors. The desalination processes considered in the research include MSD,  
47 MSF, RO and VC. The factors considered were water quality, recovery ratio, consumption of  
48 energy, efficiency of instruments and total cost (Hajeeh and Al-Othman, 2005). Various water  
49 conservation policies in Kuwait was analyzed using fuzzy AHP. Reusing treated brine water,  
50 promoting water conservation were some of their recommendations (Hajeeh, 2010). It is found  
51 from the literature that researchers have used fuzzy (Gambier and Badreddin, 2003; Ismail, 1998;  
52 Mamlook and Al-Rawajfeh, 2008; Mamlook and Badran, 2007; Tsakiris et al., 2009; Zilouchian  
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1 and Jafar, 2001), AHP (Hajeesh and Al-Othman, 2005), fuzzy AHP (Hajeesh, 2010) in  
2 desalination systems.  
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4 Integrated fuzzy AHP DEA approach can be used in energy related areas like solar photovoltaic,  
5 solar thermal, wind, desalination, power stations, materials and metallurgical applications to  
6 determine the weights of influencing parameters and to find the relative efficiency among a set  
7 of energy systems. Some researchers used fuzzy for finding the efficiency frontier in  
8 petrochemical industries (Taylan et al., 2016), generation sector (Mojallizadeh and  
9 Badamchizadeh, 2017; Tanha Aminloei and Ghaderi, 2010; Yu and Dexter, 2010). AHP was  
10 used for categorizing frontier energy industries in manufacturing sector (Jovanović et al., 2015)  
11 and integrated fuzzy AHP DEA approach has been used (Criswell and Thompson, 1996; Lee et  
12 al., 2013, 2011) for finding the relative efficiency of energy technology and hydrogen energy  
13 technologies.  
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19 Fuzzy logic helps in arriving at concrete estimates despite the vagueness of human thought. AHP  
20 helps in obtaining the relative weights for a set of critical attributes. The benefits of integrating  
21 fuzzy logic and AHP is to achieve precision in determining the relative importance of criteria  
22 and to develop a hierarchal structure for the multi-criteria decision making purpose. It can handle  
23 both linguistic assignment and numerical values. The benefits of applying an integrated fuzzy  
24 AHP approach to solar still is to determine the relative importance/weights of criteria that affects  
25 the performance and efficiency of solar still. DEA is a benchmarking technique employed to  
26 know the frontier in the selected area by estimating the relative efficiency of various decision  
27 making units (DMU). The benefits of integrating fuzzy AHP and DEA are to find the relative  
28 efficiency of DMU considering the weights of criteria obtained from fuzzy AHP. The advantage  
29 of implementing such an approach in solar still is to rank and prioritize the important criteria  
30 which is involved in the performance, efficiency and productivity of a solar still. Also, the  
31 relative efficiency of various solar stills by considering both technical and economic factors can  
32 be determined by giving due importance to the influencing criteria. The main objective of other  
33 techno-economic analysis (TEA) such as top-down or bottom-up cost approach is to determine  
34 the cost and technical feasibility of a particular system (here solar still) and compare the results.  
35 In this paper, the integrated approach (fuzzy AHP DEA) is a step ahead i.e., it helps to evaluate  
36 the relative efficiency of various solar stills considering several criteria simultaneously to arrive  
37 at an optimal decision. The pros of the integrated fuzzy AHP DEA are: comparative analysis of  
38 different variant of targets (here solar stills), any measurable criteria for all variant of solar still  
39 can be used in DEA, reverse coding of input and output criteria is possible, improvement criteria  
40 for the selected parameters can be identified and implemented, human preference can also be  
41 incorporated in DEA and fuzzy AHP DEA can be incorporated as a complement to other  
42 techniques. As every approaches have some cons associated with them, similarly this integrated  
43 fuzzy AHP DEA also has some cons such as: difficulty arises if there is a missing value in the  
44 dataset and weak assumption in DEA may lead to underestimation of the relative efficiency of  
45 decision making units.  
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58 Further, this integrated fuzzy AHP DEA approach can also be used in other energy-related areas  
59 including solar photovoltaic, solar thermal, wind, desalination, power stations, materials and  
60 metallurgical applications to determine the weights of influencing parameters and to find the  
61 relative efficiency among a set of energy systems. It is concluded that, even though various  
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1 researchers used fuzzy and AHP techniques in desalination systems, no one has used an  
2 integrated fuzzy-AHP-DEA analysis for **analysing the different solar stills**. Hence this research  
3 gap is addressed in this paper in addition to analyzing the innovative nano-PCM based solar stills  
4 from a techno-economic viewpoint. Nanoparticles were incorporated with PCM to **modify** its  
5 thermal properties like thermal conductivity, latent heat of vaporization and decreasing its  
6 charging and discharging rate (Dsilva Winfred Rufuss et al., 2017; Kamaraj et al., 2016). Even  
7 though nanoparticles **improve** the thermal properties of PCM in solar still, economic feasibility  
8 of the solar still with nano-PCM is one of the essential parameter that needs to be analyzed.  
9 Three input criteria namely fabrication/installation cost, skilled labour requirement and land area  
10 requirement are considered along with four output criteria namely annual cost, commercial  
11 potential, annual productivity and technical complexity. An integrated fuzzy-AHP-DEA analysis  
12 is carried out to determine the relative efficiencies of 20 solar stills (for which the data is  
13 available for the parameters considered). Also, the relative weights of each criteria and their  
14 importance with reference to a particular still are determined.

## 21 **2. Solar stills**

22 **Desalination is an essential response to the growing water scarcity problem. It has been reported**  
23 **in our previous paper (Dsilva Winfred Rufuss et al., 2016) that, by the year 2030 half of the**  
24 **world population will experience severe water crisis. There are various desalination process**  
25 **available to desalinate the saline water, of which solar still holds its significance owing to its**  
26 **enviro-economic friendly nature (Kaushal and Varun, 2010; Sathyamurthy et al., 2017;**  
27 **Velmurugan and Srithar, 2011). Solar stills work by the evaporation and condensation processes**  
28 **similar to natural rain. A detailed classification of the desalination process and solar stills are**  
29 **represented graphically in Fig. 1 and Fig. 2 respectively. Low productivity is a major drawback**  
30 **in solar stills, and hence extensive research work has been carried to improve the productivity by**  
31 **modifying the design and operational parameters (Ahsan et al., 2012; Arunkumar et al., 2013,**  
32 **2012; Gaur and Tiwari, 2010; Murugavel et al., 2010; Rahbar et al., 2016; Sakthivel et al., 2010;**  
33 **Sharshir et al., 2016). The various design and operational parameters are comprehensively listed**  
34 **in Fig. 3.**

35 The basic model of solar still is called a simple single slope solar still. This does not have any  
36 enhancements present for augmenting the productivity. The setup of simple single slope solar  
37 still is depicted in Fig. 4.

38 **Insert Fig. 1. Detailed tabulation showing classification of desalination processes (Nayi and**  
39 **Modi, 2018)**

40 **Insert Fig. 2. Various types of solar stills (Tiwari and Sahota, 2017)**

41 **Insert Fig. 3. Various climate, design and operational parameters influencing the productivity of**  
42 **solar still (Muftah et al., 2014)**

43 **Insert Fig. 4. Setup of simple single slope solar still (Ali Samee et al., 2007)**

44 Researchers tried to add various components like sun tracker (Abdallah et al., 2008), photo-  
45 voltaic-thermal (PVT) (Kumar and Tiwari, 2009), collector (Badran and Al-Tahaine, 2005),  
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1 concentrator (Abdel-Rehim and Lasheen, 2007) and fin (Velmurugan et al., 2008a) to improve  
2 the productivity. This resulted in changes in other parameters also namely fabrication cost, skill  
3 level of labourers required to construct the solar still, complexity, land area requirement. The  
4 pictorial representations of solar stills with sun tracker, PVT, collector, concentrator and fin are  
5 depicted in Fig. 5, Fig. 6, Fig. 7, Fig. 8 and Fig. 9 respectively.  
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9 **Insert Fig. 5.** Schematic of solar still with sun tracking system (Abdallah et al., 2008)  
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11 **Insert Fig. 6.** Solar still integrated with photo-voltaic thermal (PVT) system (Kumar and Tiwari,  
12 2009)  
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15 **Insert Fig. 7.** Solar still integrated with flat-plate collector (Badran and Al-Tahaine, 2005)  
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18 **Insert Fig. 8.** Schematic of solar still integrated with concentrators (Abdel-Rehim and Lasheen,  
19 2007)  
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22 **Insert Fig. 9.** Schematic setup of solar still integrated with fin (Velmurugan et al., 2008a)  
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25 Some researchers tried to modify the whole design of the solar still with unconventional shapes  
26 i.e, hemispherical (Ismail, 2009) and pyramid shapes (Fath et al., 2003). The design setup of  
27 hemispherical and pyramid solar still is depicted in Fig. 10 and Fig. 11 respectively. These  
28 modifications resulted in increasing the technical complexity and skilled labour required for  
29 fabrication, erection and maintenance and decreased the land area requirement as compared to  
30 conventional solar stills.  
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33 **Insert Fig. 10.** Pictorial representation of hemispherical solar still (Ismail, 2009)  
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36 **Insert Fig. 11.** Schematic configuration of pyramid type solar still (Fath et al., 2003)  
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39 The energy storage experts tried to integrate energy storage in solar still applications using wick,  
40 sponge (Velmurugan et al., 2008b), phase change materials (Shalaby et al., 2016) was integrated  
41 to solar stills to enhance the productivity. The solar still with wick, sponge and phase change  
42 materials are depicted in Fig. 12 and Fig. 13 respectively. This type of integration has no change  
43 on the land area requirement and has a slight increase on other factors like technical complexity,  
44 fabrication cost. In recent years, researchers have tried using nanoparticle impregnation in PCM  
45 for solar still applications. It was inferred from the literature that the impregnation of  
46 nanoparticles in PCM may either improve or impair the thermal properties of the base material  
47 (Dsilva Winfred Rufuss et al., 2017; Rao Nulakani et al., 2015).  
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53 As stated earlier these kinds of modifications end up with an increase in fabrication cost,  
54 technical complexity and skilled labour. Hence there is a need to identify a still with optimum  
55 factors. The criteria measured before the fabrication of solar stills are considered as input criteria  
56 and the criteria involved in the commercialization are considered as output criteria. In this  
57 **research** skilled labour requirement (SL), fabrication and installation cost (FC) and land area  
58 requirement (LA) are considered as the input criteria while economic impact (EI), commercial  
59 potential (CP), productivity (P) and technical complexity (TC) are considered as the output  
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criteria for the integrated fuzzy analytical hierarchy process. The analysis will help us to determine the unique contribution with respect to a certain criteria as well as its relative importance vis-à-vis other criteria. The traditional top down or bottom up approaches for techno-economic analysis will only present the overall cost comparison among the solar stills while the present analysis will clearly highlight how concentration on a specific input criteria will improve the overall efficiency of a solar still as well as the efficiency for each of the output criteria.

Insert Fig. 12. Schematic of solar still with sponge (Velmurugan et al., 2008b)

Insert Fig. 13. Solar still with phase change material (PCM) (Shalaby et al., 2016)

### 3. Methodology

The empirical analysis is carried out by collecting various quantitative data on the input/output criteria of the solar still. In this research, fabrication costs (FC) for the 16 solar stills are taken from the literature (Abdallah et al., 2008; Abdallah and Badran, 2008; Abdel-Rehim and Lasheen, 2007; Ali Samee et al., 2007; Badran et al., 2005; Badran and Al-Tahaine, 2005; El-Bahi and Inan, 1999; El-Bialy et al., 2016; El-Sebaili et al., 2008; Fath et al., 2003; Ismail, 2009; Kabeel et al., 2010; Kumar and Tiwari, 2009; Velmurugan et al., 2009, 2008a, 2008b; Velmurugan and Srithar, 2007; Voropoulos et al., 2001) while for the remaining four stills - Solar stills with PCM, Nano PCM namely titanium dioxide, copper oxide, graphene oxide, data is obtained from the investigation carried out using the experimental setup in the Institute for Energy Studies, Anna University Chennai, India (Dsilva Winfred Rufuss et al., 2017; Rufuss et al., 2015). The various scales for the input/output criteria such as SL, LA, EI, CP, P and TC are tabulated in Table.1. The overall methodology adopted in the study using this integrated approach is clearly depicted in Fig. 14.

Insert Table 1 Five point scale for various input and output criteria

Insert Fig. 14. Overall methodology of integrated fuzzy AHP DEA

#### 3.1. Applying the Fuzzy AHP method

AHP helps in finding the importance of criteria as a hierarchical structure. Experts were identified based on their domain knowledge in the field of renewable energy with special reference to solar energy and solar stills. They were asked to give the relative ratings for pairwise comparisons of the criteria. The consistency of each expert is determined as follows (Lee et al., 2013, 2011; Tanha Aminloei and Ghaderi, 2010; Taylan et al., 2016):

$$CI = \frac{\lambda_{\max} - n}{n - 1} \quad (1)$$

where  $\lambda_{\max}$  and  $n$  are the principal eigenvalue and dimension of the matrix. The pairwise comparison is accepted only if the  $CR \leq 0.10$ . Consistency ratio (CR) is the ratio of consistency index (CI) to random index (RI) [14, 15].

$$CR = \frac{CI}{RI} \quad (2)$$

The analysis is repeated for each expert for the input and output criteria. Though AHP captures the preference of expert, fuzzy AHP is used to determine the priority weights of the input and output criteria using hierarchical fuzzy decision making process.

The triangular fuzzy scale (TFN) and the inverse scale are given in Table 2.

**Insert Table 2 Triangular fuzzy (TFN) scale and its inverse TFN scale**

$$\text{Let } M_{ij} = (l_{ij}, m_{ij}, u_{ij}) \quad (3)$$

$M_{ij}$  be the TFN for a fuzzy pair wise comparison judgment, where  $l$ ,  $m$  and  $u$  are lower, mid and upper limit respectively.

The synthetic extent value with respect to  $i^{\text{th}}$  object is calculated using the following formulas [14, 15]

$$S_i = \sum_{j=1}^m M_{ij} \left[ \sum_{i=1}^n \sum_{j=1}^m M_{ij} \right]^{-1} \quad (4)$$

$$\sum_{j=1}^m M_{ij} = \left( \sum_{j=1}^m l_{ij}, \sum_{j=1}^m m_{ij}, \sum_{j=1}^m u_{ij} \right), i = 1, 2, 3, 4, \dots, n \quad (5)$$

$$\sum_{i=1}^n \sum_{j=1}^m M_{ij} = \left( \sum_{i=1}^n \sum_{j=1}^m l_{ij}, \sum_{i=1}^n \sum_{j=1}^m m_{ij}, \sum_{i=1}^n \sum_{j=1}^m u_{ij} \right) \quad (6)$$

$$\left[ \sum_{i=1}^n \sum_{j=1}^m M_{ij} \right]^{-1} = \left( \frac{1}{\sum_{i=1}^n \sum_{j=1}^m u_{ij}}, \frac{1}{\sum_{i=1}^n \sum_{j=1}^m m_{ij}}, \frac{1}{\sum_{i=1}^n \sum_{j=1}^m l_{ij}} \right) \quad (7)$$

The value of  $S_i$  is then determined and the degree of possibility of  $S_j = (l_j, m_j, u_j) \geq S_i = (l_i, m_i, u_i)$  is expressed by the following equation [14, 15].

$$V(S_j \geq S_i) = \text{height}(S_i \cap S_j) = u_{S_j}(d) = \begin{cases} 1, & \text{if } m_j \geq m_i \\ 0, & \text{if } l_i \geq u_j \\ \frac{l_i - u_j}{(m_j - u_j) - (m_i - l_i)}, & \text{otherwise} \end{cases} \quad (8)$$

The minimum degree of possibility  $d'$  (i) of  $V(S_i \geq S_j)$  for  $i=1,2,3,\dots,k$  and  $j= 1,2,3,\dots,k$  is calculated using [14, 15]

$$V(S \geq S_1, S_2, \dots, S_k) \text{ for } i = 1, 2, \dots, k = V[(S \geq S_1) \text{ and } (S \geq S_2) \text{ and } \dots (S \geq S_k)] \\ = \min V(S \geq S_i) \text{ for } i = 1, 2, \dots, k \quad (9)$$

1 Assume  $d'(A_i) = \min V (S \geq S_i)$  for  $1 = 1, 2, \dots, k$

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3 The weight vector is found using the equation [14, 15]

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$$W' = (d'(A_1), d'(A_2), \dots, d'(A_n))^T$$
 where  $A_i (i = 1, 2, 3, 4, \dots, n)$  are the  $n$  elements (10)

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9 The weight vectors are then normalized to get the relative weight using the formula [14, 15]

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$$W = (d(A_1), d(A_2), \dots, d(A_n))^T$$
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14 where  $W$  is a non-fuzzy number indicating the relative weight of the criteria.

### 15 16 17 **3.2. Measuring the relative efficiency using DEA**

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19 The relative efficiency of various types of solar still is calculated by using DEA approach. Fig. 15, shows the hierarchy of the DEA process which consist of three input and four output criteria. DEA is an analytical technique used to determine the efficient utilization of resources in a decision making unit (DMU). The model developed by (Charnes et al., 1978) is adopted to find the relative efficiency. The DEA formulation is as follows:

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27 There are  $n$  units with  $s$  outputs denoted by  $Y_{rk}$ ,  $r=1, 2, \dots, s$  and  $m$  inputs denoted by  $X_{ik}$ ,  $i=1, 2, \dots, m$ , the efficiency score ( $h_k$ ) for the  $DMU_k$

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$$h_k = \text{Max} \frac{\sum_{r=1}^s u_{rk} Y_{rk}}{\sum_{i=1}^m v_{ik} X_{ik}}$$
 (12)

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35 where  $u_r$  and  $v_i$  are non-negative weights.

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38 In order to obtain the efficiency of DMU in such a manner that they are not greater than 1, the equations are rewritten as follows:

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$$\text{s. t } \frac{\sum_{r=1}^s u_{rk} Y_{rk}}{\sum_{i=1}^m v_{ik} X_{ik}} \leq 1, \text{ for } j = 1, 2, 3, \dots, n$$
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$$u_{rk} > 0, \text{ for } r = 1, 2, 3, \dots, s$$
 (14)

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$$v_{ik} > 0, \text{ for } i = 1, 2, 3, \dots, m$$
 (15)

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52 The efficiency ranges between 0 and 1. The system with maximum efficiency is the system lying in the efficient frontier and is considered to be the best as compared to the other systems. The above equation is transformed to a linear programming problem one for each DMU as follows (Lee et al., 2013, 2011):

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$$h_k = \max \sum_{r=1}^s u_r Y_{rk}$$
 (16)

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$$\text{s. t } \sum_{i=1}^m v_i X_{ij} - \sum_{r=1}^s u_r Y_{rj} \geq 0 \text{ for } j = 1, 2, 3, \dots, n \quad (17)$$

$$\sum_{i=1}^m v_i X_{ik} = 1 \quad (18)$$

$$u_r \geq 0 \text{ for } r = 1, 2, 3, \dots, s \quad (19)$$

$$v_i \geq 0 \text{ for } i = 1, 2, 3, \dots, m \quad (20)$$

**Insert Fig. 15. Hierarchical structure of various input and output criteria used in DEA**

The model obtained is referred to as the CCR model. This CCR model assumes that the production components are constant return-to-scale. Assurance region (AR) is selected to avoid null outputs in the analysis. In AR-CCR model, a set of new constrains will be included in the above model in such a way that the weights are restricted with a lower and upper bound.

$$L_{1,2} \leq \frac{u_{j1}}{u_{j2}} \leq U_{1,2} \quad (21)$$

where  $L_{1,2}$  and  $U_{1,2}$  are lower and upper bound.  $u_{j1}$  and  $u_{j2}$  present the weight achieved by the DMU<sub>j</sub>. By adding equation 21 in the CCR model, AR-CCR model is obtained.

#### 4. Results and discussion

Researchers have been working in various types of solar still and have identified several technically viable stills. However, for a still to be made commercially viable we need to study the social and economic aspects in addition to technical aspects. Such a study which integrates energy production and energy efficiency parameters across various energy systems from a techno-economic viewpoint needs to be done to obtain a realistic estimate of an energy system. In this study, energy production parameters namely productivity, commercial potential; energy efficiency parameters namely technical complexity; economic parameters namely fabrication and maintenance costs; social parameters namely employee skill level, land area have been considered and studied in the MCDM analysis.

##### 4.1. Fuzzy AHP DEA approach

Experts were chosen based on their teaching, research and industrial experience in the domain area namely renewable energy, desalination and solar stills. The choice of the number of experts depend on the availability of the experts and their accessibility. There is no literature available which specifies the number of experts to be chosen for AHP based decision making process (Nixon et al., 2010). The outcome varies as the expert size varies since, greater the number of experts, arriving at a consensus becomes complex due to the uncertainty in the decision making process. The judgement of the experts should have minimum variability with high level of confidence and convergence. In general practice, literatures indicate that smaller expert size kindles effective impact and involvement which lead to the group unanimity (Dey, 2004; Nixon

et al., 2010). The consistency ratio of the experts was found and the response of 10 experts was then used for further analysis. The demographic details of the experts are given in Table 3.

**Insert Table 3 Demographic details of the experts**

The experts were asked to rank the relative importance of the various input and output criteria using AHP relative importance scale. Using the relative importance score given by the experts, the CR for each expert was determined for each of the input/output criteria and the values are tabulated in Table 4. From the Table 4, it is found that the CR value for all the ten experts are less than 0.1. Hence all the experts' opinion are considered valid and used for further analysis. The synthetic weight was then determined for the input and output criteria for each of the expert. The procedure adopted is presented for one expert for the input criteria. This procedure is repeated for all the experts as well as for the output criteria. The pairwise comparison of TFN value of one expert (expert-1) using Table 2 is shown in Table 5.

**Insert Table 4 CR value for the input and output criteria**

**Insert Table 5 Pairwise comparison**

Using the equation (4), (5), (6) and (7), the synthetic weights are obtained as follows.

$$S_1(SL) = (3, 3.666, 4.5) \otimes \left( \frac{1}{12.333}, \frac{1}{10.166}, \frac{1}{8.3} \right) \quad (23)$$

$$S_2(FC) = (1.8, 2, 2.33) \otimes \left( \frac{1}{12.33}, \frac{1}{10.166}, \frac{1}{8.3} \right) \quad (24)$$

$$S_3(LA) = (3.5, 4.5, 5.5) \otimes \left( \frac{1}{12.33}, \frac{1}{10.166}, \frac{1}{8.3} \right) \quad (25)$$

The degree of possibility  $S_j$  (equation 8) is given in Table 6.

**Insert Table 6 Comparing the values of fuzzy synthetic extent**

The minimum degree of possibility  $d'(i)$  found using equation 9 is as follows:

$$d'(1) = \min V(S_1 \geq S_2, S_3) = 0.7591$$

$$d'(2) = \min V(S_2 \geq S_1, S_3) = 0$$

$$d'(3) = \min V(S_3 \geq S_1, S_2) = 1$$

Using equation 10, the weight vector is determined and their relative weights are shown below

$$W' = (0.7591, 0, 1)^T$$

Hence the relative weights are

$$W = (0.43155, 0, 0.56845)^T$$

1 The same procedure is repeated for each of the ten experts and the weights are listed in Table 7.  
2 The lower and upper bound is calculated by considering the minimum and maximum values of  
3 the weights. These weights are then incorporated in Charnes, Cooper, Rhodes (CCR) model. The  
4 upper and lower bounds for the input criteria are tabulated in Table 8. Similarly the weights of  
5 ten experts are determined for the output criteria and the values are presented in Table 9. Also,  
6 the lower bound and the upper bound values are obtained for the output criteria and the  
7 corresponding values are tabulated in Table 10. The quantitative data used in the analysis for the  
8 20 stills is presented in Table 11 and the radar chart depicting their input/output criteria is  
9 represented in Fig. 16. From the radar chart, it is clear that **certain solar stills (such as**  
10 **still with wick, hemispherical solar still, stepped still, weir type still, still with collector,**  
11 **concentrator and fin)**, should improve its commercial potential and productivity or reduce their  
12 fabrication cost to reach the top position. The data is normalized and used for further analysis.  
13 DEA model is run using the add-in package available in Microsoft Excel. The weight  
14 distribution of AR-CCR (with weight restriction) for the 20 stills is shown in Table 12.

21 **Insert Table 7 Fuzzy AHP weights for Input criteria**

22 **Insert Table 8 Upper and lower bounds of weights input criteria**

23 **Insert Table 9 Fuzzy AHP weights for output criteria**

24 **Insert Table 10 Upper and lower bounds of weights output criteria**

25 **Insert Table 11 Input/output criteria for 20 solar stills**

26 **Insert Table 12 Weight distribution of AR-CCR (with weight restriction)**

27 **Insert Fig. 16. Input/output criteria for the twenty solar stills**

28 Here the various stills are considered as decision making units. The productive efficiency  
29 decomposition of the various DMU's (in this case, various solar stills) is obtained from the AR-  
30 CCR model and given in Table 13. The efficiency decomposition of twenty solar stills is  
31 depicted in Fig. 17. For the solar still with wick and fin **to be on the frontier, it is necessary to**  
32 **reduce the skilled labour requirement or increase its economic impact.** For a transportable  
33 hemispherical solar still **to reach the efficiency frontier, we** should reduce its fabrication cost and  
34 land area requirement. In the case of solar still with wick and sponge, **we** should improve its  
35 commercial potential and technical complexity. In the case of the stepped solar still with sun  
36 tracking system, we should reduce its fabrication cost, skilled labour requirement and improve its  
37 economic impact. For a weir type solar still, we should **focus on improving** its economic impact  
38 and productivity. The solar still with sponge & pond, shallow pond and condenser require  
39 improvements in their economic impact and productivity or reduce their fabrication cost and land  
40 area requirement. For the solar still with collector and concentrator, we should either reduce its  
41 technical complexity and skilled labour requirement or improve its economic impact and  
42 commercial potential. Pyramid type solar stills should improve its commercial potential,  
43 economic impact and productivity. In the case of solar still with PCM and nano-PCM's, **it is**  
44 **important** to reduce fabrication cost and skilled labour requirement or improve its economic  
45 impact and commercial potential to reach the efficiency frontier.

## Insert Table 13 Efficiency and rank of solar stills

### Insert Fig. 17. Efficiency decomposition of twenty solar stills

When the efficiency of a solar still is 1.00 (100%), then that particular solar still is in the efficiency frontier and is considered to be the most efficient solar still considering all the input and output criteria. From the DEA results, a pyramid type solar still and single slope solar still with PVT lies in the efficiency frontier and are the most efficient solar stills. Solar still with Nano PCM (Copper oxide) and solar still with Nano PCM (Titanium dioxide) come next with the efficiency of 0.8847 and 0.8846 respectively. Solar still with graphene oxide, though technically the best solar still (Dsilva Winfred Rufuss et al., 2016; Rufuss et al., 2015), is completely ruled out since its efficiency is only 0.487. In the case of NPCM based solar still (solar still with copper oxide and titanium dioxide) [ranked no.3 and 4] to reach the efficiency frontier there is 12% lag. Solar still with copper oxide needs to either decrease its skilled labour requirement or increase its economic impact / commercial potential to become the most efficient solar still. Similarly for solar still with titanium dioxide to improve its efficiency position, research has to be done to improve its economic impact and commercial potential.

To summarize, among the various types of solar still technologies, the top five stills which are both technically and economically efficient are pyramid type solar still, single slope solar still with PVT, solar still with NPCM (copper oxide), solar still with NPCM (titanium dioxide) and solar still with PCM. The remaining stills are either technically strong or economically strong. For example, transportable hemispherical solar still and stepped solar still with sun tracking system are technically strong, but when we consider both technical and economic aspects, it is not found among the best solar still technologies. In general, it is recommended that the relative efficiency of solar stills can be enhanced either by decreasing the cost of skilled labour (SL), fabrication (FC), and land area requirement (LA) or by increasing its economic impact (EI), commercial potential (CP), productivity (P) and technical complexity (TC). Hence future research and development in solar stills must be carried out by considering both technical and economic aspects for effective commercialization of solar still technology.

#### 4.2. Applications and recommendation for future works

This techno-economic approach to solar stills will be useful for industrialist to identify the pros and cons of various solar stills. It will help them to select a solar still based on their indigenous resource availability and their strengths. For example, if there is a policy initiative to give a 50% subsidy towards fabrication, then the ranking of stills will undergo a change i.e., pyramid type solar still will take a lead role followed by solar still with NPCM, solar still with pond, and then solar still with PCM. Thus either by increasing the level of the output criteria like productivity, economic impact or decreasing the level of input criteria such as capital cost, labour, efficiency of the energy system can be improved. The values of each parameter in the decomposition table indicates areas where a certain stills can be improved to make it competitive and to reach the efficiency frontier. This integrated fuzzy AHP DEA approach can be used in other desalination system to find the relative efficiency of desalination processes like multi-effect flash distillation (Baig et al., 2011; Choi, 2016; Elzahaby et al., 2016), membrane distillation (Nakoa et al., 2015; Orfi et al., 2016; Wang, 2011; Zhang et al., 2015), FO & RO(forward and reverse osmosis)

(Altaee and Hilal, 2015; Delgado-Torres and García-Rodríguez, 2010; Khanzada et al., 2017; Mokheimer et al., 2013; Mudgal and Davies, 2016; Qasim et al., 2015), ion exchange (AlMarzooqi et al., 2014; Hilal et al., 2015a, 2015b), seawater greenhouse techniques (Davies et al., 2004, 2006; Davies and Knowles, 2006; Davies and Paton, 2005; Yetilmezsoy and Abdul-Wahab, 2014), etc. by selecting the techno-economic input/output parameters.

This integrated approach can also be employed in other applications like renewable energy sectors (solar, wind, tidal, biomass, etc.) and power generation sectors (conventional and non-conventional power plants). In the renewable energy sector, this approach can be used to determine the energy production efficiency in solar and wind. In solar, the relative efficiency of energy production can be investigated by considering various input/output parameters like capacity, location, demand, complexity, land area requirement, etc. for various solar cells such as crystalline silicon solar cell, hybrid solar cell, gallium arsenide solar cell, polymer solar cell, and solid-state solar cell. The energy production and energy efficiency in the wind energy sector can be analyzed using this integrated fuzzy AHP DEA approach by considering input/output parameters like turbine capacity, tower height, power production, land and location, number of blades for various types of wind turbine like vertical axis wind turbine, horizontal axis wind turbine, multi-axis wind turbine, etc. A system which lies on the efficiency frontier can be used as a benchmark for other resource/system to emulate by strengthening of their respective criteria.

## 5. Conclusions

An integrated fuzzy analytical hierarchy process and data envelopment approach is used to analyze the relative efficiency of various solar stills based on various input and output criteria. Relative weights of criteria are found using fuzzy AHP approach and the overall efficiency score for the 20 solar stills is determined using the data envelopment analysis. Though many solar stills are technically strong (high productivity) yet they are not economically strong (high fabrication, operation and maintenance cost) and hence do not find a place among the top solar stills. When the productivity is considered as the only criteria, then hybrid solar still, solar still sun tracking and solar still with solar pond is found to be at the top (Dsilva Winfred Rufuss et al., 2016; Kabeel and El-Agouz, 2011; Yadav and Sudhakar, 2015), but when the other parameters such as fabrication cost, economic impact, etc are considered then pyramid type solar still, still with PVT, still with NPCM (CuO, TiO<sub>2</sub>) and PCM goes to the top five position with 100, 100, 88, 88 and 77% relative efficiency respectively. It is inferred that, solar still with copper oxide requires a reduction in the skilled labour requirement or an improvement in its commercial potential and economic impact to reach the top position. Similarly, overall efficiency of other solar stills can be increased by concentrating on the pinpointed areas.

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## References

- Abdallah, S., Badran, O., Abu-Khader, M.M., 2008. Performance evaluation of a modified design of a single slope solar still. *Desalination* 219, 222–230. doi:10.1016/j.desal.2007.05.015
- Abdallah, S., Badran, O.O., 2008. Sun tracking system for productivity enhancement of solar still. *Desalination* 220, 669–676. doi:10.1016/j.desal.2007.02.047
- Abdel-Rehim, Z.S., Lasheen, A., 2007. Experimental and theoretical study of a solar desalination system located in Cairo, Egypt. *Desalination* 217, 52–64. doi:10.1016/j.desal.2007.01.012
- Ahsan, A., Imteaz, M., Rahman, A., Yusuf, B., Fukuhara, T., 2012. Design, fabrication and performance analysis of an improved solar still. *Desalination* 292, 105–112. doi:10.1016/j.desal.2012.02.013
- Ali Samee, M., Mirza, U.K., Majeed, T., Ahmad, N., 2007. Design and performance of a simple single basin solar still. *Renew. Sustain. Energy Rev.* doi:10.1016/j.rser.2005.03.003
- AlMarzooqi, F.A., Al Ghaferi, A.A., Saadat, I., Hilal, N., 2014. Application of Capacitive Deionisation in water desalination: A review. *Desalination*. doi:10.1016/j.desal.2014.02.031
- Altaee, A., Hilal, N., 2015. High recovery rate NF-FO-RO hybrid system for inland brackish water treatment. *Desalination* 363, 19–25. doi:10.1016/j.desal.2014.12.017
- Arunkumar, T., Jayaprakash, R., Ahsan, A., Denkenberger, D., Okundamiya, M.S., 2013. Effect of water and air flow on concentric tubular solar water desalting system. *Appl. Energy* 103, 109–115. doi:10.1016/j.apenergy.2012.09.014
- Arunkumar, T., Jayaprakash, R., Denkenberger, D., Ahsan, A., Okundamiya, M.S., kumar, S., Tanaka, H., Aybar, H.Ş., 2012. An experimental study on a hemispherical solar still. *Desalination* 286, 342–348. doi:10.1016/j.desal.2011.11.047
- Badran, A.A., Al-Hallaq, A.A., Eyal Salman, I.A., Odat, M.Z., 2005. A solar still augmented with a flat-plate collector. *Desalination* 172, 227–234. doi:10.1016/j.desal.2004.06.203
- Badran, O.O., Al-Tahaine, H.A., 2005. The effect of coupling a flat-plate collector on the solar still productivity. *Desalination* 183, 137–142. doi:10.1016/j.desal.2005.02.046
- Baig, H., Antar, M.A., Zubair, S.M., 2011. Performance evaluation of a once-through multi-stage flash distillation system: Impact of brine heater fouling. *Energy Convers. Manag.* 52, 1414–1425. doi:10.1016/j.enconman.2010.10.004
- Charnes, A., Cooper, W.W., Rhodes, E., 1978. Measuring the efficiency of decision making units. *Eur. J. Oper. Res.* 2, 429–444. doi:10.1016/0377-2217(78)90138-8
- Choi, S.H., 2016. On the brine re-utilization of a multi-stage flashing (MSF) desalination plant. *Desalination* 398, 64–76. doi:10.1016/j.desal.2016.07.020
- Criswell, D.R., Thompson, R.G., 1996. Data envelopment analysis of space and terrestrially-based large scale commercial power systems for earth: A prototype analysis of their relative economic advantages. *Sol. Energy*. doi:10.1016/0038-092X(95)00113-6
- Davies, P.A., Harris, I., Knowles, P.R., 2006. Cooling of greenhouses using seawater: A solar driven liquid-desiccant cycle for greenhouse cooling in hot climates, in: *Acta Horticulturae*. pp. 139–146.



- 1 Davies, P.A., Knowles, P.R., 2006. Seawater bitterns as a source of liquid desiccant for use in  
2 solar-cooled greenhouses. *Desalination* 196, 266–279. doi:10.1016/j.desal.2006.03.010  
3
- 4 Davies, P.A., Paton, C., 2005. The Seawater Greenhouse in the United Arab Emirates: thermal  
5 modelling and evaluation of design options. *Desalination* 173, 103–111.  
6 doi:10.1016/j.desal.2004.06.211  
7
- 8 Davies, P., Turner, K., Paton, C., 2004. Potential of the Seawater Greenhouse in Middle Eastern  
9 Climates. *Eng. Conf.* 523–540.  
10
- 11 Delgado-Torres, A.M., García-Rodríguez, L., 2010. Preliminary design of seawater and brackish  
12 water reverse osmosis desalination systems driven by low-temperature solar organic  
13 Rankine cycles (ORC). *Energy Convers. Manag.* 51, 2913–2920.  
14 doi:10.1016/j.enconman.2010.06.032  
15
- 16 Dey, P.K., 2004. Analytic hierarchy process helps evaluate project in Indian oil pipelines  
17 industry. *Int. J. Oper. Prod. Manag.* 24, 588–604. doi:10.1108/01443570410538122  
18
- 19 Dsilva Winfred Rufuss, D., Iniyani, S., Suganthi, L., Davies, P.A., 2017. Low mass fraction  
20 impregnation with graphene oxide (GO) enhances thermo-physical properties of paraffin for  
21 heat storage applications. *Thermochim. Acta* 655, 226–233. doi:10.1016/j.tca.2017.07.005  
22
- 23 Dsilva Winfred Rufuss, D., Iniyani, S., Suganthi, L., Davies, P.A., 2016. Solar stills: A  
24 comprehensive review of designs, performance and material advances. *Renew. Sustain.*  
25 *Energy Rev.* 63, 464–496. doi:10.1016/j.rser.2016.05.068  
26
- 27 El-Bahi, A., Inan, D., 1999. Analysis of a parallel double glass solar still with separate  
28 condenser. *Renew. Energy* 17, 509–521. doi:10.1016/S0960-1481(98)00768-X  
29
- 30 El-Bialy, E., Shalaby, S.M., Kabeel, A.E., Fathy, A.M., 2016. Cost analysis for several solar  
31 desalination systems. *Desalination* 384, 12–30. doi:10.1016/j.desal.2016.01.028  
32
- 33 El-Sebaili, A.A., Ramadan, M.R.I., Aboul-Enein, S., Salem, N., 2008. Thermal performance of a  
34 single-basin solar still integrated with a shallow solar pond. *Energy Convers. Manag.* 49,  
35 2839–2848. doi:10.1016/j.enconman.2008.03.002  
36
- 37 Elzahaby, A.M., Kabeel, A.E., Bassuoni, M.M., Elbar, A.R.A., 2016. Direct contact membrane  
38 water distillation assisted with solar energy. *Energy Convers. Manag.* 110, 397–406.  
39 doi:10.1016/j.enconman.2015.12.046  
40
- 41 Fath, H.E.S., El-Samanoudy, M., Fahmy, K., Hassabou, A., 2003. Thermal-economic analysis  
42 and comparison between pyramid-shaped and single-slope solar still configurations.  
43 *Desalination* 159, 69–79. doi:10.1016/S0011-9164(03)90046-4  
44
- 45 Gambier, A., Badreddin, E., 2003. Application of hybrid modeling and control techniques to  
46 desalination plants. *Desalination* 152, 175–184. doi:10.1016/S0011-9164(02)01060-3  
47
- 48 Gaur, M.K., Tiwari, G.N., 2010. Optimization of number of collectors for integrated PV/T  
49 hybrid active solar still. *Appl. Energy* 87, 1763–1772. doi:10.1016/j.apenergy.2009.10.019  
50
- 51 Hajeesh, M., 2010. *Journal of industrial engineering international., Journal of Industrial*  
52 *Engineering, International.* Islamic Azad University.  
53
- 54 Hajeesh, M., Al-Othman, A., 2005. Application of the analytical hierarchy process in the selection  
55 of desalination plants. *Desalination* 174, 97–108. doi:10.1016/j.desal.2004.09.005  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65

- 1 Hilal, N., Kochkodan, V., Al Abdulgader, H., Johnson, D., 2015a. A combined ion exchange-  
2 nanofiltration process for water desalination: II. Membrane selection. *Desalination* 363, 51–  
3 57. doi:10.1016/j.desal.2014.11.017  
4
- 5 Hilal, N., Kochkodan, V., Al Abdulgader, H., Mandale, S., Al-Jlil, S.A., 2015b. A combined ion  
6 exchange-nanofiltration process for water desalination: I. sulphate-chloride ion-exchange in  
7 saline solutions. *Desalination* 363, 44–50. doi:10.1016/j.desal.2014.11.016  
8  
9
- 10 Ismail, A., 1998. Fuzzy model reference learning control of multi-stage flash desalination plants.  
11 *Desalination* 116, 157–164. doi:10.1016/S0011-9164(98)00192-1  
12
- 13 Ismail, B.I., 2009. Design and performance of a transportable hemispherical solar still. *Renew.*  
14 *Energy* 34, 145–150. doi:10.1016/j.renene.2008.03.013  
15  
16
- 17 Jovanović, B., Filipović, J., Bakić, V., 2015. Prioritization of manufacturing sectors in Serbia for  
18 energy management improvement - AHP method. *Energy Convers. Manag.* 98, 225–235.  
19 doi:10.1016/j.enconman.2015.03.107  
20
- 21 Kabeel, A.E., El-Agouz, S.A., 2011. Review of researches and developments on solar stills.  
22 *Desalination*. doi:10.1016/j.desal.2011.03.042  
23
- 24 Kabeel, A.E., Hamed, A.M., El-Agouz, S.A., 2010. Cost analysis of different solar still  
25 configurations. *Energy* 35, 2901–2908. doi:10.1016/j.energy.2010.03.021  
26  
27
- 28 Kamaraj, M., Sundar, J.V., Subramanian, V., 2016. Dioxin sensing properties of graphene and  
29 hexagonal boron nitride based van der Waals solids: a first-principles study. *RSC Adv.* 6.  
30 doi:10.1039/c6ra18976h  
31
- 32 Kaushal, A., Varun, 2010. Solar stills: A review. *Renew. Sustain. Energy Rev.*  
33 doi:10.1016/j.rser.2009.05.011  
34  
35
- 36 Khanzada, N.K., Khan, S.J., Davies, P.A., 2017. Performance evaluation of reverse osmosis  
37 (RO) pre-treatment technologies for in-land brackish water treatment. *Desalination* 406, 44–  
38 50. doi:10.1016/j.desal.2016.06.030  
39
- 40 Kumar, S., Tiwari, G.N., 2009. Life cycle cost analysis of single slope hybrid (PV/T) active solar  
41 still. *Appl. Energy* 86, 1995–2004. doi:10.1016/j.apenergy.2009.03.005  
42  
43
- 44 Lee, S.K., Mogi, G., Hui, K.S., 2013. A fuzzy analytic hierarchy process (AHP)/data  
45 envelopment analysis (DEA) hybrid model for efficiently allocating energy R&D resources:  
46 In the case of energy technologies against high oil prices. *Renew. Sustain. Energy Rev.* 21,  
47 347–355. doi:10.1016/j.rser.2012.12.067  
48
- 49 Lee, S.K., Mogi, G., Li, Z., Hui, K.S., Lee, S.K., Hui, K.N., Park, S.Y., Ha, Y.J., Kim, J.W.,  
50 2011. Measuring the relative efficiency of hydrogen energy technologies for implementing  
51 the hydrogen economy: An integrated fuzzy AHP/DEA approach. *Int. J. Hydrogen Energy*  
52 36, 12655–12663. doi:10.1016/j.ijhydene.2011.06.135  
53  
54
- 55 Mamlook, R., Al-Rawajfeh, A.E., 2008. Fuzzy set implementation for controlling and evaluation  
56 of factors affecting multiple-effect distillers. *Desalination* 222, 541–547.  
57 doi:10.1016/j.desal.2007.01.131  
58  
59
- 60 Mamlook, R., Badran, O., 2007. Fuzzy sets implementation for the evaluation of factors  
61 affecting solar still production. *Desalination* 203, 394–402. doi:10.1016/j.desal.2006.02.024  
62  
63
- 64 Mojallizadeh, M.R., Badamchizadeh, M.A., 2017. Second-order fuzzy sliding-mode control of  
65

1 photovoltaic power generation systems. *Sol. Energy* 149, 332–340.  
2 doi:10.1016/j.solener.2017.04.014  
3

4 Mokheimer, E.M.A., Sahin, A.Z., Al-Sharafi, A., Ali, A.I., 2013. Modeling and optimization of  
5 hybrid wind-solar-powered reverse osmosis water desalination system in Saudi Arabia.  
6 *Energy Convers. Manag.* 75, 86–97. doi:10.1016/j.enconman.2013.06.002  
7

8 Mudgal, A., Davies, P.A., 2016. A cost-effective steam-driven RO plant for brackish  
9 groundwater. *Desalination* 385, 167–177. doi:10.1016/j.desal.2016.02.022  
10

11 Muftah, A.F., Alghoul, M.A., Fudholi, A., Abdul-Majeed, M.M., Sopian, K., 2014. Factors  
12 affecting basin type solar still productivity: A detailed review. *Renew. Sustain. Energy Rev.*  
13 doi:10.1016/j.rser.2013.12.052  
14

15 Murugavel, K.K., Sivakumar, S., Ahamed, J.R., Chockalingam, K.K.S.K., Srithar, K., 2010.  
16 Single basin double slope solar still with minimum basin depth and energy storing  
17 materials. *Appl. Energy* 87, 514–523. doi:10.1016/j.apenergy.2009.07.023  
18

19 Nakoa, K., Rahaoui, K., Date, A., Akbarzadeh, A., 2015. An experimental review on coupling of  
20 solar pond with membrane distillation. *Sol. Energy* 119, 319–331.  
21 doi:10.1016/j.solener.2015.06.010  
22

23 Nayi, K.H., Modi, K. V., 2018. Pyramid solar still: A comprehensive review. *Renew. Sustain.*  
24 *Energy Rev.* doi:10.1016/j.rser.2017.07.004  
25

26 Nixon, J.D., Dey, P.K., Davies, P.A., 2010. Which is the best solar thermal collection technology  
27 for electricity generation in north-west India? Evaluation of options using the analytical  
28 hierarchy process. *Energy* 35, 5230–5240. doi:10.1016/j.energy.2010.07.042  
29

30 Orfi, J., Loussif, N., Davies, P.A., 2016. Heat and mass transfer in membrane distillation used for  
31 desalination with slip flow. *Desalination* 381, 135–142. doi:10.1016/j.desal.2015.12.009  
32

33 Qasim, M., Darwish, N.A., Sarp, S., Hilal, N., 2015. Water desalination by forward (direct)  
34 osmosis phenomenon: A comprehensive review. *Desalination* 374, 47–69.  
35 doi:10.1016/j.desal.2015.07.016  
36

37 Rahbar, N., Esfahani, J.A., Asadi, A., 2016. An experimental investigation on productivity and  
38 performance of a new improved design portable asymmetrical solar still utilizing  
39 thermoelectric modules. *Energy Convers. Manag.* 118, 55–62.  
40 doi:10.1016/j.enconman.2016.03.052  
41

42 Rao Nulakani, N.V., Kamaraj, M., Subramanian, V., 2015. Coro-graphene and circumcoro-  
43 graphyne: novel two-dimensional materials with exciting electronic properties. *RSC Adv.* 5,  
44 78910–78916. doi:10.1039/C5RA14477A  
45

46 Rufuss, D.D.W., Iniyar, S., Suganthi, L., Davies, P.A., Akinaga, T., 2015. Analysis of solar still  
47 with nanoparticle incorporated phase change material for solar desalination application 8–  
48 12.  
49

50 Sakthivel, M., Shanmugasundaram, S., Alwarsamy, T., 2010. An experimental study on a  
51 regenerative solar still with energy storage medium - Jute cloth. *Desalination* 264, 24–31.  
52 doi:10.1016/j.desal.2010.06.074  
53

54 Sathyamurthy, R., El-Agouz, S.A., Nagarajan, P.K., Subramani, J., Arunkumar, T., Mageshbabu,  
55 D., Madhu, B., Bharathwaaj, R., Prakash, N., 2017. A Review of integrating solar collectors  
56 to solar still. *Renew. Sustain. Energy Rev.* doi:10.1016/j.rser.2016.11.223  
57  
58  
59  
60  
61  
62  
63  
64  
65

- 1 Shalaby, S.M., El-Bialy, E., El-Sebaili, A.A., 2016. An experimental investigation of a v-  
2 corrugated absorber single-basin solar still using PCM. *Desalination* 398, 247–255.  
3 doi:10.1016/j.desal.2016.07.042  
4
- 5 Sharshir, S.W., Peng, G., Yang, N., Eltawil, M.A., Ali, M.K.A., Kabeel, A.E., 2016. A hybrid  
6 desalination system using humidification-dehumidification and solar stills integrated with  
7 evacuated solar water heater. *Energy Convers. Manag.* 124, 287–296.  
8 doi:10.1016/j.enconman.2016.07.028  
9
- 10 Tanha Aminloei, R., Ghaderi, S.F., 2010. Generation planning in Iranian power plants with fuzzy  
11 hierarchical production planning. *Energy Convers. Manag.* 51, 1230–1241.  
12 doi:10.1016/j.enconman.2009.12.034  
13
- 14 Taylan, O., Kaya, D., Demirbas, A., 2016. An integrated multi attribute decision model for  
15 energy efficiency processes in petrochemical industry applying fuzzy set theory. *Energy  
16 Convers. Manag.* 117, 501–512. doi:10.1016/j.enconman.2016.03.048  
17
- 18 Tiwari, G.N., Sahota, L., 2017. Review on the energy and economic efficiencies of passive and  
19 active solar distillation systems. *Desalination* 401, 151–179.  
20 doi:10.1016/j.desal.2016.08.023  
21
- 22 Tsakiris, G., Spiliotis, M., Paritsis, S., Alexakis, D., 2009. Assessing the water potential of  
23 karstic saline springs by applying a fuzzy approach: The case of Almyros (Heraklion,  
24 Crete). *Desalination* 237, 54–64. doi:10.1016/j.desal.2007.12.022  
25
- 26 Velmurugan, V., Deenadayalan, C.K., Vinod, H., Srithar, K., 2008a. Desalination of effluent  
27 using fin type solar still. *Energy* 33, 1719–1727. doi:10.1016/j.energy.2008.07.001  
28
- 29 Velmurugan, V., Gopalakrishnan, M., Raghu, R., Srithar, K., 2008b. Single basin solar still with  
30 fin for enhancing productivity. *Energy Convers. Manag.* 49, 2602–2608.  
31 doi:10.1016/j.enconman.2008.05.010  
32
- 33 Velmurugan, V., Naveen Kumar, K.J., Noorul Haq, T., Srithar, K., 2009. Performance analysis  
34 in stepped solar still for effluent desalination. *Energy* 34, 1179–1186.  
35 doi:10.1016/j.energy.2009.04.029  
36
- 37 Velmurugan, V., Srithar, K., 2011. Performance analysis of solar stills based on various factors  
38 affecting the productivity - A review. *Renew. Sustain. Energy Rev.*  
39 doi:10.1016/j.rser.2010.10.012  
40
- 41 Velmurugan, V., Srithar, K., 2007. Solar stills integrated with a mini solar pond - analytical  
42 simulation and experimental validation. *Desalination* 216, 232–241.  
43 doi:10.1016/j.desal.2006.12.012  
44
- 45 Voropoulos, K., Mathioulakis, E., Belessiotis, V., 2001. Experimental investigation of a solar  
46 still coupled with solar collectors. *Desalination* 138, 103–110. doi:10.1016/S0011-  
47 9164(01)00251-X  
48
- 49 Wang, C.C., 2011. On the heat transfer correlation for membrane distillation. *Energy Convers.  
50 Manag.* 52, 1968–1973. doi:10.1016/j.enconman.2010.11.014  
51
- 52 Yadav, S., Sudhakar, K., 2015. Different domestic designs of solar stills: A review. *Renew.  
53 Sustain. Energy Rev.* 47, 718–731. doi:10.1016/j.rser.2015.03.064  
54
- 55 Yetilmezsoy, K., Abdul-Wahab, S.A., 2014. A composite desirability function-based modeling  
56 approach in predicting mass condensate flux of condenser in seawater greenhouse.  
57  
58  
59  
60  
61  
62  
63  
64  
65

1 Desalination 344, 171–180. doi:10.1016/j.desal.2014.03.029

2  
3 Yu, Z., Dexter, A., 2010. Hierarchical fuzzy control of low-energy building systems. Sol. Energy  
4 84, 538–548. doi:10.1016/j.solener.2009.03.014

5  
6 Zhang, Y., Peng, Y., Ji, S., Li, Z., Chen, P., 2015. Review of thermal efficiency and heat  
7 recycling in membrane distillation processes. Desalination. doi:10.1016/j.desal.2015.04.013

8  
9 Zilouchian, A., Jafar, M., 2001. Automation and process control of reverse osmosis plants using  
10 soft computing methodologies. Desalination 135, 51–59. doi:10.1016/S0011-  
11 9164(01)00138-2

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# Techno-economic analysis of solar stills using integrated fuzzy analytical hierarchy process and data envelopment analysis

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## Abstract

Desalination using solar stills is an ancient economic method for water desalination. Over the years, research and development in the area of solar still has resulted in increased distillate yield by means of integration of PCM (phase change material), photo-voltaic thermal (PVT), etc with the still. Nano-PCM is an upcoming technology which modifies the thermal performance of PCM. The aim of this research is to analyze the efficiency of 20 solar stills including nano-PCM based solar stills considering various input and output criteria using integrated fuzzy analytical hierarchy process (AHP) and data envelopment analysis (DEA). The efficiency derived here is relative with regard to the parameters and stills considered in this study. The result infers that, even though the productivity of stepped solar still with sun tracking system was high, but when techno-economic aspects were considered it is not among the top solar stills. The analysis indicated pyramid type solar still, single slope solar still with PVT, solar still with NPCM (paraffin + copper oxide), solar still with NPCM (paraffin + titanium dioxide) and solar still with PCM (paraffin) occupies the top five positions with relative efficiency of 100, 100, 88.47, 88.46 and 76.93% respectively.

## Keywords

Solar stills; Fuzzy AHP DEA; Relative efficiency; MCDM

## 1. Introduction

Solar desalination is a type of desalination process in which evaporation and condensation processes are driven by solar energy. Among the various types of solar desalination processes, solar stills are significant because of their low environmental impact, technical simplicity, low capital and maintenance cost (Dsilva Winfred Rufuss et al., 2016). Solar still can be used in extremely adverse environments, where there is no source of power for running the otherwise efficient desalination process (Dsilva Winfred Rufuss et al., 2016). Various researchers have modified the conventional solar still to improve its productivity. However this led to an increase in capital and maintenance cost. Studies carried out by earlier researchers (El-Bialy et al., 2016; Kabeel et al., 2010) determined the various costs of solar stills. However, there is no study found in the literature review so far which presents an optimized multi-criteria decision model (MCDM) that considers various criteria such as cost, employee's skill, productivity and technical

1 features of solar stills. These aspects need to be considered to ascertain the importance of each  
2 criteria for the selection of an ideal solar still that can be taken up for commercialization. This  
3 paper focuses on the MCDM approach to analyze the relative efficiency of solar stills based on  
4 various input and output criteria using an integrated fuzzy AHP model.  
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7 There are various criteria / parameters influencing a solar still such as atmospheric condition,  
8 design and economics. Atmospheric condition includes weather, ambient temperature, location,  
9 and latitude / longitude degrees. The design aspect includes area, glass cover inclination, brine  
10 depth, solar intensity, productivity, salt concentration and insulators. Economic aspects include  
11 present capital cost, annual maintenance/ operational cost, annual salvage value and cost of  
12 distilled water per litre. Hence selection of a solar still for commercialization needs to be done by  
13 considering such parameters as mentioned above. In this paper, fuzzy analytical hierarchy  
14 process (AHP) and data envelopment analysis (DEA) techniques are used to optimize some of  
15 the above mentioned parameters to arrive at an efficiency for each still relative to the parameters  
16 considered. Generally, technical (thermodynamic) efficiency will be used in the comparison of  
17 solar stills which considers only the technical aspects. In this study in addition to technical  
18 aspects other parameters are considered and the efficiency is obtained relative to the parameters  
19 and the stills considered. Technical efficiency is an absolute efficiency that can be compared  
20 across various stills while relative efficiency is constrained within the parameters used and the  
21 stills used in the study.  
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29 Many researchers have used fuzzy AHP techniques in desalination systems like multi-stage  
30 desalination (MSD), reverse osmosis (RO), multi-stage flash desalination (MSF), vapor  
31 compression (VC) and multi-effect distillation (MED). Fuzzy logic was used in controlling the  
32 upper saline water temperature of MSD plants. The research also focused on controlling various  
33 parameters for implementing MSD plants in the selected location (Ismail, 1998). Various  
34 operational constraints was adopted for implementing a RO desalination plant using fuzzy logic.  
35 The proposed methodology resulted in profit for the plant by increasing the availability and  
36 decreasing the manpower requirement for RO implementation (Zilouchian and Jafar, 2001).  
37 Fuzzy logic was adopted for analyzing MSF and RO systems using various control parameters  
38 like brine salinity, pre-heating (Gambier and Badreddin, 2003). Water potential was assessed for  
39 irrigation and human consumption using fuzzy logic. It was found that the water used for  
40 irrigation is more important than for human consumption (Tsakiris et al., 2009). Major factors  
41 which affect the daily productivity of solar still was analyzed using fuzzy logic (Mamlook and  
42 Badran, 2007). The same authors (Mamlook and Al-Rawajfeh, 2008) extended the research by  
43 using fuzzy logic to analyze which of those factors affect the productivity of MED. The various  
44 factors considered in their research included top saline water temperature, pH, temperature and  
45 salinity of the sea water. The AHP was used to determine the most suitable desalination process  
46 considering seven factors. The desalination processes considered in the research include MSD,  
47 MSF, RO and VC. The factors considered were water quality, recovery ratio, consumption of  
48 energy, efficiency of instruments and total cost (Hajeeh and Al-Othman, 2005). Various water  
49 conservation policies in Kuwait was analyzed using fuzzy AHP. Reusing treated brine water,  
50 promoting water conservation were some of their recommendations (Hajeeh, 2010). It is found  
51 from the literature that researchers have used fuzzy (Gambier and Badreddin, 2003; Ismail, 1998;  
52 Mamlook and Al-Rawajfeh, 2008; Mamlook and Badran, 2007; Tsakiris et al., 2009; Zilouchian  
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1 and Jafar, 2001), AHP (Hajeesh and Al-Othman, 2005), fuzzy AHP (Hajeesh, 2010) in  
2 desalination systems.  
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4 Integrated fuzzy AHP DEA approach can be used in energy related areas like solar photovoltaic,  
5 solar thermal, wind, desalination, power stations, materials and metallurgical applications to  
6 determine the weights of influencing parameters and to find the relative efficiency among a set  
7 of energy systems. Some researchers used fuzzy for finding the efficiency frontier in  
8 petrochemical industries (Taylan et al., 2016), generation sector (Mojallizadeh and  
9 Badamchizadeh, 2017; Tanha Aminloei and Ghaderi, 2010; Yu and Dexter, 2010). AHP was  
10 used for categorizing frontier energy industries in manufacturing sector (Jovanović et al., 2015)  
11 and integrated fuzzy AHP DEA approach has been used (Criswell and Thompson, 1996; Lee et  
12 al., 2013, 2011) for finding the relative efficiency of energy technology and hydrogen energy  
13 technologies.  
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19 Fuzzy logic helps in arriving at concrete estimates despite the vagueness of human thought. AHP  
20 helps in obtaining the relative weights for a set of critical attributes. The benefits of integrating  
21 fuzzy logic and AHP is to achieve precision in determining the relative importance of criteria  
22 and to develop a hierarchal structure for the multi-criteria decision making purpose. It can handle  
23 both linguistic assignment and numerical values. The benefits of applying an integrated fuzzy  
24 AHP approach to solar still is to determine the relative importance/weights of criteria that affects  
25 the performance and efficiency of solar still. DEA is a benchmarking technique employed to  
26 know the frontier in the selected area by estimating the relative efficiency of various decision  
27 making units (DMU). The benefits of integrating fuzzy AHP and DEA are to find the relative  
28 efficiency of DMU considering the weights of criteria obtained from fuzzy AHP. The advantage  
29 of implementing such an approach in solar still is to rank and prioritize the important criteria  
30 which is involved in the performance, efficiency and productivity of a solar still. Also, the  
31 relative efficiency of various solar stills by considering both technical and economic factors can  
32 be determined by giving due importance to the influencing criteria. The main objective of other  
33 techno-economic analysis (TEA) such as top-down or bottom-up cost approach is to determine  
34 the cost and technical feasibility of a particular system (here solar still) and compare the results.  
35 In this paper, the integrated approach (fuzzy AHP DEA) is a step ahead i.e., it helps to evaluate  
36 the relative efficiency of various solar stills considering several criteria simultaneously to arrive  
37 at an optimal decision. The pros of the integrated fuzzy AHP DEA are: comparative analysis of  
38 different variant of targets (here solar stills), any measurable criteria for all variant of solar still  
39 can be used in DEA, reverse coding of input and output criteria is possible, improvement criteria  
40 for the selected parameters can be identified and implemented, human preference can also be  
41 incorporated in DEA and fuzzy AHP DEA can be incorporated as a complement to other  
42 techniques. As every approaches have some cons associated with them, similarly this integrated  
43 fuzzy AHP DEA also has some cons such as: difficulty arises if there is a missing value in the  
44 dataset and weak assumption in DEA may lead to underestimation of the relative efficiency of  
45 decision making units.  
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58 Further, this integrated fuzzy AHP DEA approach can also be used in other energy-related areas  
59 including solar photovoltaic, solar thermal, wind, desalination, power stations, materials and  
60 metallurgical applications to determine the weights of influencing parameters and to find the  
61 relative efficiency among a set of energy systems. It is concluded that, even though various  
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1 researchers used fuzzy and AHP techniques in desalination systems, no one has used an  
2 integrated fuzzy-AHP-DEA analysis for analysing the different solar stills. Hence this research  
3 gap is addressed in this paper in addition to analyzing the innovative nano-PCM based solar stills  
4 from a techno-economic viewpoint. Nanoparticles were incorporated with PCM to modify its  
5 thermal properties like thermal conductivity, latent heat of vaporization and decreasing its  
6 charging and discharging rate (Dsilva Winfred Rufuss et al., 2017; Kamaraj et al., 2016). Even  
7 though nanoparticles improve the thermal properties of PCM in solar still, economic feasibility  
8 of the solar still with nano-PCM is one of the essential parameter that needs to be analyzed.  
9 Three input criteria namely fabrication/installation cost, skilled labour requirement and land area  
10 requirement are considered along with four output criteria namely annual cost, commercial  
11 potential, annual productivity and technical complexity. An integrated fuzzy-AHP-DEA analysis  
12 is carried out to determine the relative efficiencies of 20 solar stills (for which the data is  
13 available for the parameters considered). Also, the relative weights of each criteria and their  
14 importance with reference to a particular still are determined.

## 21 **2. Solar stills**

22 Desalination is an essential response to the growing water scarcity problem. It has been reported  
23 in our previous paper (Dsilva Winfred Rufuss et al., 2016) that, by the year 2030 half of the  
24 world population will experience severe water crisis. There are various desalination process  
25 available to desalinate the saline water, of which solar still holds its significance owing to its  
26 enviro-economic friendly nature (Kaushal and Varun, 2010; Sathyamurthy et al., 2017;  
27 Velmurugan and Srithar, 2011). Solar stills work by the evaporation and condensation processes  
28 similar to natural rain. A detailed classification of the desalination process and solar stills are  
29 represented graphically in Fig. 1 and Fig. 2 respectively. Low productivity is a major drawback  
30 in solar stills, and hence extensive research work has been carried to improve the productivity by  
31 modifying the design and operational parameters (Ahsan et al., 2012; Arunkumar et al., 2013,  
32 2012; Gaur and Tiwari, 2010; Murugavel et al., 2010; Rahbar et al., 2016; Sakthivel et al., 2010;  
33 Sharshir et al., 2016). The various design and operational parameters are comprehensively listed  
34 in Fig. 3.

35 The basic model of solar still is called a simple single slope solar still. This does not have any  
36 enhancements present for augmenting the productivity. The setup of simple single slope solar  
37 still is depicted in Fig. 4.

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47 **Insert Fig. 1.** Detailed tabulation showing classification of desalination processes (Nayi and  
48 Modi, 2018)

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51 **Insert Fig. 2.** Various types of solar stills (Tiwari and Sahota, 2017)

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54 **Insert Fig. 3.** Various climate, design and operational parameters influencing the productivity of  
55 solar still (Muftah et al., 2014)

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58 **Insert Fig. 4.** Setup of simple single slope solar still (Ali Samee et al., 2007)

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61 Researchers tried to add various components like sun tracker (Abdallah et al., 2008), photo-  
62 voltaic-thermal (PVT) (Kumar and Tiwari, 2009), collector (Badran and Al-Tahaine, 2005),  
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1 concentrator (Abdel-Rehim and Lasheen, 2007) and fin (Velmurugan et al., 2008a) to improve  
2 the productivity. This resulted in changes in other parameters also namely fabrication cost, skill  
3 level of labourers required to construct the solar still, complexity, land area requirement. The  
4 pictorial representations of solar stills with sun tracker, PVT, collector, concentrator and fin are  
5 depicted in Fig. 5, Fig. 6, Fig. 7, Fig. 8 and Fig. 9 respectively.  
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10 Insert **Fig. 5.** Schematic of solar still with sun tracking system (Abdallah et al., 2008)

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12 Insert **Fig. 6.** Solar still integrated with photo-voltaic thermal (PVT) system (Kumar and Tiwari,  
13 2009)  
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16 Insert **Fig. 7.** Solar still integrated with flat-plate collector (Badran and Al-Tahaine, 2005)  
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19 Insert **Fig. 8.** Schematic of solar still integrated with concentrators (Abdel-Rehim and Lasheen,  
20 2007)  
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23 Insert **Fig. 9.** Schematic setup of solar still integrated with fin (Velmurugan et al., 2008a)  
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25 Some researchers tried to modify the whole design of the solar still with unconventional shapes  
26 i.e, hemispherical (Ismail, 2009) and pyramid shapes (Fath et al., 2003). The design setup of  
27 hemispherical and pyramid solar still is depicted in Fig. 10 and Fig. 11 respectively. These  
28 modifications resulted in increasing the technical complexity and skilled labour required for  
29 fabrication, erection and maintenance and decreased the land area requirement as compared to  
30 conventional solar stills.  
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35 Insert **Fig. 10.** Pictorial representation of hemispherical solar still (Ismail, 2009)  
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38 Insert **Fig. 11.** Schematic configuration of pyramid type solar still (Fath et al., 2003)  
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40 The energy storage experts tried to integrate energy storage in solar still applications using wick,  
41 sponge (Velmurugan et al., 2008b), phase change materials (Shalaby et al., 2016) was integrated  
42 to solar stills to enhance the productivity. The solar still with wick, sponge and phase change  
43 materials are depicted in Fig. 12 and Fig. 13 respectively. This type of integration has no change  
44 on the land area requirement and has a slight increase on other factors like technical complexity,  
45 fabrication cost. In recent years, researchers have tried using nanoparticle impregnation in PCM  
46 for solar still applications. It was inferred from the literature that the impregnation of  
47 nanoparticles in PCM may either improve or impair the thermal properties of the base material  
48 (Dsilva Winfred Rufuss et al., 2017; Rao Nulakani et al., 2015).  
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54 As stated earlier these kinds of modifications end up with an increase in fabrication cost,  
55 technical complexity and skilled labour. Hence there is a need to identify a still with optimum  
56 factors. The criteria measured before the fabrication of solar stills are considered as input criteria  
57 and the criteria involved in the commercialization are considered as output criteria. In this  
58 research skilled labour requirement (SL), fabrication and installation cost (FC) and land area  
59 requirement (LA) are considered as the input criteria while economic impact (EI), commercial  
60 potential (CP), productivity (P) and technical complexity (TC) are considered as the output  
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1 criteria for the integrated fuzzy analytical hierarchy process. The analysis will help us to  
2 determine the unique contribution with respect to a certain criteria as well as its relative  
3 importance vis-à-vis other criteria. The traditional top down or bottom up approaches for techno-  
4 economic analysis will only present the overall cost comparison among the solar stills while the  
5 present analysis will clearly highlight how concentration on a specific input criteria will improve  
6 the overall efficiency of a solar still as well as the efficiency for each of the output criteria.  
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10 Insert **Fig. 12.** Schematic of solar still with sponge (Velmurugan et al., 2008b)

11 Insert **Fig. 13.** Solar still with phase change material (PCM) (Shalaby et al., 2016)

### 12 13 14 15 **3. Methodology**

16  
17 The empirical analysis is carried out by collecting various quantitative data on the input/output  
18 criteria of the solar still. In this research, fabrication costs (FC) for the 16 solar stills are taken  
19 from the literature (Abdallah et al., 2008; Abdallah and Badran, 2008; Abdel-Rehim and  
20 Lasheen, 2007; Ali Samee et al., 2007; Badran et al., 2005; Badran and Al-Tahaine, 2005; El-  
21 Bahi and Inan, 1999; El-Bialy et al., 2016; El-Sebaili et al., 2008; Fath et al., 2003; Ismail, 2009;  
22 Kabeel et al., 2010; Kumar and Tiwari, 2009; Velmurugan et al., 2009, 2008a, 2008b;  
23 Velmurugan and Srithar, 2007; Voropoulos et al., 2001) while for the remaining four stills -  
24 Solar stills with PCM, Nano PCM namely titanium dioxide, copper oxide, graphene oxide, data  
25 is obtained from the investigation carried out using the experimental setup in the Institute for  
26 Energy Studies, Anna University Chennai, India (Dsilva Winfred Rufuss et al., 2017; Rufuss et  
27 al., 2015). The various scales for the input/output criteria such as SL, LA, EI, CP, P and TC are  
28 tabulated in Table.1. The overall methodology adopted in the study using this integrated  
29 approach is clearly depicted in Fig. 14.  
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37 Insert **Table 1** Five point scale for various input and output criteria

38  
39 Insert **Fig. 14.** Overall methodology of integrated fuzzy AHP DEA

#### 40 41 42 43 **3.1. Applying the Fuzzy AHP method**

44  
45 AHP helps in finding the importance of criteria as a hierarchical structure. Experts were  
46 identified based on their domain knowledge in the field of renewable energy with special  
47 reference to solar energy and solar stills. They were asked to give the relative ratings for pairwise  
48 comparisons of the criteria. The consistency of each expert is determined as follows (Lee et al.,  
49 2013, 2011; Tanha Aminloei and Ghaderi, 2010; Taylan et al., 2016):  
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$$53 \quad CI = \frac{\lambda_{\max} - n}{n - 1} \quad (1)$$

54  
55 where  $\lambda_{\max}$  and  $n$  are the principal eigenvalue and dimension of the matrix. The pairwise  
56 comparison is accepted only if the  $CR \leq 0.10$ . Consistency ratio (CR) is the ratio of consistency  
57 index (CI) to random index (RI) [14, 15].  
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$$CR = \frac{CI}{RI} \quad (2)$$

The analysis is repeated for each expert for the input and output criteria. Though AHP captures the preference of expert, fuzzy AHP is used to determine the priority weights of the input and output criteria using hierarchical fuzzy decision making process.

The triangular fuzzy scale (TFN) and the inverse scale are given in Table 2.

Insert **Table 2** Triangular fuzzy (TFN) scale and its inverse TFN scale

$$\text{Let } M_{ij} = (l_{ij}, m_{ij}, u_{ij}) \quad (3)$$

$M_{ij}$  be the TFN for a fuzzy pair wise comparison judgment, where  $l$ ,  $m$  and  $u$  are lower, mid and upper limit respectively.

The synthetic extent value with respect to  $i^{\text{th}}$  object is calculated using the following formulas [14, 15]

$$S_i = \sum_{j=1}^m M_{ij} \left[ \sum_{i=1}^n \sum_{j=1}^m M_{ij} \right]^{-1} \quad (4)$$

$$\sum_{j=1}^m M_{ij} = \left( \sum_{j=1}^m l_{ij}, \sum_{j=1}^m m_{ij}, \sum_{j=1}^m u_{ij} \right), i = 1, 2, 3, 4, \dots, n \quad (5)$$

$$\sum_{i=1}^n \sum_{j=1}^m M_{ij} = \left( \sum_{i=1}^n \sum_{j=1}^m l_{ij}, \sum_{i=1}^n \sum_{j=1}^m m_{ij}, \sum_{i=1}^n \sum_{j=1}^m u_{ij} \right) \quad (6)$$

$$\left[ \sum_{i=1}^n \sum_{j=1}^m M_{ij} \right]^{-1} = \left( \frac{1}{\sum_{i=1}^n \sum_{j=1}^m u_{ij}}, \frac{1}{\sum_{i=1}^n \sum_{j=1}^m m_{ij}}, \frac{1}{\sum_{i=1}^n \sum_{j=1}^m l_{ij}} \right) \quad (7)$$

The value of  $S_i$  is then determined and the degree of possibility of  $S_j = (l_j, m_j, u_j) \geq S_i = (l_i, m_i, u_i)$  is expressed by the following equation [14, 15].

$$V(S_j \geq S_i) = \text{height}(S_i \cap S_j) = u_{S_j}(d) = \begin{cases} 1, & \text{if } m_j \geq m_i \\ 0, & \text{if } l_i \geq u_j \\ \frac{l_i - u_j}{(m_j - u_j) - (m_i - l_i)}, & \text{otherwise} \end{cases} \quad (8)$$

The minimum degree of possibility  $d'$  (i) of  $V(S_i \geq S_j)$  for  $i=1,2,3,\dots,k$  and  $j= 1,2,3,\dots,k$  is calculated using [14, 15]

$$V(S \geq S_1, S_2, \dots, S_k) \text{ for } i = 1, 2, \dots, k = V[(S \geq S_1) \text{ and } (S \geq S_2) \text{ and } \dots (S \geq S_k)] \\ = \min V(S \geq S_i) \text{ for } i = 1, 2, \dots, k \quad (9)$$

1 Assume  $d'(A_i) = \min V (S \geq S_i)$  for  $i = 1, 2, \dots, k$

2  
3 The weight vector is found using the equation [14, 15]

4  
5  
6 
$$W' = (d'(A_1), d'(A_2), \dots, d'(A_n))^T$$
 where  $A_i (i = 1, 2, 3, 4, \dots, n)$  are the  $n$  elements (10)

7  
8  
9 The weight vectors are then normalized to get the relative weight using the formula [14, 15]

10  
11 
$$W = (d(A_1), d(A_2), \dots, d(A_n))^T$$
 (11)

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14 where  $W$  is a non-fuzzy number indicating the relative weight of the criteria.

### 15 16 17 **3.2. Measuring the relative efficiency using DEA**

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19 The relative efficiency of various types of solar still is calculated by using DEA approach. Fig. 15, shows the hierarchy of the DEA process which consist of three input and four output criteria. DEA is an analytical technique used to determine the efficient utilization of resources in a decision making unit (DMU). The model developed by (Charnes et al., 1978) is adopted to find the relative efficiency. The DEA formulation is as follows:

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27 There are  $n$  units with  $s$  outputs denoted by  $Y_{rk}$ ,  $r=1, 2, \dots, s$  and  $m$  inputs denoted by  $X_{ik}$ ,  $i=1, 2, \dots, m$ , the efficiency score ( $h_k$ ) for the  $DMU_k$

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32 
$$h_k = \text{Max} \frac{\sum_{r=1}^s u_{rk} Y_{rk}}{\sum_{i=1}^m v_{ik} X_{ik}}$$
 (12)

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35 where  $u_r$  and  $v_i$  are non-negative weights.

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38 In order to obtain the efficiency of DMU in such a manner that they are not greater than 1, the equations are rewritten as follows:

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42 
$$\text{s. t } \frac{\sum_{r=1}^s u_{rk} Y_{rk}}{\sum_{i=1}^m v_{ik} X_{ik}} \leq 1, \text{ for } j = 1, 2, 3, \dots, n$$
 (13)

43  
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45  
46 
$$u_{rk} > 0, \text{ for } r = 1, 2, 3, \dots, s$$
 (14)

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48  
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50 
$$v_{ik} > 0, \text{ for } i = 1, 2, 3, \dots, m$$
 (15)

51  
52 The efficiency ranges between 0 and 1. The system with maximum efficiency is the system lying in the efficient frontier and is considered to be the best as compared to the other systems. The above equation is transformed to a linear programming problem one for each DMU as follows (Lee et al., 2013, 2011):

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$$h_k = \max \sum_{r=1}^s u_r Y_{rk}$$
 (16)

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$$\text{s. t } \sum_{i=1}^m v_i X_{ij} - \sum_{r=1}^s u_r Y_{rj} \geq 0 \text{ for } j = 1, 2, 3, \dots, n \quad (17)$$

$$\sum_{i=1}^m v_i X_{ik} = 1 \quad (18)$$

$$u_r \geq 0 \text{ for } r = 1, 2, 3, \dots, s \quad (19)$$

$$v_i \geq 0 \text{ for } i = 1, 2, 3, \dots, m \quad (20)$$

Insert **Fig. 15**. Hierarchical structure of various input and output criteria used in DEA

The model obtained is referred to as the CCR model. This CCR model assumes that the production components are constant return-to-scale. Assurance region (AR) is selected to avoid null outputs in the analysis. In AR-CCR model, a set of new constrains will be included in the above model in such a way that the weights are restricted with a lower and upper bound.

$$L_{1,2} \leq \frac{u_{j1}}{u_{j2}} \leq U_{1,2} \quad (21)$$

where  $L_{1,2}$  and  $U_{1,2}$  are lower and upper bound.  $u_{j1}$  and  $u_{j2}$  present the weight achieved by the DMU<sub>j</sub>. By adding equation 21 in the CCR model, AR-CCR model is obtained.

#### 4. Results and discussion

Researchers have been working in various types of solar still and have identified several technically viable stills. However, for a still to be made commercially viable we need to study the social and economic aspects in addition to technical aspects. Such a study which integrates energy production and energy efficiency parameters across various energy systems from a techno-economic viewpoint needs to be done to obtain a realistic estimate of an energy system. In this study, energy production parameters namely productivity, commercial potential; energy efficiency parameters namely technical complexity; economic parameters namely fabrication and maintenance costs; social parameters namely employee skill level, land area have been considered and studied in the MCDM analysis.

##### 4.1. Fuzzy AHP DEA approach

Experts were chosen based on their teaching, research and industrial experience in the domain area namely renewable energy, desalination and solar stills. The choice of the number of experts depend on the availability of the experts and their accessibility. There is no literature available which specifies the number of experts to be chosen for AHP based decision making process (Nixon et al., 2010). The outcome varies as the expert size varies since, greater the number of experts, arriving at a consensus becomes complex due to the uncertainty in the decision making process. The judgement of the experts should have minimum variability with high level of confidence and convergence. In general practice, literatures indicate that smaller expert size kindles effective impact and involvement which lead to the group unanimity (Dey, 2004; Nixon

et al., 2010). The consistency ratio of the experts was found and the response of 10 experts was then used for further analysis. The demographic details of the experts are given in Table 3.

Insert **Table 3** Demographic details of the experts

The experts were asked to rank the relative importance of the various input and output criteria using AHP relative importance scale. Using the relative importance score given by the experts, the CR for each expert was determined for each of the input/output criteria and the values are tabulated in Table 4. From the Table 4, it is found that the CR value for all the ten experts are less than 0.1. Hence all the experts' opinion are considered valid and used for further analysis. The synthetic weight was then determined for the input and output criteria for each of the expert. The procedure adopted is presented for one expert for the input criteria. This procedure is repeated for all the experts as well as for the output criteria. The pairwise comparison of TFN value of one expert (expert-1) using Table 2 is shown in Table 5.

Insert **Table 4** CR value for the input and output criteria

Insert **Table 5** Pairwise comparison

Using the equation (4), (5), (6) and (7), the synthetic weights are obtained as follows.

$$S_1(\text{SL}) = (3, 3.666, 4.5) \otimes \left( \frac{1}{12.333}, \frac{1}{10.166}, \frac{1}{8.3} \right) \quad (23)$$

$$S_2(\text{FC}) = (1.8, 2, 2.33) \otimes \left( \frac{1}{12.33}, \frac{1}{10.166}, \frac{1}{8.3} \right) \quad (24)$$

$$S_3(\text{LA}) = (3.5, 4.5, 5.5) \otimes \left( \frac{1}{12.33}, \frac{1}{10.166}, \frac{1}{8.3} \right) \quad (25)$$

The degree of possibility  $S_j$  (equation 8) is given in Table 6.

Insert **Table 6** Comparing the values of fuzzy synthetic extent

The minimum degree of possibility  $d'(i)$  found using equation 9 is as follows:

$$d'(1) = \min V(S_1 \geq S_2, S_3) = 0.7591$$

$$d'(2) = \min V(S_2 \geq S_1, S_3) = 0$$

$$d'(3) = \min V(S_3 \geq S_1, S_2) = 1$$

Using equation 10, the weight vector is determined and their relative weights are shown below

$$W' = (0.7591, 0, 1)^T$$

Hence the relative weights are

$$W = (0.43155, 0, 0.56845)^T$$

1 The same procedure is repeated for each of the ten experts and the weights are listed in Table 7.  
2 The lower and upper bound is calculated by considering the minimum and maximum values of  
3 the weights. These weights are then incorporated in Charnes, Cooper, Rhodes (CCR) model. The  
4 upper and lower bounds for the input criteria are tabulated in Table 8. Similarly the weights of  
5 ten experts are determined for the output criteria and the values are presented in Table 9. Also,  
6 the lower bound and the upper bound values are obtained for the output criteria and the  
7 corresponding values are tabulated in Table 10. The quantitative data used in the analysis for the  
8 20 stills is presented in Table 11 and the radar chart depicting their input/output criteria is  
9 represented in Fig. 16. From the radar chart, it is clear that certain solar stills (such as  
10 still with wick, hemispherical solar still, stepped still, weir type still, still with collector,  
11 concentrator and fin), should improve its commercial potential and productivity or reduce their  
12 fabrication cost to reach the top position. The data is normalized and used for further analysis.  
13 DEA model is run using the add-in package available in Microsoft Excel. The weight  
14 distribution of AR-CCR (with weight restriction) for the 20 stills is shown in Table 12.  
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22 **Insert Table 7** Fuzzy AHP weights for Input criteria

23 **Insert Table 8** Upper and lower bounds of weights input criteria

24 **Insert Table 9** Fuzzy AHP weights for output criteria

25 **Insert Table 10** Upper and lower bounds of weights output criteria

26 **Insert Table 11** Input/output criteria for 20 solar stills

27 **Insert Table 12** Weight distribution of AR-CCR (with weight restriction)

28 **Insert Fig. 16.** Input/output criteria for the twenty solar stills

29 Here the various stills are considered as decision making units. The productive efficiency  
30 decomposition of the various DMU's (in this case, various solar stills) is obtained from the AR-  
31 CCR model and given in Table 13. The efficiency decomposition of twenty solar stills is  
32 depicted in Fig. 17. For the solar still with wick and fin to be on the frontier, it is necessary to  
33 reduce the skilled labour requirement or increase its economic impact. For a transportable  
34 hemispherical solar still to reach the efficiency frontier, we should reduce its fabrication cost and  
35 land area requirement. In the case of solar still with wick and sponge, we should improve its  
36 commercial potential and technical complexity. In the case of the stepped solar still with sun  
37 tracking system, we should reduce its fabrication cost, skilled labour requirement and improve its  
38 economic impact. For a weir type solar still, we should focus on improving its economic impact  
39 and productivity. The solar still with sponge & pond, shallow pond and condenser require  
40 improvements in their economic impact and productivity or reduce their fabrication cost and land  
41 area requirement. For the solar still with collector and concentrator, we should either reduce its  
42 technical complexity and skilled labour requirement or improve its economic impact and  
43 commercial potential. Pyramid type solar stills should improve its commercial potential,  
44 economic impact and productivity. In the case of solar still with PCM and nano-PCM's, it is  
45 important to reduce fabrication cost and skilled labour requirement or improve its economic  
46 impact and commercial potential to reach the efficiency frontier.  
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## Insert **Table 13** Efficiency and rank of solar stills

### Insert **Fig. 17.** Efficiency decomposition of twenty solar stills

When the efficiency of a solar still is 1.00 (100%), then that particular solar still is in the efficiency frontier and is considered to be the most efficient solar still considering all the input and output criteria. From the DEA results, a pyramid type solar still and single slope solar still with PVT lies in the efficiency frontier and are the most efficient solar stills. Solar still with Nano PCM (Copper oxide) and solar still with Nano PCM (Titanium dioxide) come next with the efficiency of 0.8847 and 0.8846 respectively. Solar still with graphene oxide, though technically the best solar still (Dsilva Winfred Rufuss et al., 2016; Rufuss et al., 2015), is completely ruled out since its efficiency is only 0.487. In the case of NPCM based solar still (solar still with copper oxide and titanium dioxide) [ranked no.3 and 4] to reach the efficiency frontier there is 12% lag. Solar still with copper oxide needs to either decrease its skilled labour requirement or increase its economic impact / commercial potential to become the most efficient solar still. Similarly for solar still with titanium dioxide to improve its efficiency position, research has to be done to improve its economic impact and commercial potential.

To summarize, among the various types of solar still technologies, the top five stills which are both technically and economically efficient are pyramid type solar still, single slope solar still with PVT, solar still with NPCM (copper oxide), solar still with NPCM (titanium dioxide) and solar still with PCM. The remaining stills are either technically strong or economically strong. For example, transportable hemispherical solar still and stepped solar still with sun tracking system are technically strong, but when we consider both technical and economic aspects, it is not found among the best solar still technologies. In general, it is recommended that the relative efficiency of solar stills can be enhanced either by decreasing the cost of skilled labour (SL), fabrication (FC), and land area requirement (LA) or by increasing its economic impact (EI), commercial potential (CP), productivity (P) and technical complexity (TC). Hence future research and development in solar stills must be carried out by considering both technical and economic aspects for effective commercialization of solar still technology.

#### **4.2. Applications and recommendation for future works**

This techno-economic approach to solar stills will be useful for industrialist to identify the pros and cons of various solar stills. It will help them to select a solar still based on their indigenous resource availability and their strengths. For example, if there is a policy initiative to give a 50% subsidy towards fabrication, then the ranking of stills will undergo a change i.e., pyramid type solar still will take a lead role followed by solar still with NPCM, solar still with pond, and then solar still with PCM. Thus either by increasing the level of the output criteria like productivity, economic impact or decreasing the level of input criteria such as capital cost, labour, efficiency of the energy system can be improved. The values of each parameter in the decomposition table indicates areas where a certain stills can be improved to make it competitive and to reach the efficiency frontier. This integrated fuzzy AHP DEA approach can be used in other desalination system to find the relative efficiency of desalination processes like multi-effect flash distillation (Baig et al., 2011; Choi, 2016; Elzahaby et al., 2016), membrane distillation (Nakoa et al., 2015; Orfi et al., 2016; Wang, 2011; Zhang et al., 2015), FO & RO(forward and reverse osmosis)



(Altaee and Hilal, 2015; Delgado-Torres and García-Rodríguez, 2010; Khanzada et al., 2017; Mokheimer et al., 2013; Mudgal and Davies, 2016; Qasim et al., 2015), ion exchange (AlMarzooqi et al., 2014; Hilal et al., 2015a, 2015b), seawater greenhouse techniques (Davies et al., 2004, 2006; Davies and Knowles, 2006; Davies and Paton, 2005; Yetilmezsoy and Abdul-Wahab, 2014), etc. by selecting the techno-economic input/output parameters.

This integrated approach can also be employed in other applications like renewable energy sectors (solar, wind, tidal, biomass, etc.) and power generation sectors (conventional and non-conventional power plants). In the renewable energy sector, this approach can be used to determine the energy production efficiency in solar and wind. In solar, the relative efficiency of energy production can be investigated by considering various input/output parameters like capacity, location, demand, complexity, land area requirement, etc. for various solar cells such as crystalline silicon solar cell, hybrid solar cell, gallium arsenide solar cell, polymer solar cell, and solid-state solar cell. The energy production and energy efficiency in the wind energy sector can be analyzed using this integrated fuzzy AHP DEA approach by considering input/output parameters like turbine capacity, tower height, power production, land and location, number of blades for various types of wind turbine like vertical axis wind turbine, horizontal axis wind turbine, multi-axis wind turbine, etc. A system which lies on the efficiency frontier can be used as a benchmark for other resource/system to emulate by strengthening of their respective criteria.

## 5. Conclusions

An integrated fuzzy analytical hierarchy process and data envelopment approach is used to analyze the relative efficiency of various solar stills based on various input and output criteria. Relative weights of criteria are found using fuzzy AHP approach and the overall efficiency score for the 20 solar stills is determined using the data envelopment analysis. Though many solar stills are technically strong (high productivity) yet they are not economically strong (high fabrication, operation and maintenance cost) and hence do not find a place among the top solar stills. When the productivity is considered as the only criteria, then hybrid solar still, solar still sun tracking and solar still with solar pond is found to be at the top (Dsilva Winfred Rufuss et al., 2016; Kabeel and El-Agouz, 2011; Yadav and Sudhakar, 2015), but when the other parameters such as fabrication cost, economic impact, etc are considered then pyramid type solar still, still with PVT, still with NPCM (CuO, TiO<sub>2</sub>) and PCM goes to the top five position with 100, 100, 88, 88 and 77% relative efficiency respectively. It is inferred that, solar still with copper oxide requires a reduction in the skilled labour requirement or an improvement in its commercial potential and economic impact to reach the top position. Similarly, overall efficiency of other solar stills can be increased by concentrating on the pinpointed areas.

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## References

- Abdallah, S., Badran, O., Abu-Khader, M.M., 2008. Performance evaluation of a modified design of a single slope solar still. *Desalination* 219, 222–230. doi:10.1016/j.desal.2007.05.015
- Abdallah, S., Badran, O.O., 2008. Sun tracking system for productivity enhancement of solar still. *Desalination* 220, 669–676. doi:10.1016/j.desal.2007.02.047
- Abdel-Rehim, Z.S., Lasheen, A., 2007. Experimental and theoretical study of a solar desalination system located in Cairo, Egypt. *Desalination* 217, 52–64. doi:10.1016/j.desal.2007.01.012
- Ahsan, A., Imteaz, M., Rahman, A., Yusuf, B., Fukuhara, T., 2012. Design, fabrication and performance analysis of an improved solar still. *Desalination* 292, 105–112. doi:10.1016/j.desal.2012.02.013
- Ali Samee, M., Mirza, U.K., Majeed, T., Ahmad, N., 2007. Design and performance of a simple single basin solar still. *Renew. Sustain. Energy Rev.* doi:10.1016/j.rser.2005.03.003
- AlMarzooqi, F.A., Al Ghaferi, A.A., Saadat, I., Hilal, N., 2014. Application of Capacitive Deionisation in water desalination: A review. *Desalination*. doi:10.1016/j.desal.2014.02.031
- Altaee, A., Hilal, N., 2015. High recovery rate NF-FO-RO hybrid system for inland brackish water treatment. *Desalination* 363, 19–25. doi:10.1016/j.desal.2014.12.017
- Arunkumar, T., Jayaprakash, R., Ahsan, A., Denkenberger, D., Okundamiya, M.S., 2013. Effect of water and air flow on concentric tubular solar water desalting system. *Appl. Energy* 103, 109–115. doi:10.1016/j.apenergy.2012.09.014
- Arunkumar, T., Jayaprakash, R., Denkenberger, D., Ahsan, A., Okundamiya, M.S., kumar, S., Tanaka, H., Aybar, H.Ş., 2012. An experimental study on a hemispherical solar still. *Desalination* 286, 342–348. doi:10.1016/j.desal.2011.11.047
- Badran, A.A., Al-Hallaq, A.A., Eyal Salman, I.A., Odat, M.Z., 2005. A solar still augmented with a flat-plate collector. *Desalination* 172, 227–234. doi:10.1016/j.desal.2004.06.203
- Badran, O.O., Al-Tahaine, H.A., 2005. The effect of coupling a flat-plate collector on the solar still productivity. *Desalination* 183, 137–142. doi:10.1016/j.desal.2005.02.046
- Baig, H., Antar, M.A., Zubair, S.M., 2011. Performance evaluation of a once-through multi-stage flash distillation system: Impact of brine heater fouling. *Energy Convers. Manag.* 52, 1414–1425. doi:10.1016/j.enconman.2010.10.004
- Charnes, A., Cooper, W.W., Rhodes, E., 1978. Measuring the efficiency of decision making units. *Eur. J. Oper. Res.* 2, 429–444. doi:10.1016/0377-2217(78)90138-8
- Choi, S.H., 2016. On the brine re-utilization of a multi-stage flashing (MSF) desalination plant. *Desalination* 398, 64–76. doi:10.1016/j.desal.2016.07.020
- Criswell, D.R., Thompson, R.G., 1996. Data envelopment analysis of space and terrestrially-based large scale commercial power systems for earth: A prototype analysis of their relative economic advantages. *Sol. Energy*. doi:10.1016/0038-092X(95)00113-6
- Davies, P.A., Harris, I., Knowles, P.R., 2006. Cooling of greenhouses using seawater: A solar driven liquid-desiccant cycle for greenhouse cooling in hot climates, in: *Acta Horticulturae*. pp. 139–146.

- 1 Davies, P.A., Knowles, P.R., 2006. Seawater bitterns as a source of liquid desiccant for use in  
2 solar-cooled greenhouses. *Desalination* 196, 266–279. doi:10.1016/j.desal.2006.03.010  
3
- 4 Davies, P.A., Paton, C., 2005. The Seawater Greenhouse in the United Arab Emirates: thermal  
5 modelling and evaluation of design options. *Desalination* 173, 103–111.  
6 doi:10.1016/j.desal.2004.06.211  
7
- 8 Davies, P., Turner, K., Paton, C., 2004. Potential of the Seawater Greenhouse in Middle Eastern  
9 Climates. *Eng. Conf.* 523–540.  
10
- 11 Delgado-Torres, A.M., García-Rodríguez, L., 2010. Preliminary design of seawater and brackish  
12 water reverse osmosis desalination systems driven by low-temperature solar organic  
13 Rankine cycles (ORC). *Energy Convers. Manag.* 51, 2913–2920.  
14 doi:10.1016/j.enconman.2010.06.032  
15
- 16 Dey, P.K., 2004. Analytic hierarchy process helps evaluate project in Indian oil pipelines  
17 industry. *Int. J. Oper. Prod. Manag.* 24, 588–604. doi:10.1108/01443570410538122  
18
- 19 Dsilva Winfred Rufuss, D., Iniyar, S., Suganthi, L., Davies, P.A., 2017. Low mass fraction  
20 impregnation with graphene oxide (GO) enhances thermo-physical properties of paraffin for  
21 heat storage applications. *Thermochim. Acta* 655, 226–233. doi:10.1016/j.tca.2017.07.005  
22
- 23 Dsilva Winfred Rufuss, D., Iniyar, S., Suganthi, L., Davies, P.A., 2016. Solar stills: A  
24 comprehensive review of designs, performance and material advances. *Renew. Sustain.*  
25 *Energy Rev.* 63, 464–496. doi:10.1016/j.rser.2016.05.068  
26
- 27 El-Bahi, A., Inan, D., 1999. Analysis of a parallel double glass solar still with separate  
28 condenser. *Renew. Energy* 17, 509–521. doi:10.1016/S0960-1481(98)00768-X  
29
- 30 El-Bialy, E., Shalaby, S.M., Kabeel, A.E., Fathy, A.M., 2016. Cost analysis for several solar  
31 desalination systems. *Desalination* 384, 12–30. doi:10.1016/j.desal.2016.01.028  
32
- 33 El-Sebaili, A.A., Ramadan, M.R.I., Aboul-Enein, S., Salem, N., 2008. Thermal performance of a  
34 single-basin solar still integrated with a shallow solar pond. *Energy Convers. Manag.* 49,  
35 2839–2848. doi:10.1016/j.enconman.2008.03.002  
36
- 37 Elzahaby, A.M., Kabeel, A.E., Bassuoni, M.M., Elbar, A.R.A., 2016. Direct contact membrane  
38 water distillation assisted with solar energy. *Energy Convers. Manag.* 110, 397–406.  
39 doi:10.1016/j.enconman.2015.12.046  
40
- 41 Fath, H.E.S., El-Samanoudy, M., Fahmy, K., Hassabou, A., 2003. Thermal-economic analysis  
42 and comparison between pyramid-shaped and single-slope solar still configurations.  
43 *Desalination* 159, 69–79. doi:10.1016/S0011-9164(03)90046-4  
44
- 45 Gambier, A., Badreddin, E., 2003. Application of hybrid modeling and control techniques to  
46 desalination plants. *Desalination* 152, 175–184. doi:10.1016/S0011-9164(02)01060-3  
47
- 48 Gaur, M.K., Tiwari, G.N., 2010. Optimization of number of collectors for integrated PV/T  
49 hybrid active solar still. *Appl. Energy* 87, 1763–1772. doi:10.1016/j.apenergy.2009.10.019  
50
- 51 Hajeesh, M., 2010. *Journal of industrial engineering international., Journal of Industrial*  
52 *Engineering, International.* Islamic Azad University.  
53
- 54 Hajeesh, M., Al-Othman, A., 2005. Application of the analytical hierarchy process in the selection  
55 of desalination plants. *Desalination* 174, 97–108. doi:10.1016/j.desal.2004.09.005  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65

- 1 Hilal, N., Kochkodan, V., Al Abdulgader, H., Johnson, D., 2015a. A combined ion exchange-  
2 nanofiltration process for water desalination: II. Membrane selection. *Desalination* 363, 51–  
3 57. doi:10.1016/j.desal.2014.11.017  
4
- 5 Hilal, N., Kochkodan, V., Al Abdulgader, H., Mandale, S., Al-Jlil, S.A., 2015b. A combined ion  
6 exchange-nanofiltration process for water desalination: I. sulphate-chloride ion-exchange in  
7 saline solutions. *Desalination* 363, 44–50. doi:10.1016/j.desal.2014.11.016  
8  
9
- 10 Ismail, A., 1998. Fuzzy model reference learning control of multi-stage flash desalination plants.  
11 *Desalination* 116, 157–164. doi:10.1016/S0011-9164(98)00192-1  
12
- 13 Ismail, B.I., 2009. Design and performance of a transportable hemispherical solar still. *Renew.*  
14 *Energy* 34, 145–150. doi:10.1016/j.renene.2008.03.013  
15  
16
- 17 Jovanović, B., Filipović, J., Bakić, V., 2015. Prioritization of manufacturing sectors in Serbia for  
18 energy management improvement - AHP method. *Energy Convers. Manag.* 98, 225–235.  
19 doi:10.1016/j.enconman.2015.03.107  
20
- 21 Kabeel, A.E., El-Agouz, S.A., 2011. Review of researches and developments on solar stills.  
22 *Desalination*. doi:10.1016/j.desal.2011.03.042  
23
- 24 Kabeel, A.E., Hamed, A.M., El-Agouz, S.A., 2010. Cost analysis of different solar still  
25 configurations. *Energy* 35, 2901–2908. doi:10.1016/j.energy.2010.03.021  
26  
27
- 28 Kamaraj, M., Sundar, J.V., Subramanian, V., 2016. Dioxin sensing properties of graphene and  
29 hexagonal boron nitride based van der Waals solids: a first-principles study. *RSC Adv.* 6.  
30 doi:10.1039/c6ra18976h  
31
- 32 Kaushal, A., Varun, 2010. Solar stills: A review. *Renew. Sustain. Energy Rev.*  
33 doi:10.1016/j.rser.2009.05.011  
34  
35
- 36 Khanzada, N.K., Khan, S.J., Davies, P.A., 2017. Performance evaluation of reverse osmosis  
37 (RO) pre-treatment technologies for in-land brackish water treatment. *Desalination* 406, 44–  
38 50. doi:10.1016/j.desal.2016.06.030  
39
- 40 Kumar, S., Tiwari, G.N., 2009. Life cycle cost analysis of single slope hybrid (PV/T) active solar  
41 still. *Appl. Energy* 86, 1995–2004. doi:10.1016/j.apenergy.2009.03.005  
42  
43
- 44 Lee, S.K., Mogi, G., Hui, K.S., 2013. A fuzzy analytic hierarchy process (AHP)/data  
45 envelopment analysis (DEA) hybrid model for efficiently allocating energy R&D resources:  
46 In the case of energy technologies against high oil prices. *Renew. Sustain. Energy Rev.* 21,  
47 347–355. doi:10.1016/j.rser.2012.12.067  
48
- 49 Lee, S.K., Mogi, G., Li, Z., Hui, K.S., Lee, S.K., Hui, K.N., Park, S.Y., Ha, Y.J., Kim, J.W.,  
50 2011. Measuring the relative efficiency of hydrogen energy technologies for implementing  
51 the hydrogen economy: An integrated fuzzy AHP/DEA approach. *Int. J. Hydrogen Energy*  
52 36, 12655–12663. doi:10.1016/j.ijhydene.2011.06.135  
53  
54
- 55 Mamlook, R., Al-Rawajfeh, A.E., 2008. Fuzzy set implementation for controlling and evaluation  
56 of factors affecting multiple-effect distillers. *Desalination* 222, 541–547.  
57 doi:10.1016/j.desal.2007.01.131  
58  
59
- 60 Mamlook, R., Badran, O., 2007. Fuzzy sets implementation for the evaluation of factors  
61 affecting solar still production. *Desalination* 203, 394–402. doi:10.1016/j.desal.2006.02.024  
62  
63
- 64 Mojallizadeh, M.R., Badamchizadeh, M.A., 2017. Second-order fuzzy sliding-mode control of  
65

1 photovoltaic power generation systems. *Sol. Energy* 149, 332–340.  
2 doi:10.1016/j.solener.2017.04.014  
3

4 Mokheimer, E.M.A., Sahin, A.Z., Al-Sharafi, A., Ali, A.I., 2013. Modeling and optimization of  
5 hybrid wind-solar-powered reverse osmosis water desalination system in Saudi Arabia.  
6 *Energy Convers. Manag.* 75, 86–97. doi:10.1016/j.enconman.2013.06.002  
7

8 Mudgal, A., Davies, P.A., 2016. A cost-effective steam-driven RO plant for brackish  
9 groundwater. *Desalination* 385, 167–177. doi:10.1016/j.desal.2016.02.022  
10

11 Muftah, A.F., Alghoul, M.A., Fudholi, A., Abdul-Majeed, M.M., Sopian, K., 2014. Factors  
12 affecting basin type solar still productivity: A detailed review. *Renew. Sustain. Energy Rev.*  
13 doi:10.1016/j.rser.2013.12.052  
14

15 Murugavel, K.K., Sivakumar, S., Ahamed, J.R., Chockalingam, K.K.S.K., Srithar, K., 2010.  
16 Single basin double slope solar still with minimum basin depth and energy storing  
17 materials. *Appl. Energy* 87, 514–523. doi:10.1016/j.apenergy.2009.07.023  
18

19 Nakoa, K., Rahaoui, K., Date, A., Akbarzadeh, A., 2015. An experimental review on coupling of  
20 solar pond with membrane distillation. *Sol. Energy* 119, 319–331.  
21 doi:10.1016/j.solener.2015.06.010  
22

23 Nayi, K.H., Modi, K. V., 2018. Pyramid solar still: A comprehensive review. *Renew. Sustain.*  
24 *Energy Rev.* doi:10.1016/j.rser.2017.07.004  
25

26 Nixon, J.D., Dey, P.K., Davies, P.A., 2010. Which is the best solar thermal collection technology  
27 for electricity generation in north-west India? Evaluation of options using the analytical  
28 hierarchy process. *Energy* 35, 5230–5240. doi:10.1016/j.energy.2010.07.042  
29

30 Orfi, J., Loussif, N., Davies, P.A., 2016. Heat and mass transfer in membrane distillation used for  
31 desalination with slip flow. *Desalination* 381, 135–142. doi:10.1016/j.desal.2015.12.009  
32

33 Qasim, M., Darwish, N.A., Sarp, S., Hilal, N., 2015. Water desalination by forward (direct)  
34 osmosis phenomenon: A comprehensive review. *Desalination* 374, 47–69.  
35 doi:10.1016/j.desal.2015.07.016  
36

37 Rahbar, N., Esfahani, J.A., Asadi, A., 2016. An experimental investigation on productivity and  
38 performance of a new improved design portable asymmetrical solar still utilizing  
39 thermoelectric modules. *Energy Convers. Manag.* 118, 55–62.  
40 doi:10.1016/j.enconman.2016.03.052  
41

42 Rao Nulakani, N.V., Kamaraj, M., Subramanian, V., 2015. Coro-graphene and circumcoro-  
43 graphyne: novel two-dimensional materials with exciting electronic properties. *RSC Adv.* 5,  
44 78910–78916. doi:10.1039/C5RA14477A  
45

46 Rufuss, D.D.W., Iniyar, S., Suganthi, L., Davies, P.A., Akinaga, T., 2015. Analysis of solar still  
47 with nanoparticle incorporated phase change material for solar desalination application 8–  
48 12.  
49

50 Sakthivel, M., Shanmugasundaram, S., Alwarsamy, T., 2010. An experimental study on a  
51 regenerative solar still with energy storage medium - Jute cloth. *Desalination* 264, 24–31.  
52 doi:10.1016/j.desal.2010.06.074  
53

54 Sathyamurthy, R., El-Agouz, S.A., Nagarajan, P.K., Subramani, J., Arunkumar, T., Mageshbabu,  
55 D., Madhu, B., Bharathwaaj, R., Prakash, N., 2017. A Review of integrating solar collectors  
56 to solar still. *Renew. Sustain. Energy Rev.* doi:10.1016/j.rser.2016.11.223  
57  
58  
59  
60  
61  
62  
63  
64  
65



- 1 Shalaby, S.M., El-Bialy, E., El-Sebaili, A.A., 2016. An experimental investigation of a v-  
2 corrugated absorber single-basin solar still using PCM. *Desalination* 398, 247–255.  
3 doi:10.1016/j.desal.2016.07.042  
4
- 5 Sharshir, S.W., Peng, G., Yang, N., Eltawil, M.A., Ali, M.K.A., Kabeel, A.E., 2016. A hybrid  
6 desalination system using humidification-dehumidification and solar stills integrated with  
7 evacuated solar water heater. *Energy Convers. Manag.* 124, 287–296.  
8 doi:10.1016/j.enconman.2016.07.028  
9
- 10 Tanha Aminloei, R., Ghaderi, S.F., 2010. Generation planning in Iranian power plants with fuzzy  
11 hierarchical production planning. *Energy Convers. Manag.* 51, 1230–1241.  
12 doi:10.1016/j.enconman.2009.12.034  
13
- 14 Taylan, O., Kaya, D., Demirbas, A., 2016. An integrated multi attribute decision model for  
15 energy efficiency processes in petrochemical industry applying fuzzy set theory. *Energy  
16 Convers. Manag.* 117, 501–512. doi:10.1016/j.enconman.2016.03.048  
17
- 18 Tiwari, G.N., Sahota, L., 2017. Review on the energy and economic efficiencies of passive and  
19 active solar distillation systems. *Desalination* 401, 151–179.  
20 doi:10.1016/j.desal.2016.08.023  
21
- 22 Tsakiris, G., Spiliotis, M., Paritsis, S., Alexakis, D., 2009. Assessing the water potential of  
23 karstic saline springs by applying a fuzzy approach: The case of Almyros (Heraklion,  
24 Crete). *Desalination* 237, 54–64. doi:10.1016/j.desal.2007.12.022  
25
- 26 Velmurugan, V., Deenadayalan, C.K., Vinod, H., Srithar, K., 2008a. Desalination of effluent  
27 using fin type solar still. *Energy* 33, 1719–1727. doi:10.1016/j.energy.2008.07.001  
28
- 29 Velmurugan, V., Gopalakrishnan, M., Raghu, R., Srithar, K., 2008b. Single basin solar still with  
30 fin for enhancing productivity. *Energy Convers. Manag.* 49, 2602–2608.  
31 doi:10.1016/j.enconman.2008.05.010  
32
- 33 Velmurugan, V., Naveen Kumar, K.J., Noorul Haq, T., Srithar, K., 2009. Performance analysis  
34 in stepped solar still for effluent desalination. *Energy* 34, 1179–1186.  
35 doi:10.1016/j.energy.2009.04.029  
36
- 37 Velmurugan, V., Srithar, K., 2011. Performance analysis of solar stills based on various factors  
38 affecting the productivity - A review. *Renew. Sustain. Energy Rev.*  
39 doi:10.1016/j.rser.2010.10.012  
40
- 41 Velmurugan, V., Srithar, K., 2007. Solar stills integrated with a mini solar pond - analytical  
42 simulation and experimental validation. *Desalination* 216, 232–241.  
43 doi:10.1016/j.desal.2006.12.012  
44
- 45 Voropoulos, K., Mathioulakis, E., Belessiotis, V., 2001. Experimental investigation of a solar  
46 still coupled with solar collectors. *Desalination* 138, 103–110. doi:10.1016/S0011-  
47 9164(01)00251-X  
48
- 49 Wang, C.C., 2011. On the heat transfer correlation for membrane distillation. *Energy Convers.  
50 Manag.* 52, 1968–1973. doi:10.1016/j.enconman.2010.11.014  
51
- 52 Yadav, S., Sudhakar, K., 2015. Different domestic designs of solar stills: A review. *Renew.  
53 Sustain. Energy Rev.* 47, 718–731. doi:10.1016/j.rser.2015.03.064  
54
- 55 Yetilmezsoy, K., Abdul-Wahab, S.A., 2014. A composite desirability function-based modeling  
56 approach in predicting mass condensate flux of condenser in seawater greenhouse.  
57  
58  
59  
60  
61  
62  
63  
64  
65



1 Desalination 344, 171–180. doi:10.1016/j.desal.2014.03.029

2  
3 Yu, Z., Dexter, A., 2010. Hierarchical fuzzy control of low-energy building systems. Sol. Energy  
4 84, 538–548. doi:10.1016/j.solener.2009.03.014

5  
6 Zhang, Y., Peng, Y., Ji, S., Li, Z., Chen, P., 2015. Review of thermal efficiency and heat  
7 recycling in membrane distillation processes. Desalination. doi:10.1016/j.desal.2015.04.013

8  
9 Zilouchian, A., Jafar, M., 2001. Automation and process control of reverse osmosis plants using  
10 soft computing methodologies. Desalination 135, 51–59. doi:10.1016/S0011-  
11 9164(01)00138-2  
12  
13  
14  
15  
16  
17  
18  
19  
20  
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**Table 1**

Five point scale for various input and output criteria

a. Skilled labour requirement		b. Land area requirement	
Scale	Definition	Scale	Definition
1	More than 5 person required	1	More than three active components are coupled with still
2	At least 4 person required	2	Two components are coupled with still
3	At least 3 person required	3	One active component is coupled with still
4	At least 2 person required	4	Complexity in design and size
5	One person is enough	5	No active component is coupled with still
c. Economic impact		d. Commercial potential	
Scale	Definition	Scale	Definition
1	The annual maintenance cost of the system above 80 \$/m <sup>2</sup>	1	Research and development stage
2	The annual maintenance cost of the system between 60-80 \$/m <sup>2</sup>	2	Technology transfer stage
3	The annual maintenance cost of the system between 40-60 \$/m <sup>2</sup>	3	Patent acquirement stage
4	The annual maintenance cost of the system between 20-40 \$/m <sup>2</sup>	4	In the phase of dissemination
5	The annual maintenance cost of the system between than 0-20 \$/m <sup>2</sup>	5	In the phase of commercialization
e. Productivity		f. Technical complexity	
Scale	Definition	Scale	Definition
1	Average annual productivity ranges between 0-250 lit/m <sup>2</sup>	1	Solar still coupled with two or more component
2	Average annual productivity ranges between 250-500 lit/m <sup>2</sup>	2	Solar still coupled with any one component
3	Average annual productivity ranges between 500-750 lit/m <sup>2</sup>	3	Modifying the design of conventional still setup
4	Average annual productivity ranges between 750-1000 lit/m <sup>2</sup>	4	Small modification in the existing conventional still setup
5	Average annual productivity ranges above 1000 lit/m <sup>2</sup>	5	Conventional setup

**Table 2 Triangular fuzzy (TFN) scale and its inverse TFN scale**

Scale of importance	Triangular fuzzy scale	Triangular fuzzy inverse scale
Equally important	(1,1,1)	(1,1,1)
Moderately important	(1/2,1,3/2)	(2/3,1,2)
Moderately more important	(1,3/2,2)	(1/2,2/3,1)
Strongly important	(3/2,2,5/2)	(2/5,1/2,2/3)
Very strongly important	(2,5/2,3)	(1/3,2/5,1/2)
Absolutely extremely important	(5/2,3,7/2)	(2/7,1/3,2/5)

**Table 3 Demographic details of the experts**

**Table 3**

Demographic details of the experts

Type of experts	Years of experience		Specialization
	10 to 15 years	15 years and above	
Academicians	0	2	Renewable energy
Industrialists	0	3	Desalination
Researchers	2	3	Solar still

**Table 4 CR value for the input and output criteria**

**Table 4**

CR value for the input and output criteria

Experts	CR value for	
	Input criteria	Output criteria
Expert 1	0.056352	0.081938
Expert 2	0	0.07702
Expert 3	0.017789	0
Expert 4	0.05234	0.021225
Expert 5	0.056352	0.031959
Expert 6	0.056352	0.092605
Expert 7	0.032986	0.083818
Expert 8	0.009503	0.085752
Expert 9	0.061082	0.088472
Expert 10	0.020183	0.0923



**Table 5** Pairwise comparison

**Table 5**  
Pairwise comparison for Expert-1

	SL	FC	LA
SL	(1,1,1)	(3/2,2,5/2)	(1/2,2/3,1)
FC	(2/5,1/2,2/3)	(1,1,1)	(2/5,1/2,2/3)
LA	(1,3/2,2)	(3/2,2,5/2)	(1,1,1)

**Table 6** Comparing the values of fuzzy synthetic extent

**Table 6**  
Comparing the values of fuzzy synthetic extent

$V(S_1 \geq S_j)$	Value
$V(S_1 \geq S_2)$	1
$V(S_1 \geq S_3)$	0.759169
$V(S_2 \geq S_j)$	Value
$V(S_2 \geq S_1)$	0.187702
$V(S_2 \geq S_3)$	0
$V(S_3 \geq S_j)$	Value
$V(S_3 \geq S_1)$	1
$V(S_3 \geq S_2)$	1

**Table 7 Fuzzy AHP weights for Input criteria**

**Table 7**  
Fuzzy AHP weights for Input criteria

Experts	SL	FC	LA
Expert 1	0.43155		0.56845
Expert 2	0.932849		0.067151
Expert 3	0.391644	0.45041	0.157945
Expert 4	0.343264	0.449537	0.207199
Expert 5	0.43155	0.56845	
Expert 6		0.43155	0.56845
Expert 7	1		
Expert 8		0.529104	0.470896
Expert 9		0.568981	0.431019
Expert 10	0.379857		0.620143

**Table 8 Upper and lower bounds of weights input criteria**

**Table 8**  
Upper and lower bounds of weights input criteria

Input weight ratio	Lower bound	Upper bound
$u_1/u_2=SL/FC$	0.759169	0.869528
$u_1/u_3=SL/LA$	0.612532	13.89189
$u_2/u_3=FC/LA$	0.759169	2.81687

**Table 9 Fuzzy AHP weights for output criteria**

**Table 9**  
Fuzzy AHP weights for output criteria

Experts	EI	CP	P	TC	Total
Expert 1	0.175001			0.824999	1
Expert 2		0.237335		0.762665	1
Expert 3	0.30111	0.09667	0.30111	0.30111	1
Expert 4	0.247096	0.421012	0.246513	0.085379	1
Expert 5	0.104572	0.187767	0.20532	0.502341	1
Expert 6	0.140981	0.501199	0.35782		1
Expert 7	0.424853		0.074449	0.500698	1
Expert 8	0.346887	0.336262		0.316851	1
Expert 9	0.477976	0.269775	0.252249		1
Expert 10	0.044319	0.399463		0.556218	1

**Table 10** Upper and lower bounds of weights output criteria

**Table 10**  
Upper and lower bounds of weights output criteria

Output weight ratio	Lower bound	Upper bound
$u_1/u_2=EI/CP$	0.110947	3.11482
$u_1/u_3=EI/P$	0.394	5.706604
$u_1/u_4=EI/TS$	0.07968	2.89411
$u_2/u_3=CP/P$	0.321046	1.707865
$u_2/u_4=CP/TS$	0.311192	4.931093
$u_3/u_4=P/TS$	0.148691	2.887284



**Table 11**

Input/output criteria for 20 solar stills

Type of Solar still	References	SL	FC	LA	EI	CP	P	TC
Solar still with wick and fin	(Velmurugan et al., 2008b)	3	250	4	3	1	3	1
Transportable hemispherical solar still	(Ismail, 2009)	3	1916	4	1	1	5	3
Stepped solar still with wick and sponge	(Velmurugan et al., 2009)	3	360	4	2	1	5	1
Stepped solar still with sun tracking system	(Abdallah et al., 2008)	1	729.16	3	1	1	5	2
weir type solar still	(Sadineni et al., 2008)	3	288.95	4	3	1	5	3
solar still with sponge and pond	(Velmurugan and Srithar, 2007)	3	350	3	2	1	4	1
soar still with shallow solar pond	(El-Sebaai et al., 2008)	2	320	3	2	1	5	2
solar still with condenser	(El-Bahi and Inan, 1999)	3	350	3	2	1	5	2
single slope solar still	(Ali Samee et al., 2007)	5	345.45	5	4	1	5	5
single slope solar still with PVT	(Kumar and Tiwari, 2009)	1	250	2	3	1	2	5
solar still with collector	(Badran and Al-Tahaine, 2005)	3	480	3	1	1	4	2
solar still with concentrator	(Abdel-Rehim and Lasheen, 2007)	3	300	3	3	1	4	2
solar still with sun tracking	(Abdallah and Badran, 2008)	3	300	3	3	1	1	2
Pyramid shape solar still	(Fath et al., 2003)	2	173.61	4	4	1	5	3
Pyramid shape solar still with collector	(Badran et al., 2005)	1	488.06	4	1	1	4	1
solar still with fin	(Velmurugan et al., 2008a)	3	200	4	4	1	3	4
Solar still with PCM	(Rufuss et al., 2015)	4	178.9	4	4	1	5	4
Solar still with Nano PCM (Titanium di oxide)	(Rufuss et al., 2015)	3	179.34	4	4	1	5	4
Solar still with Nano PCM (Graphene oxide)	(Rufuss et al., 2015)	3	618.9	4	1	1	5	4
Solar still with Nano PCM (Copper oxide)	(Rufuss et al., 2015)	3	179.26	4	4	1	5	4
Average		2.75	412.88	3.6	2.6	1	4.25	2.75

**Table 12**

Weight distribution of AR-CCR (with weight restriction)

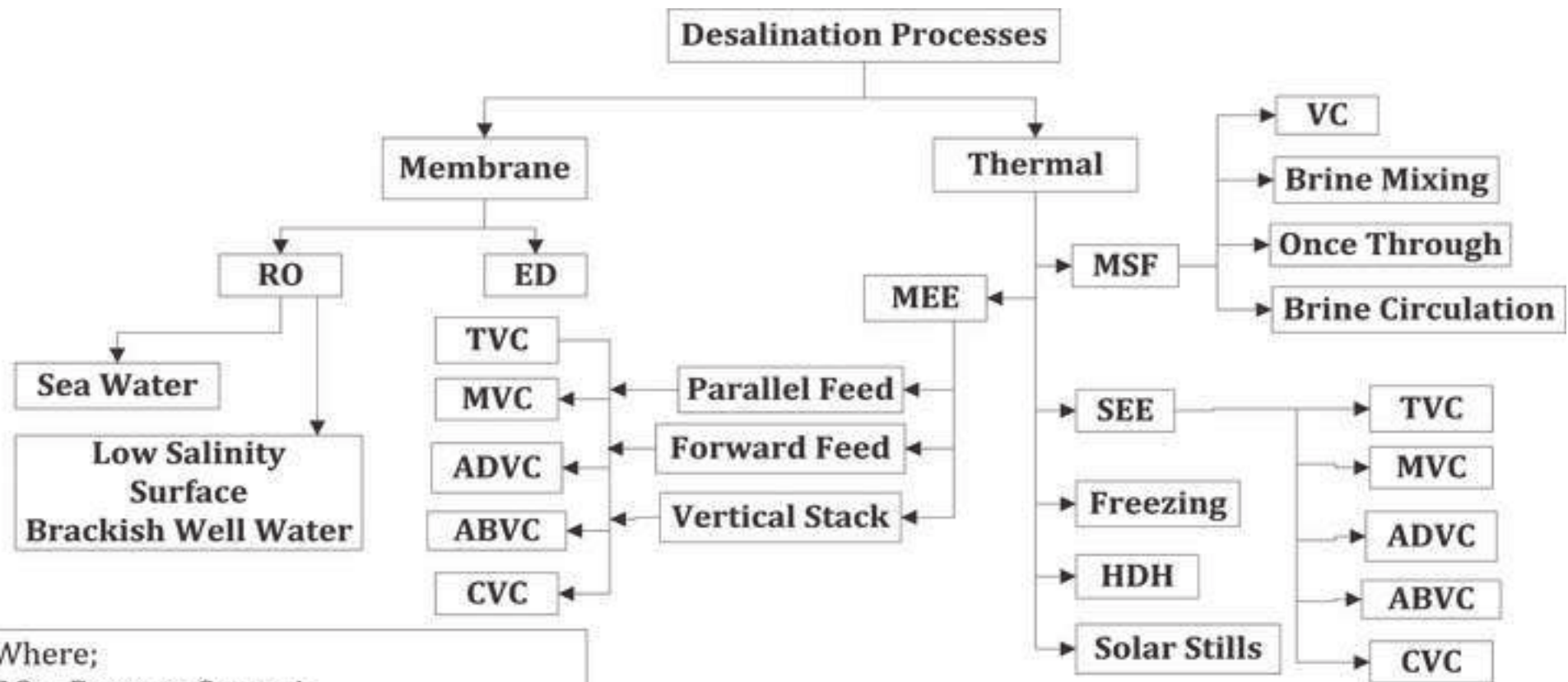
Type of Solar still	AR-CCR (with weight restriction)						
	Input weights			Output weights			
	SL	FC	LA	EI	CP	P	TC
Solar still with wick and fin	0.0076	0.0100	0.0035	0.0027	0.0046	0.0027	0.0009
Transportable hemispherical solar still	0.0049	0.0056	0.0074	0.0019	0.0016	0.0049	0.0017
Stepped solar still with wick and sponge	0.0063	0.0083	0.0043	0.0020	0.0017	0.0052	0.0018
Stepped solar still with sun tracking system	0.0052	0.0060	0.0079	0.0021	0.0017	0.0053	0.0018
weir type solar still	0.0052	0.0069	0.0035	0.0017	0.0014	0.0043	0.0015
solar still with sponge and pond	0.0051	0.0068	0.0084	0.0013	0.0055	0.0032	0.0011
soar still with shallow solar pond	0.0044	0.0058	0.0072	0.0019	0.0016	0.0049	0.0017
solar still with condenser	0.0044	0.0058	0.0072	0.0019	0.0016	0.0049	0.0017
single slope solar still	0.0033	0.0044	0.0054	0.0014	0.0012	0.0037	0.0013
single slope solar still with PVT	0.0048	0.0064	0.0079	0.0003	0.0013	0.0008	0.0043
solar still with collector	0.0052	0.0068	0.0084	0.0013	0.0056	0.0033	0.0011
solar still with concentrator	0.0046	0.0061	0.0075	0.0020	0.0016	0.0051	0.0018
solar still with sun tracking	0.0057	0.0075	0.0093	0.0030	0.0051	0.0030	0.0010
Pyramid shape solar still	0.0056	0.0073	0.0026	0.0025	0.0023	0.0025	0.0009
Pyramid shape solar still with collector	0.0087	0.0100	0.0035	0.0013	0.0058	0.0034	0.0012
solar still with fin	0.0060	0.0079	0.0028	0.0035	0.0011	0.0025	0.0012
Solar still with PCM	0.0047	0.0062	0.0032	0.0015	0.0012	0.0038	0.0013
Solar still with Nano PCM (Titanium di oxide)	0.0047	0.0062	0.0032	0.0015	0.0012	0.0038	0.0013
Solar still with Nano PCM (Graphene oxide)	0.0043	0.0053	0.0070	0.0018	0.0015	0.0046	0.0016
Solar still with Nano PCM (Copper oxide)	0.0047	0.0062	0.0032	0.0015	0.0012	0.0038	0.0013
No. of Zeros in weights	0	0	0	0	0	0	0

**Table 13**

Efficiency and rank of solar stills

Type of Solar still	Efficiency decomposition								Rank
	Efficiency	SL	FC	LA	EI	CP	P	TC	
Solar still with wick and fin	0.5504	0.8253	0.6034	0.3883	0.3129	0.4621	0.1910	0.0341	12
Transportable hemispherical solar still	0.2533	0.5310	2.5976	0.8192	0.0748	0.1584	0.5804	0.1864	20
Stepped solar still with wick and sponge	0.5277	0.6909	0.7273	0.4767	0.1573	0.1666	0.6107	0.0654	15
Stepped solar still with sun tracking system	0.5269	0.1887	1.0540	0.6551	0.0797	0.1689	0.6189	0.1325	16
weir type solar still	0.6905	0.5712	0.4827	0.3942	0.1951	0.1378	0.5049	0.1622	8
solar still with sponge and pond	0.5468	0.5591	0.5723	0.6973	0.0985	0.5549	0.3058	0.0409	13
soar still with shallow solar pond	0.7279	0.3214	0.4512	0.6012	0.1477	0.1564	0.5732	0.1227	7
solar still with condenser	0.6342	0.4821	0.4935	0.6012	0.1477	0.1564	0.5732	0.1227	10
single slope solar still	0.5809	0.6034	0.3657	0.7524	0.2218	0.1175	0.4304	0.2304	11
single slope solar still with PVT	1.0000	0.1758	0.3856	0.4385	0.0399	0.1349	0.0372	0.7881	1
solar still with collector	0.4858	0.5638	0.7914	0.7031	0.0496	0.5595	0.3083	0.0825	19
solar still with concentrator	0.6368	0.5026	0.4410	0.6268	0.2309	0.1631	0.4781	0.1279	9
solar still with sun tracking	0.5129	0.6240	0.5474	0.7781	0.3451	0.5096	0.0702	0.0752	17
Pyramid shape solar still	1.0000	0.4053	0.3087	0.2860	0.3855	0.2260	0.2941	0.0944	2
Pyramid shape solar still with collector	0.5304	0.3157	1.1804	0.3891	0.0518	0.5836	0.3216	0.0430	14
solar still with fin	0.7437	0.6542	0.3826	0.3078	0.5344	0.1115	0.1795	0.1746	6
Solar still with PCM	0.7693	0.6806	0.2671	0.3522	0.2325	0.1231	0.4512	0.1932	5
Solar still with Nano-PCM (paraffin + TiO <sub>2</sub> )	0.8846	0.5105	0.2677	0.3522	0.2325	0.1231	0.4512	0.1932	4
Solar still with Nano-PCM (paraffin + GO)	0.4870	0.4704	0.8010	0.7821	0.0704	0.1491	0.5465	0.2340	18
Solar still with Nano-PCM (paraffin + CO)	0.8847	0.5105	0.2676	0.3522	0.2325	0.1231	0.4512	0.1932	3

Fig. 1. Detailed tabulation showing classification of desalination.  
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Where;  
 RO = Reverse Osmosis  
 ED = Electro Dialysis  
 MEE = Multiple Effect Evaporation  
 SEE = Single Effect Evaporation  
 MSF = Multistage Flash  
 VC = Vapor Compression  
 TVC = Thermal Vapor Compression  
 MVC = Mechanical Vapor Compression  
 ADVC = Adsorption Vapor Compression  
 ABVC = Absorption Vapor Compression  
 CVC = Chemical Vapor Compression  
 HDH = Humidification Dehumidification

Fig. 2. Various types of solar stills (Tiwar and Sanjota, 2017)  
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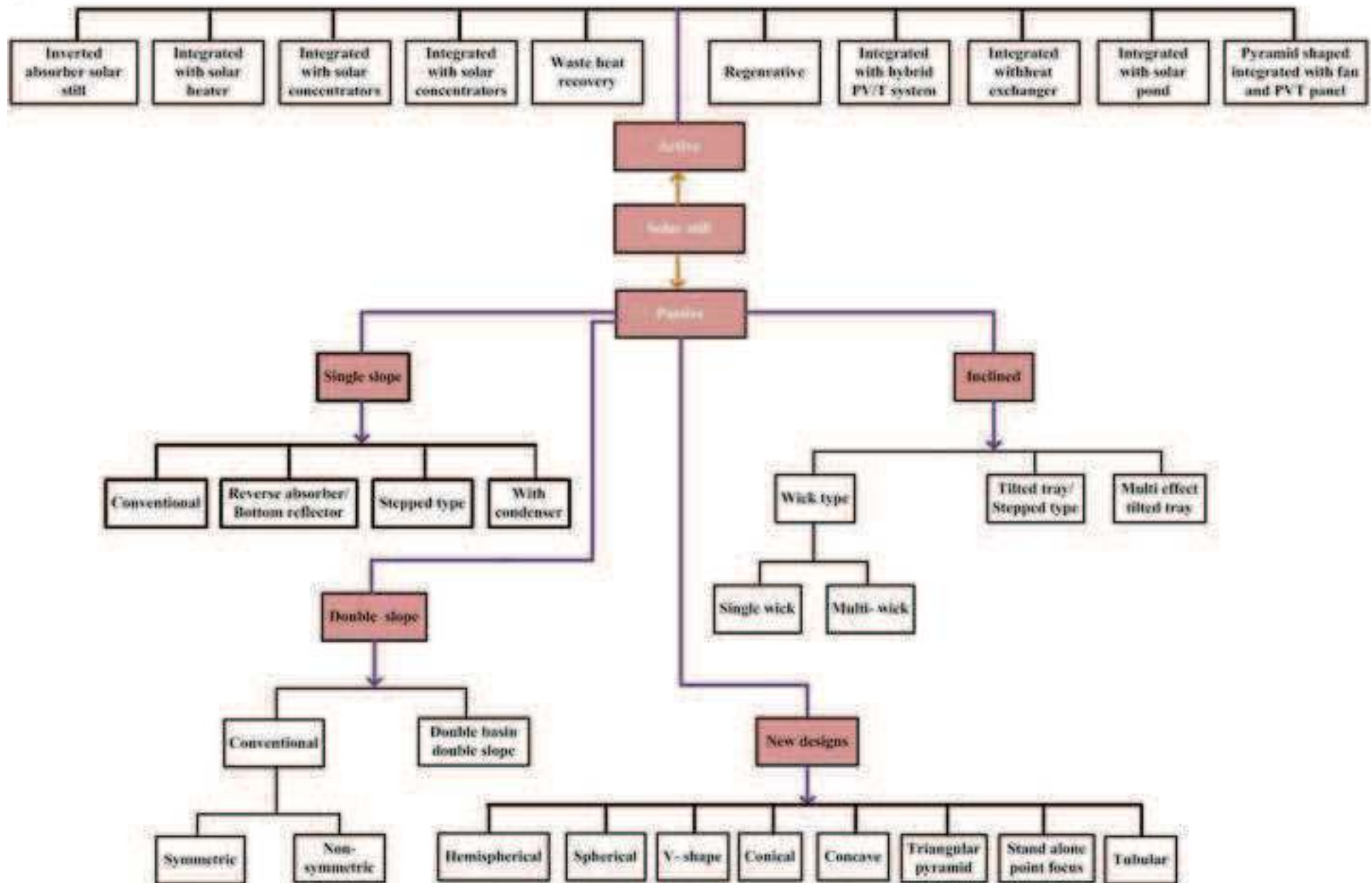


Fig. 3. Various climate, design and operational parameters inf..  
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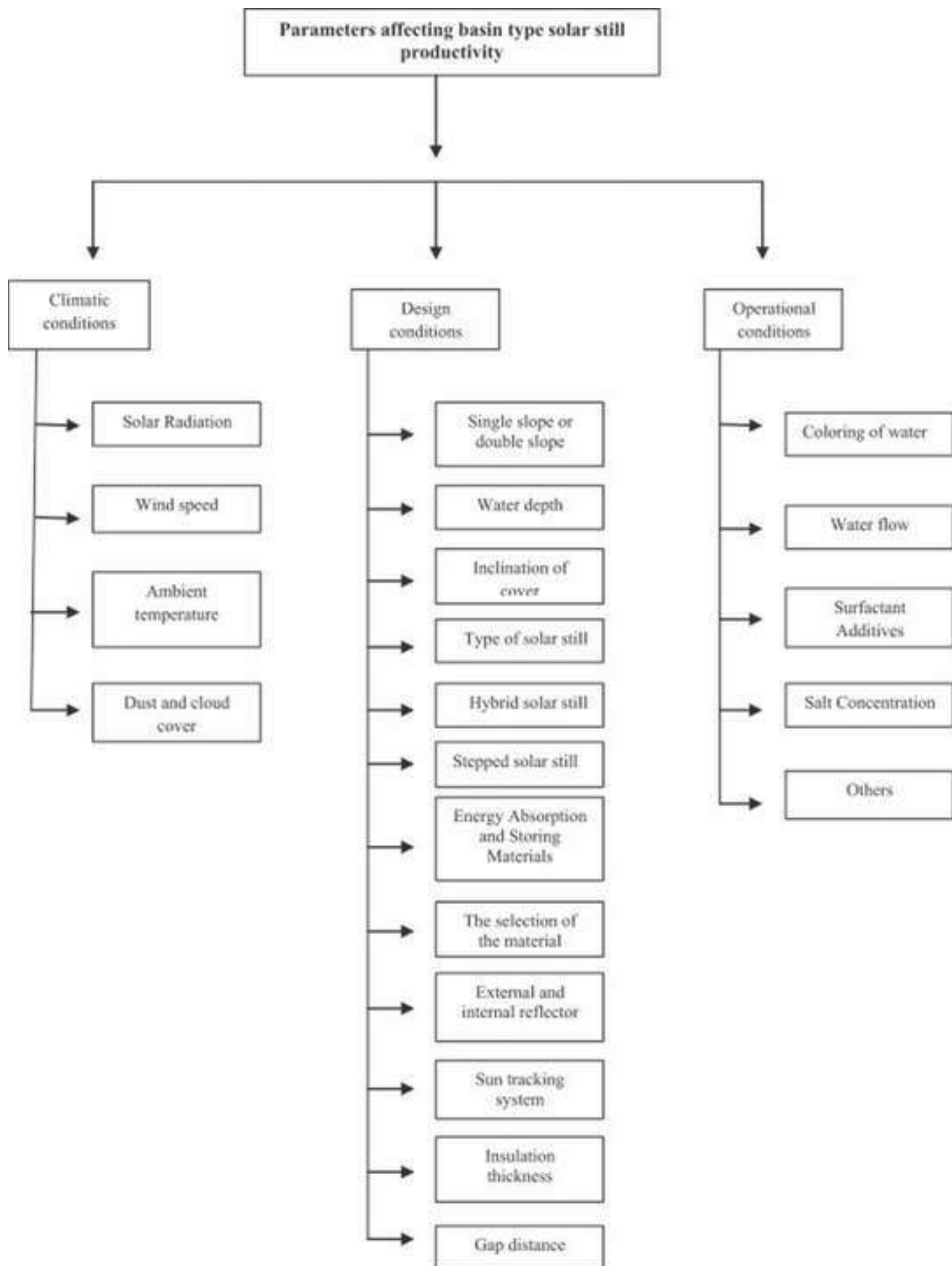




Fig. 4. Setup of simple single slope solar still (Ali Samee et al., 2015).  
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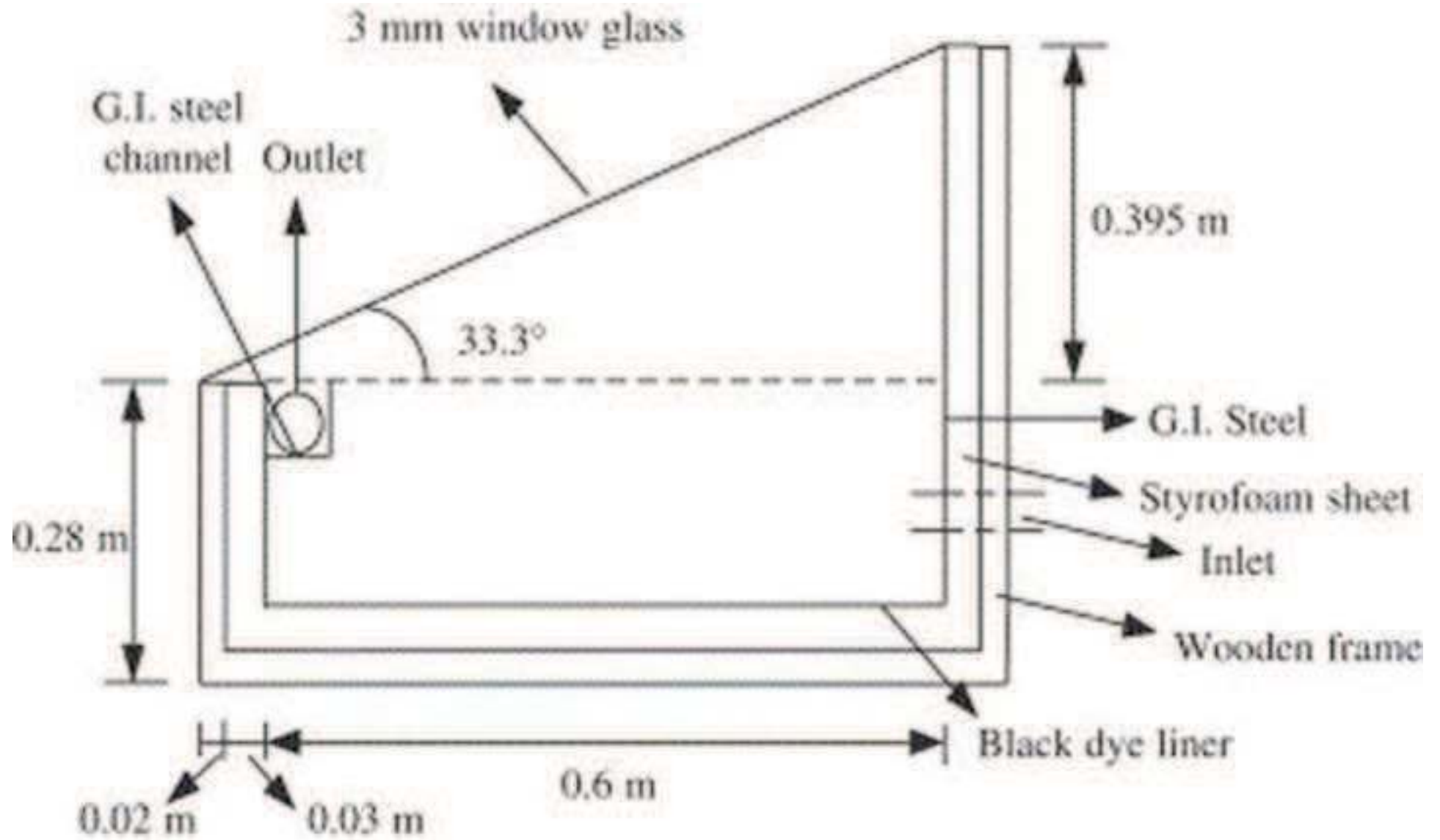
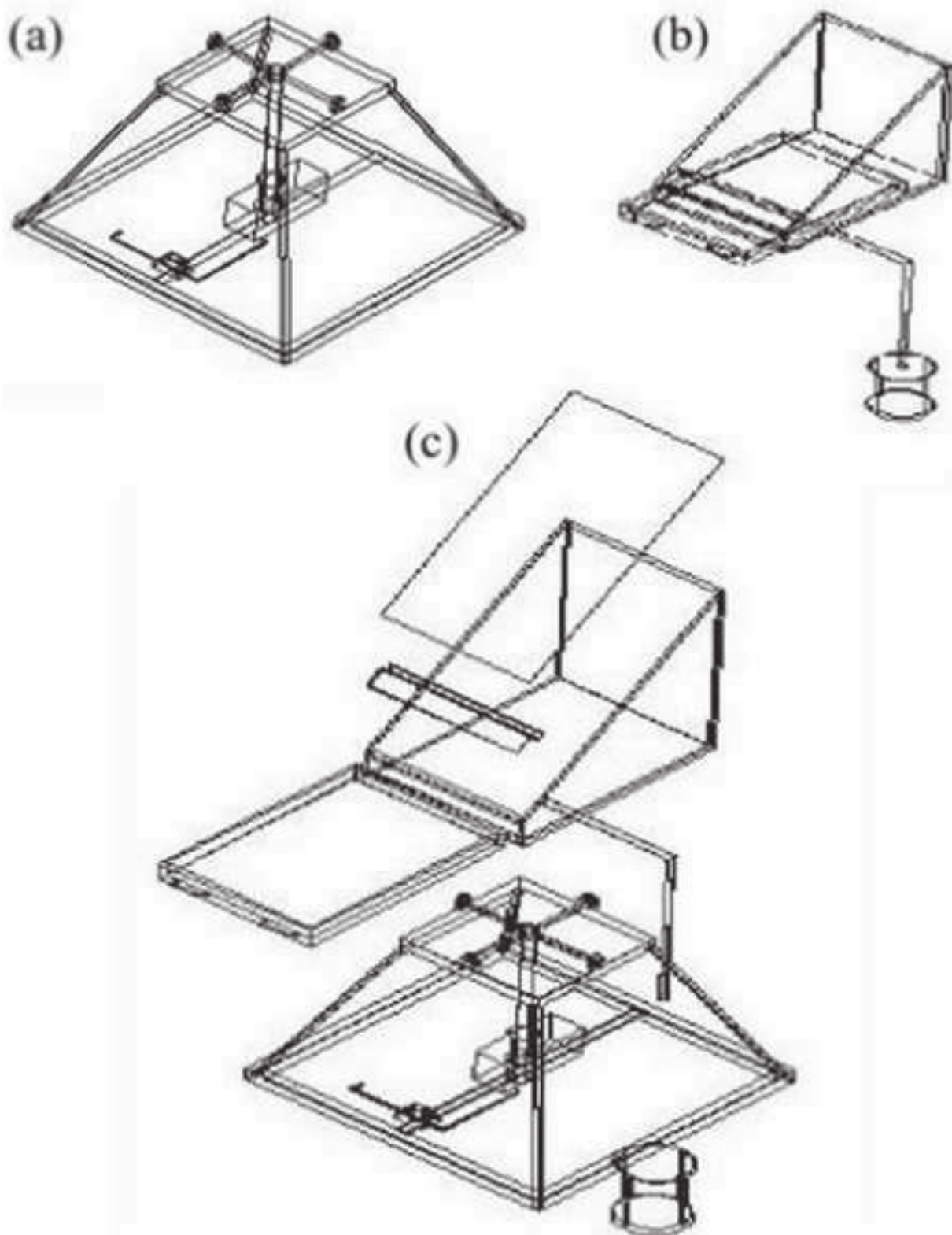




Fig. 5. Schematic of solar still with sun tracking system (Abd..  
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Three-dimensional view of the sun tracking distiller. (a) base, motor and bearing. (b) Distiller. (c) All involved parts of the distiller and tracking system.

Fig. 6. Solar still integrated with photo-voltaic thermal (PVT).  
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Fig. 7: Solar still integrated with flat-plate collector (Baur...  
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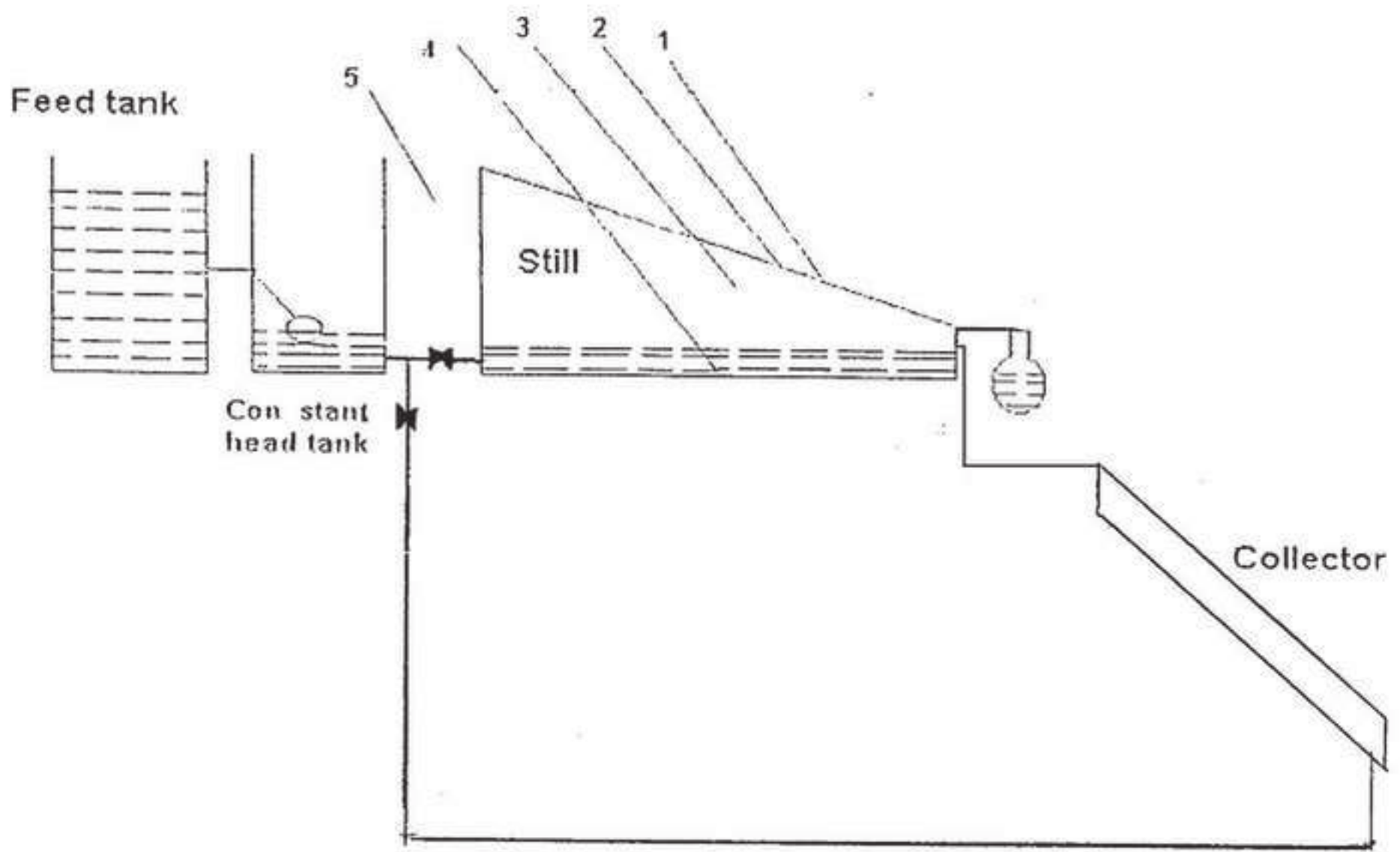




Fig. 6. Schematic of solar still integrated with concentrators.  
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Fig. 9. Schematic setup of solar still integrated with IM (ve...  
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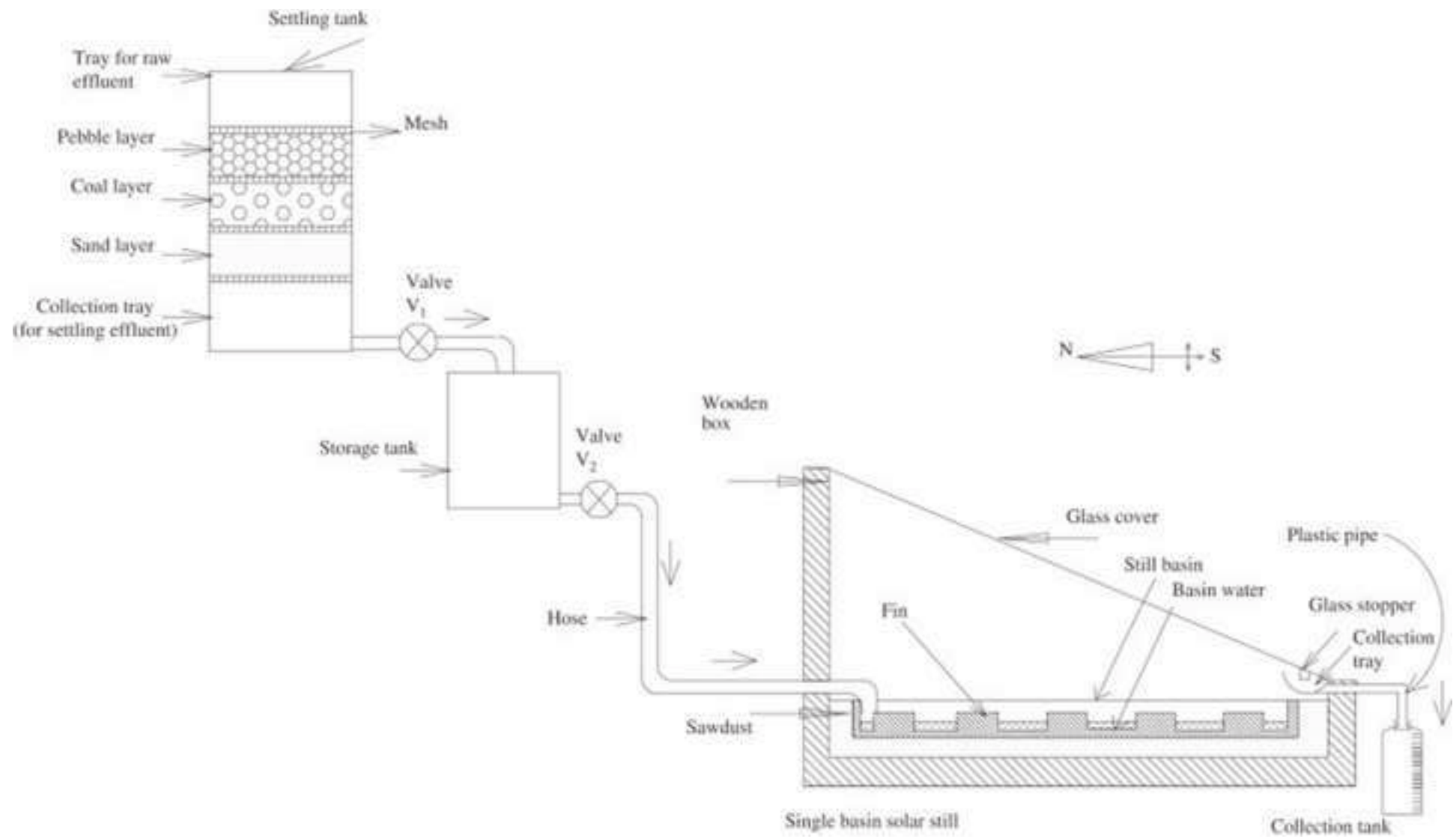


Fig. 10. Pictorial representation of hemispherical solar still.  
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Fig. 11. Schematic configuration of pyramid type solar still.  
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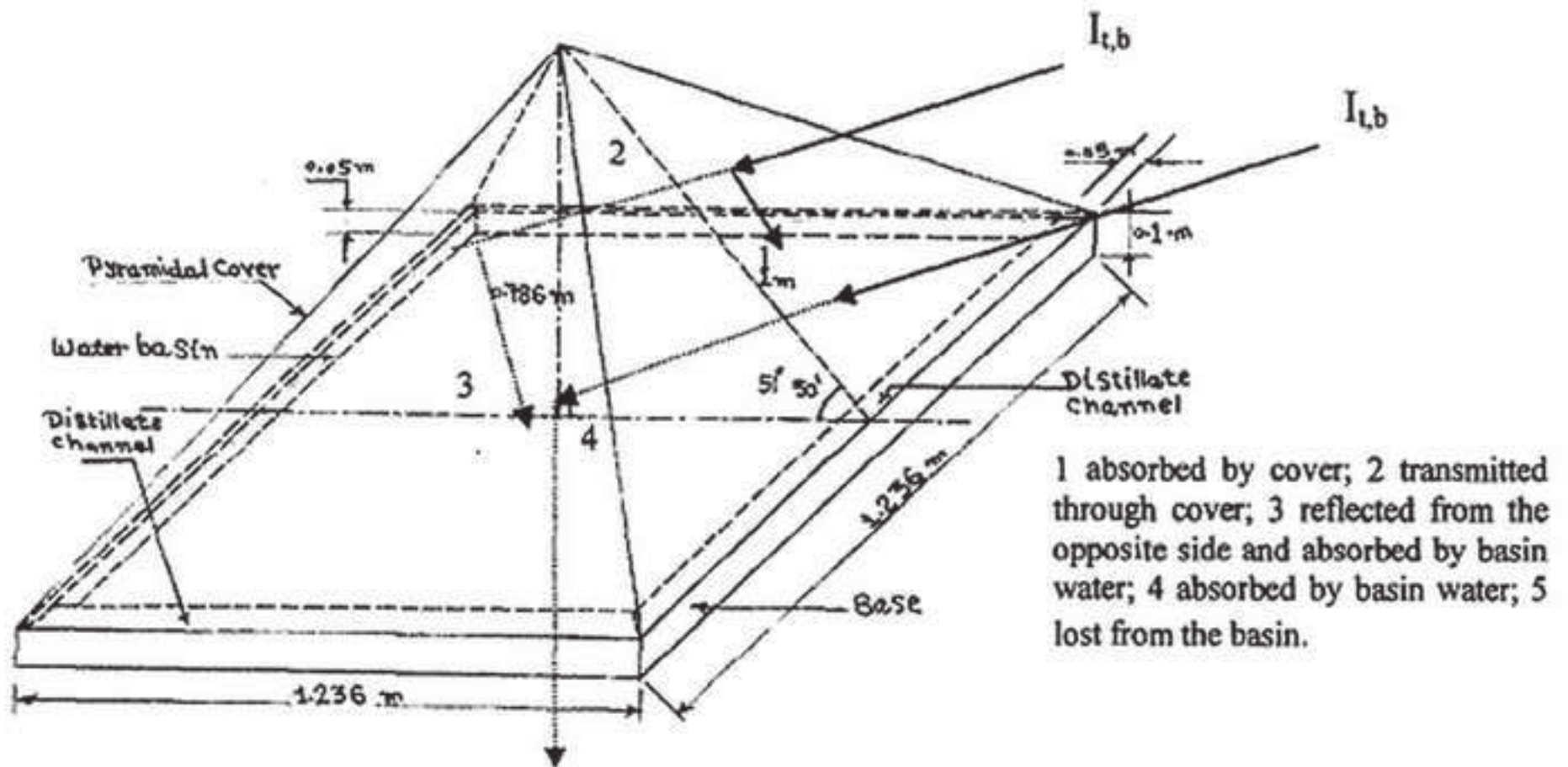




Fig. 12. Schematic of solar still with sponge (Velmurugan et al.  
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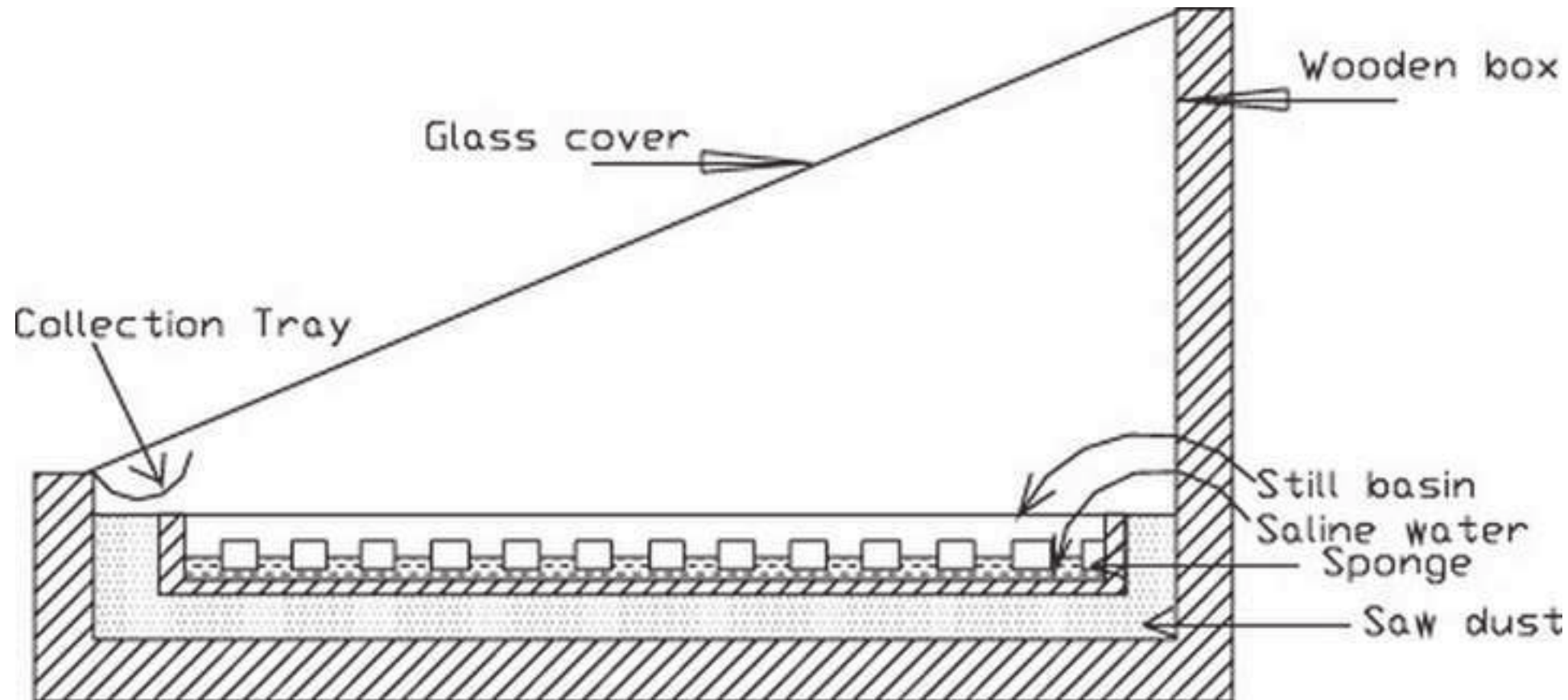


Fig. 15. Solar still with phase change material (PCM) (Shalaby..  
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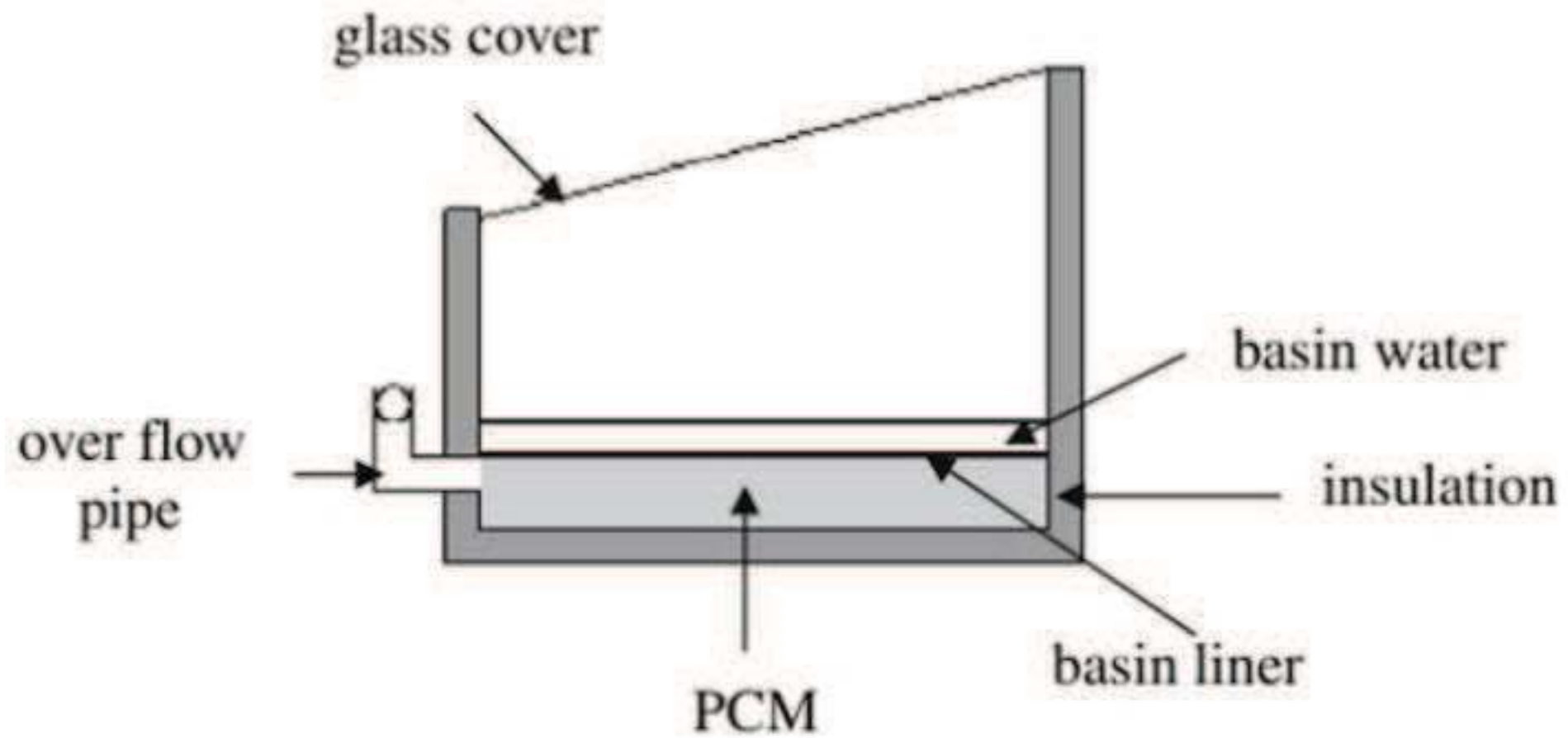


Fig. 14. Overall methodology of integrated fuzzy AHP-DEA  
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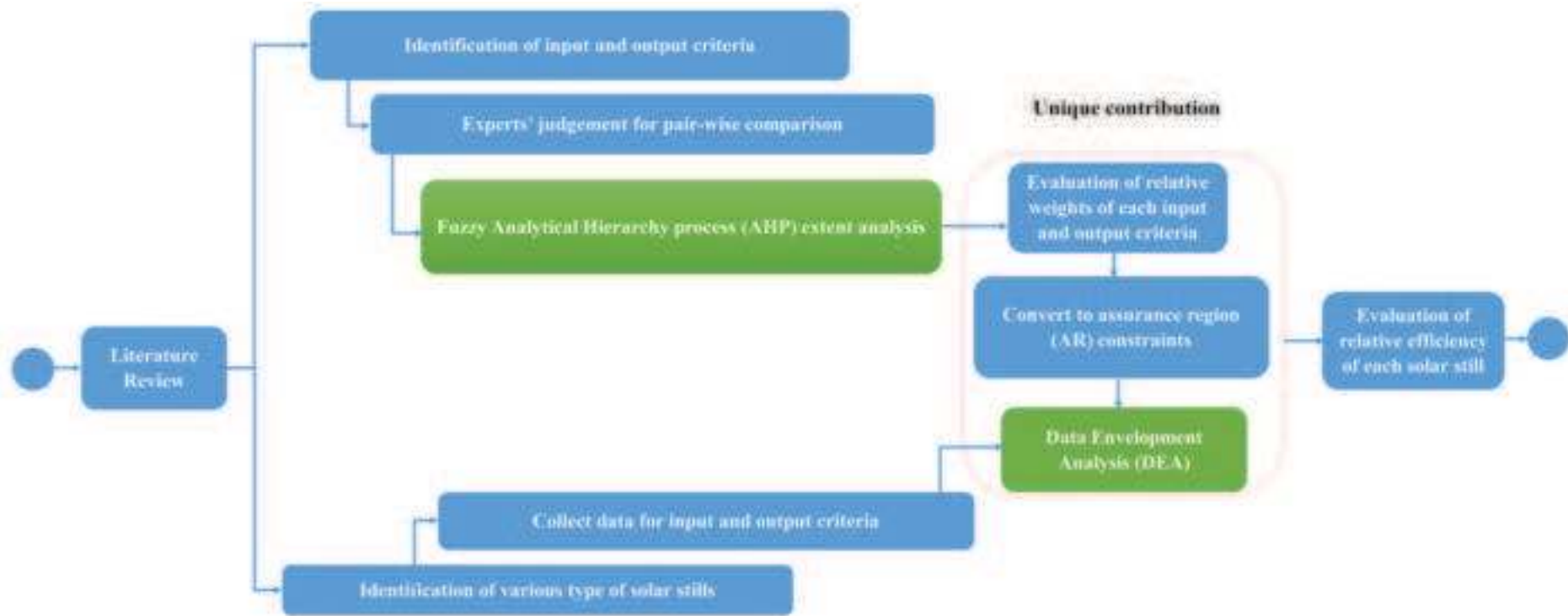


Fig. 15. Hierarchical structure of various input and output c...  
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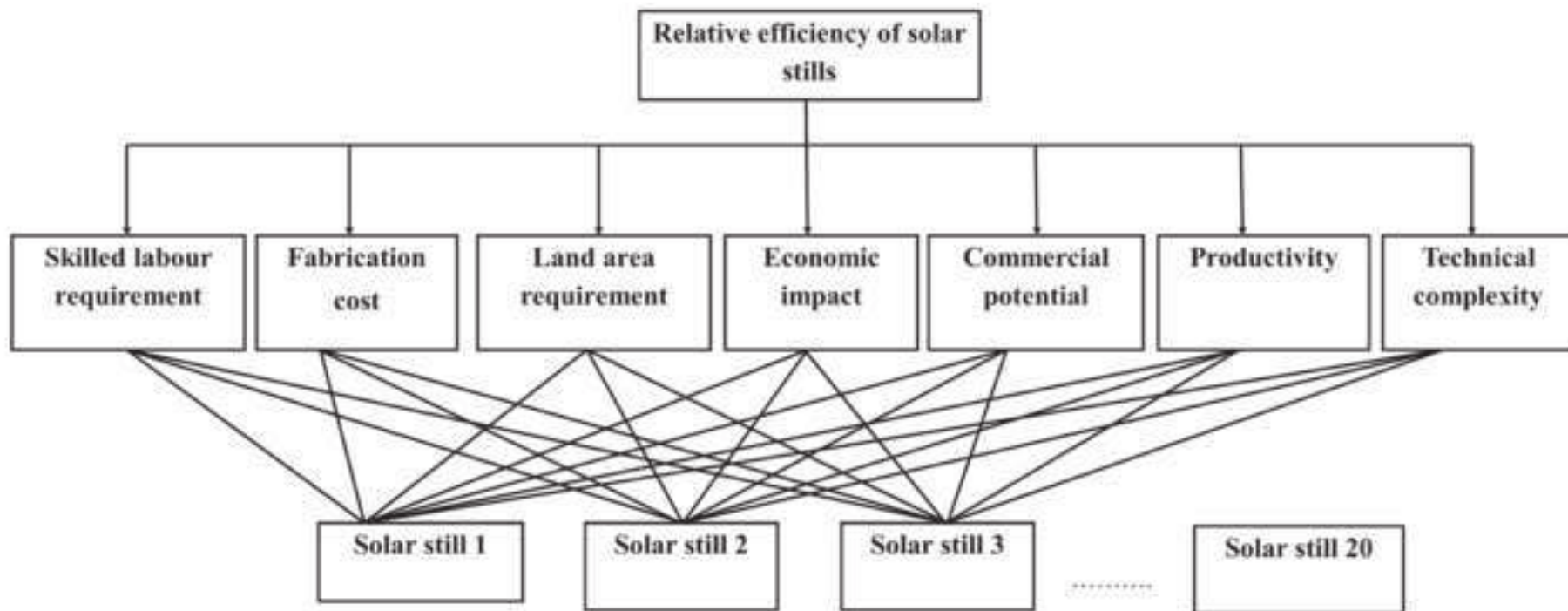


Fig. 16. Input/output criteria for the twenty solar stills  
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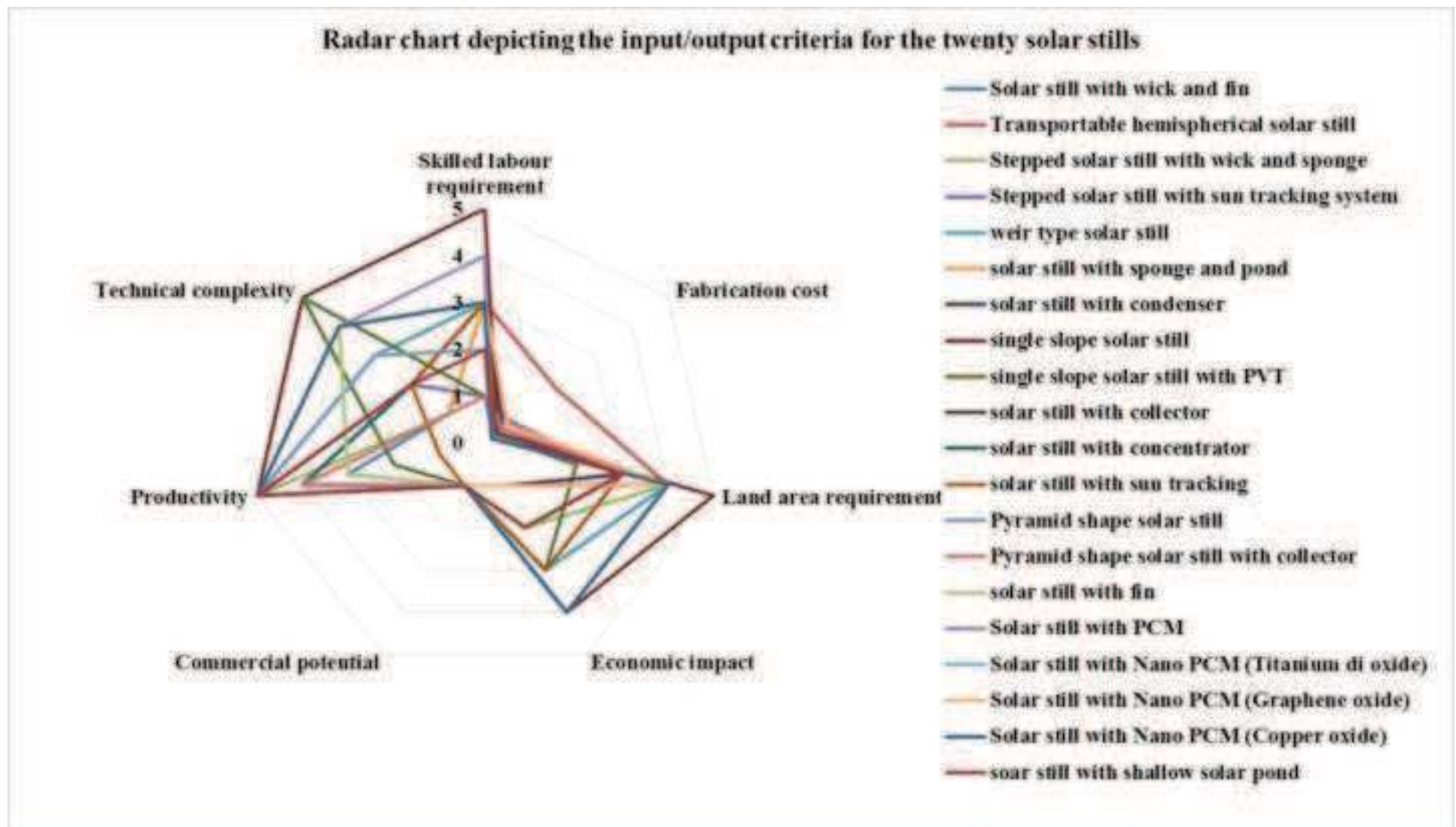




Fig. 17: Efficiency decomposition of twenty solar stills  
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