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A COMPARATIVE STUDY OF THERMAL RADIATION EFFECTS ON MHD FLOW OF NANOFLUIDS AND HEAT TRANSFER OVER A STRETCHING SHEET

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ABSTRACT

In this work, the steady natural convective boundary layer flow of nanofluid and heat transfer over a stretching sheet in the presence of a uniform transverse magnetic field is investigated. We consider two different base fluids and three different nanoparticles were examined as nanofluid. A new model was used in the simulation of nanofluid. Similarity transformations are used to obtain a system of nonlinear ordinary differential equations. The resulting equations are solved numerically by shooting method with Runge-Kutta fourth order scheme (MATLAB package). The effects of various parameters describing the transport in the presence of thermal radiation, buoyancy parameter, magnetic parameter and heat source/sink and nanoparticle volume concentration on the nanofluid velocity, temperature, the heat transfer coefficient and skin-friction coefficient are studied through graphs and table. Furthermore, comparisons with published results are in very good agreement.

Keywords: *MHD*, *nanofluids*, *free convection*, *thermal radiation*, *heat source/sink*, *stretching sheet*.

1. INTRODUCTION

Nanomaterials are being applied in more and more fields with potential applications in the areas of material sciences, electronics, and medicine. Among the nanotechnologies, nanofluid has received great attention in recent years because of its unique properties. Nanofluid is characterized as a base fluid with suspended solid nanoparticles of tiny size (1-100 nm) and nanofluid exhibits higher thermal conductivity and convective heat transfer coefficient compared to the traditional fluids such as oil, water, and ethylene glycol. As indicated by Choi (1995), the thermal conductivity of the conventional heat transfer fluid improved around two times when included with small nanoparticles even if the fraction is less than 1% of the volume. Because of enhanced heat transfer characteristics, nanofluids find numerous applications in engineering processes, particularly in the cooling technologies.

Eastman et al. (1997) suggested that an enlargement in thermal conductivity of around 60% can be accomplished for a nanofluid including water and 5% vol. of CuO nanoparticles. This means that the expansion in the surface region owing to the suspension of nanoparticles. Similarly, it was absolutely spoken to that a nanofluid, as well as Cu nanometer-sized particles scattered in ethylene glycol, has an abundant higher effective thermal physical phenomenon than either for real oil or ethylene glycol having a similar volume fraction of scattered base metal nanoparticles. Eastman et al. (2000) displayed that an improvement in the thermal conductivity relies on the shape, estimate and thermal attributes of nanoparticles. Mechanisms of heat flow in suspensions of nano-sized particles studied by Keblinski et al. (2002). Das et al. (2003) examined a two to a four fold rise in thermal conductivity development for nanofluid containing TiO₂- water or Al₂O₃ - water nanoparticles over a small temperature vary from 21°-51°C. To study the effects of the concentration and size variation of the nanoparticles, the concentration and size are varied from 0% - 5% and 25-100 nm respectively over the

Reynolds number range of 250 -1500 for Au -water nanofluid. Buongiorno (2005) analyzed the flow characteristics of viscous, with incompressible fluids with suspended nano-sized solid particles high significant due to the application of such fluids in heat transfer devices. Xie et al. (2010) have examined magnesium oxide nanofluids; higher thermal conductivity and lower viscosity with ethylene glycol-based nanofluids containing oxide nanoparticles. Electro-oxidation of ethylene glycol has attracted considerable interest for mobile, stationary and portable applications owing to its high theoretical energy capacity, high boiling point and high efficiency of electric power conversion has been analyzed in a review article by Yue et al. (2012). The existing literature was shown that ensures the enlargement of nanoparticles in the base fluid may accomplish an essentially reducing in the heat transfer; for comprehensive review, see (Kakac and Pramuanjaroenkij (2009), Sheikholeslami et al. (2014), Nayak et al. (2017), and Nayak et al. (2017)).

The study of boundary layer flow passing a stretching sheet become an important and interesting challenge for research studies due to its practical utility in industry and engineering. It has potential applications in many areas such as cooling of metallic sheet, stretching of the plastic film, industrialized polymer sheet, metal spinning, crystal growing, electronic chips, filaments and wires, glass blowing, artificial fibers, paper production, metallurgical processes, rubber sheets, and polymer extrusion. The quality yet ultimate production formations among these techniques are dependent over the concerning cooling and stretching. The studies on boundary layer flow of nanofluid over a stretching sheet have attracted the attention of a large of a number of researchers. The boundary layer flow and heat transfer in a viscous fluid contacting metallic nanoparticles over a stretching sheet in the presence of thermal radiation have investigated by Hamad and Ferdows (2012). Effects of chemical reaction on the MHD flow of a visco-elastic fluid through porous medium have been presented by Nayak et al. (2014).

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Sheikholeslami et al. (2014) have examined the effect of thermal radiation on a magnetic field effect on CuO-water nanofluid and heat transfer. Tukyilmazoglu (2014) have described the exact analytical solution for heat and mass transfer of magnetohydrodynamic slip flow in nanofluids. Unsteady radiative MHD free convective flow and mass transfer of a viscoelastic fluid past an inclined porous plate analyzed by Nayak et al. (2015). Rushi Kumar et al. (2015) investigated on unsteady free convection flow in the presence of magnetic field fixed relative to the fluid or the plate by using Laplace transformation technique. Gireesha et al. (2016) have analyzed the development of steady boundary layer flow of a nanofluid over a stretching sheet in the presence of radiation effects. It is found that the induced magnetic field and temperature distributions are enhanced with the strengthening of hydromagnetic field. Recently Mabood et al. (2016) have studied the MHD stagnation point of water-based nanofluid in which the heat and mass transfer includes the effects of the volume fraction of nanoparticles, radiation, viscous dissipation and chemical reaction.

The investigation of magnetohydrodynamics with heat transfer within the effect of thermal radiation has gained a great consideration due to its diversified applications involved in designs of the fins, steel rolling, manufacturing engineering and various propulsion devices for aircraft, in cooling of reactors in geophysics and astrophysicist. It is associated with the study of solar structures, radio spread by the ionosphere etc. It is because of the interaction of electromagnetic fields and electrically conducting fluids. Conducting fluid moves through the magnetic field, an electric field and therefore a current may be started, and in this manner, the current interacts with the magnetic field to make a body force on the fluid. Such interactions occur both in nature and in new man-made devices. In the research center, numerous devices have been made based on the principle of the magnetohydrodynamic interaction directly, such as impetus units and power generators or which include liquid electromagnetic field interactions; for example, electrical discharges, MHD pumps, electron beam dynamics, MHD bearing, traveling wave tubes, etc. Recently, many researchers have examined the influences of electrically conducting nanofluids, such as water mixed with a petite acid and another ingredient in the presence of a magnetic field on the flow and heat transfer of an incompressible, viscous, electrically conducting fluid past a moving surface or a stretching plate in the motionless fluid. Effects of thermal radiation on the steady laminar MHD boundary layer flow of a nanofluid over an exponentially stretching sheet have been presented by Loganathan and Vimala (2013). Khan (2013) studied the effects of magnetic field on the radiative flow of a nanofluid past a stretching sheet. Sheikholeslami and Ganji (2014) have studied the effects of thermal radiation on unsteady nanofluid flow and heat transfer in presence of magnetic field. Hayat et al. (2014) analyzed the magnetohydrodynamic boundary layer flow of nanofluid. Navak (2015) examined the chemical reaction effect on MHD viscoelastic fluid over a stretching sheet through a porous medium. Satya Narayana and Venkateswarlu (2016) examined heat transfer analysis of water-based nanofluid over a stretching sheet using different types of nanoparticles such as Cu, Ag, TiO₂, and Al₂O₃. There have been published several recent numerical studies on the modeling of heat transfer and nanofluids (Khan and Pop (2010), Makinde and Aziz (2011), Nadeem et al. (2014), A Daniel (2015), and Pourmehran et al. (2016)).

The objective of the present study is to investigate the MHD natural convective boundary layer flow of nanofluid and heat transfer over a stretching sheet in the presence of heat source parameter. Three types of water; ethylene glycol 50% based nanofluids containing nanoparticles of copper (Cu), copper oxide (CuO) and magnesium oxide (MgO) have been considering in the present work. This model has considered a new micro-convection model, namely Patel model for more heat transfer capability of nanofluids. A new model was used in the simulation of nanofluid. The governing nonlinear partial differential equations are transformed into a system of nonlinear ordinary differential equations using similarity transformation and then tackled numerically by shooting method with Runge-Kutta fourth order scheme (MATLAB package). The dependency of velocity, temperature, and nanoparticles volume

fraction profiles as well as the skin-friction coefficient and local Nusselt number on these parameters has been discussed.

2. MATHEMATICAL ANALYSES

The physical model and geometry of the problem are shown in Fig. 1. We consider the two-dimensional steady magnetohydrodynamic boundary layer flow of an incompressible nanofluid over a stretching sheet in the presence of a uniform transverse magnetic field. It is assumed that the magnetic Reynolds number insignificant in the free convection flow, hence the induced magnetic field is ignored. Electric field and dissipation effects are neglected. The x-axis is taken along the stretching surface in the upward direction, y - axis is normal to it. A

uniform magnetic field of strength B_0 is applied normal to the fluid flow

direction. The nanofluids consist of two different types of base fluids; water, ethylene glycol 50% with three different types of nanoparticles; namely Cu(copper), CuO(copper oxide), and MgO (magnesium oxide). It is assumed that the base fluid and the nanoparticles are in thermal equilibrium and no slip occurs between them. Under the above assumptions, the boundary layer equations governing for this problem can be written as follows [Rashidi et al. (2014)]

Table 1 Thermophysical properties of water and nanoparticles at T=300K ([Hakan et al. (2008), Sekulić et al. (2005)]).

Physical	Pure	Ethylene	Ĉu	CuO	MgO
properties	water	glycol 50%			
ho (kg/m ³)	997.1	1052.1	8933	6320	3580
c_p (J/kg.K)	4179	3301.7	385	531.8	960
k (W/m.K)	0.613	0.432	401	76.5	48.4
$\beta \times 10^5 K^{-1}$	21	57	1.67	1.80	1.26
μ_f (Ns/m ²)	0.001 003	0.0031871	-	-	-
d_f or d_s (nm)	0.24	0.32	30-60	30-60	30-60



Fig. 1 Physical model

The flow is governed by the following equations: $\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$

$$\rho_{nf}\left(u\frac{\partial u}{\partial x}+v\frac{\partial u}{\partial y}\right)=\mu_{nf}\frac{\partial^2 u}{\partial y^2}+g(\rho\beta)_{nf}(T-T_{\infty})-\sigma B_0^2 u$$
(2)

(1)

$$\left(\rho c_{p}\right)_{nf}\left(u\frac{\partial T}{\partial x}+v\frac{\partial T}{\partial y}\right)=k_{nf}\frac{\partial^{2}T}{\partial y^{2}}-\frac{\partial q_{r}}{\partial y}-\mathcal{Q}_{0}\left(T-T_{\infty}\right)$$
(3)

u is the velocity components along the *x*-direction, *T* the temperature of the nanofluid, μ_{nf} the dynamic viscosity of the nanofluid, β_{nf} the thermal expansion coefficient of the nanofluid, ρ_{nf} the density of the nanofluid, k_{nf} the thermal conductivity of the nanofluid , $(\rho c_p)_{nf}$ the

heat capacitance of the nanofluid, Q_0 heat generation constant, g the acceleration due to gravity and q_r the radiative heat flux which are given as in Ref.[Choi (2001), Pak and Young (1998), Govindaraju et al. (2015)]

$$\mu_{nf} = \mu_f \left(1 + 39.11\phi + 533.9\phi^2 \right), \ \rho_{nf} = (1 - \phi)\rho_f + \phi\rho_s, (\rho c_p)_{nf} = (1 - \phi)(\rho c_p)_f + \phi(\rho c_p)_s, \ (\rho\beta)_{nf} = (1 - \phi)(\rho\beta)_f + \phi(\rho\beta)_s$$
(4)

where, ϕ is the solid volume fraction of the nanoparticle. The effective thermal conductivity of nanofluid is calculated by Patel et al. (2005) model as follows:

$$\frac{k_{nf}}{k_f} = 1 + \frac{k_s A_s}{k_f A_f} + ck_s Pe \frac{A_s}{k_f A_f}, \quad \frac{A_s}{A_f} = \frac{d_f}{d_s} \frac{\phi}{1 - \phi}, \quad Pe = \frac{u_s d_s}{\alpha_f}, \quad u_s = \frac{2k_b T}{\pi \mu_f d_s^2}, \\ c = 25,000$$

Where, ρ_f the density of the base fluid, ρ_s the density of the nanoparticle, k_f the thermal conductivity of the base fluid, k_s the thermal conductivity of the nanoparticle, Pe the Peclet number, α_f the thermal diffusivity of liquid, μ_f the viscosity of the base fluid, $(\rho c_p)_f$ the heat capacitance of the base fluid and $(\rho c_p)_s$ the heat capacitance of nanoparticles and c is constant.

The radiative heat flux for an optically thick fluid can be found from Rosseland (1931) approximation and its formula is derived from the diffusion concept of radiative heat transfer in the following way

$$q_r = -\frac{4\sigma^*}{3k_{nf}^*}\frac{\partial T^4}{\partial y}$$
(5)

where $\sigma^* (= 5.67 \times 10^{-8} W / m^2 K^4)$, $k^* (m^{-1})$ states 'Stefan-Boltzmann' constant, the Rosseland mean absorption coefficient respectively. It is

supposed that due to variation in temperature in the fluid flow domain are adequately very small and that T^4 may well derive as a linear function of temperature. Hence, this attained by elucidating T^4 in a Taylor series about T_{∞} , thus:

$$T^{4} = T_{\infty}^{4} + 4T_{\infty}^{3}(T - T_{\infty}) + 6T_{\infty}^{2}(T - T_{\infty})^{2} + --$$
(6)

Ignoring higher order terms in Eq. (6) beyond the first order in $(T - T_{\infty})$, we get

$$T^{4} \cong T_{\infty}^{4} + 4T_{\infty}^{3}(T - T_{\infty})$$

$$T^{4} \cong T_{\infty}^{4} + 4TT_{\infty}^{3} - 4T_{\infty}^{4}$$

$$T^{4} \cong 4TT_{\infty}^{3} - 3T_{\infty}^{4}$$
(7)

Considering the above equation, Eq. (3) becomes

$$\left(\rho c_{p}\right)_{rf}\left(u\frac{\partial T}{\partial x}+v\frac{\partial T}{\partial y}\right) = \left(k_{rf}+\frac{16\sigma^{*}T_{\infty}^{3}}{3k_{rf}^{*}}\right)\frac{\partial^{2}T}{\partial y^{2}}-Q_{0}(T-T_{\infty})$$
(8)

The boundary conditions of equations (1) to (3) are as follows

$$u = u_w(x) = ax, \quad v = 0, \ T = T_w \qquad \text{at} \quad y = 0$$
$$u \to 0, \qquad T \to T_{\infty}, \qquad \text{as} \quad y \to \infty \qquad (9)$$

The following similarity variables are also introduced

$$u = axf'(\eta), \ v = -\sqrt{av_f} f(\eta), \ \theta(\eta) = \frac{T - T_{\infty}}{T_w - T_{\infty}}, \ \eta = \sqrt{a/v_f} y$$

We get the following governing equations which are dimensionless.

$$f''' - Aa_1\left(\left(f'\right)^2 - ff''\right) - MAf' + \lambda Aa_2\theta = 0$$
⁽¹⁰⁾

$$\theta'' + \frac{3N \operatorname{Pr} a_3 k_f}{k_{nf} \left(3N+4\right)} f \,\theta' - \frac{3N \operatorname{Pr} k_f}{k_{nf} \left(3N+4\right)} \theta = 0 \tag{11}$$

The corresponding boundary conditions become

$$f = 0, \quad f' = 1, \quad \theta = 1 \quad \text{at } \eta = 0$$

$$f' \to \infty, \quad \theta = 0 \quad \text{as } \eta \to 0$$
(12)

where

$$a_{1} = \left[(1 - \phi) + \phi \left(\frac{\rho_{s}}{\rho_{f}} \right) \right], a_{2} = \left[(1 - \phi) + \phi \frac{(\rho \beta)_{s}}{(\rho \beta)_{f}} \right]$$
$$a_{3} = \left[(1 - \phi) + \phi \frac{(\rho c_{p})_{s}}{(\rho c_{p})_{f}} \right],$$

The dimensionless constants appearing in equations (10) and (11) are the magnetic parameter M, buoyancy parameter λ , viscosity ratio A, Prandtl number Pr, heat source parameter Q, and N is the radiation parameters which are defined as follows.

$$M = \frac{\sigma B_0^2}{a\rho_f}, \lambda = \frac{g\beta_f(T_w - T_w)}{au_w}, A = \frac{\mu_f}{\mu_{gf}}, \Pr = \frac{v_f(\rho C_p)_f}{k_f}, Q = \frac{Q_0}{a(\rho C_p)_f},$$
$$N = \frac{k_{nf}k_{nf}^*}{4\sigma^* T_w^3}$$

Skin-friction:

From velocity field, we study the skin-friction which is given in dimensionless form as follows:

$$C_f \operatorname{Re}_x^{\frac{1}{2}} = -\frac{1}{A} \left[\frac{\partial u}{\partial \eta} \right]_{\eta=0} = -\frac{1}{A} f''(0)$$
(13)

Nusselt Number:

From temperature field, we study the Nusselt number which is given in dimensionless form as follows:

$$Nu_{x} \operatorname{Re}_{x}^{-\frac{1}{2}} = -\frac{k_{nf}}{k_{f}} \left[\frac{\partial \theta}{\partial \eta} \right]_{\eta=0} = -\frac{k_{nf}}{k_{f}} \theta'(0)$$
(14)

Table 2 Comparison between the present solutions for various values of ϕ with previously published results when Pr=6.2, $N=Q=\lambda=0$

М	ϕ	Hamad (2011) (Cu-water)		Present Results (Cu-water)	
1		-f''(0)	<i>-θ</i> '(0)	-f''(0)	<i>-θ</i> '(0)
	0.05 0.1 0.2	1.4524 1.4657 1.4331	1.5237 1.3884 1.1670	1.45243 1.45842 1.43301	1.5236 1.3882 1.1653

3. RESULT AND DISCUSSIONS

The equations (10) and (11) with the boundary condition (12) were solved numerically by shooting method with Runge-Kutta fourth order scheme (MATLAB package). The impacts of various governing dimensionless parameters are examined, namely the magnetic parameter (*M*), buoyancy parameter (λ), radiation parameter (*N*), volume fraction parameter (ϕ), heat source/sink parameter (*Q*), Prandtl number (*Pr*) in transit of flow field, transverse velocity $f'(\eta)$, temperature $\theta(\eta)$ are studied graphically shown in Figs. 2-9. The values of the volume fraction of nanoparticles are taken in the range of $0 \le \phi \le 0.2$.

The behavior of velocity and temperature by the influence of nanoparticles, magnetic parameter, buoyancy parameter, radiation parameter, heat source/sink parameter and volume fraction are illustrated in Figs. 2-9. In Fig. 2 reveals that the effect of volume fraction of nanoparticles on the fluid velocity, it increases due to the absence of surface tension forces and hence, the momentum boundary layer thickness increases. The higher value of volume fraction obtained for CuO–ethylene glycol 50% than MgO-ethylene glycol 50% can be attributed to the higher value of copper ionic radius (0.121nm) than the magnesium ionic radius (0.072nm). From Fig. 3, it is observed that the effect of volume fraction of nanoparticles of the temperature distribution metallic nanoparticles has much higher heat conductivity than common liquids. It also observed that with the increasing volume fraction of nanoparticles the thermal boundary layer increases.

In Fig. 4 depicts that the velocity profiles for the various magnetic parameter. It is observed that an increase in magnetic parameter the velocity decreases. It is due to the fact that the application of transverse magnetic field will result in a Lorentz force similar to drag force, which tends to resist the fluid flow and thus reducing its velocity and it is also noticed that the momentum boundary layer thickness increases with increasing value of the magnetic parameter. Physically it is seen that when any fluid is subjected to a magnetic field than the viscosity rises. The results of which is that the fluid's capacity to transfer force can be restricted with help of an electromagnet which gives rise to its various possible control-based applications including MHD ion propulsion, electromagnetic tossing of meats, MHD control time etc. The different values of the magnetic parameter obtained for CuO - ethylene glycol 50% and MgO- ethylene glycol 50% can be attributed to the higher value of the magnetic moment of copper ions than that of the magnetic moment of non-magnetic magnesium ions.

From Fig. 5 represents the variation of the nanofluid temperature of the magnetic parameter. It is observed that an increase in magnetic parameter the temperature increases. Owing to the nanofluid has thick thermal boundary layer and also, temperature increments in the nanofluid due to its high thermal conductivity. The temperature distribution of CuO – ethylene glycol 50% is greater than that of MgO- ethylene glycol 50%. This can be attributed to the higher value of the magnetic moment of copper ions than that of the magnetic moment of non-magnetic magnesium ions on applying the increasing value of magnetic field. The higher magnetic dipole moment occurred due to an increase of magnetic field in case of copper ions. This, in turn, increases the higher temperature distribution than the magnesium ions.



Fig. 2 Velocity profile for different ϕ



Fig. 3 Temperature profile for different ϕ



Fig. 4 Velocity profile for different *M*



Fig. 5 Temperature profile for different M



Fig. 6 Velocity profile for different *N*

In Fig. 6, the nanofluid velocity decreases with the increasing values of radiation parameter N. It is noted that the momentum of boundary layer thickness decreases when N tends to decrease inside a boundary layer region and consequently it accelerates the viscosity of the nanofluid. Physically, the presence of thermal radiative parameter implies to more heat absorbs the liquid that compares to low velocity. CuO – ethylene glycol 50% is greater than that of MgO- ethylene glycol 50% owing to high thermal conductivity than magnesium oxide.



Fig. 7 Temperature for different N



Fig. 8 Velocity profile for different λ



Fig. 9 Temperature profile for different *Q*

From Fig. 7 it is observed that the nanofluid temperature decreases as N decreases; it is due to the fact that the conduction effect of the nanofluids decreases in the presence of thermal radiation. Therefore, higher values of radiation parameter incriminate higher surface heat flux and so, decrease the temperature within the boundary layer region, this leads to an increase in the heat transfer rate. The radiation parameter of CuO – ethylene glycol 50% are decreasing slower than that of MgOethylene glycol 50% which can be attributed to the high thermal conductivity of copper oxide than magnesium oxide. For large values of R, it is pointed out that, the temperature decreases more rapidly with the increase of R, therefore, using radiation we can control the temperature distribution and flow transport, these types of applications can be used in pseudoscientific alternative medicine to control blood pressure through the process of magneto therapy.

From Fig. 8 depicts that the velocity profiles for CuO – ethylene glycol 50% and MgO-ethylene glycol 50%. Since the momentum boundary layer thickness increases with increasing values of buoyancy parameter enabling more flow. The effect of heat source parameter on the temperature field is shown in Fig. 9. It is noticed that the temperature of the fluid decreases with different values of heat source parameter. In the case of heat absorption, the absorbed heat by the nanofluid causes to decrease of more number of energy levels. Thus, decreases the temperature of the nanofluid.

4. CONCLUSION

Investigation of the MHD natural convective boundary-layer flow of a nanofluid and heat transfer over a stretching sheet considering the thermal radiation and heat source effects was represented in this paper. The resulting system of nonlinear partial differential equations is solved numerically by shooting method with Runge-Kutta fourth order scheme (MATLAB package). The effects of various parameters on velocity and temperature profiles are studied through graphs and table. The following conclusions have arrived:

- The velocity and temperature of the nanofluid increases with increasing of volume fraction parameter.
- The nanofluid velocity decreases as the existence of the magnetic field parameter becomes stronger
- The velocity and temperature of the nanofluid decreases with increasing of radiation parameter.
- The temperature of the nanofluid decreases with increasing of heat absorption parameter.

The present study has numerous applications involving heat transfer and other applications such as chemical sensors, biological applications, glass, solar energy transformation, electronics, petrochemical products, light-weight, heat-insulating and refractory fiberboard and metallic ceramics etc.

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